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Source / Izvornik: Physical Review C - Nuclear Physics, 1999, 60, 51302 - 4

Journal article, Published version Rad u časopisu, Objavljena verzija rada (izdavačev PDF)

https://doi.org/10.1103/PhysRevC.60.051302

Permanent link / Trajna poveznica: https://urn.nsk.hr/urn:nbn:hr:217:440104

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Transitional Lu and spherical Ta ground-state proton emitters in the relativistic Hartree-Bogoliubov model

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(Received 7 July 1999; published 1 October 1999)

Properties of transitional Lu and spherical Ta ground-state proton emitters are calculated with the relativistic Hartree-Bogoliubov model. The NL3 effective interaction is used in the mean-field Lagrangian, and pairing correlations are described by the pairing part of the finite range Gogny interaction D1S. Proton separation energies, ground-state quadrupole deformations, single-particle orbitals occupied by the odd valence proton, and the corresponding spectroscopic factors are compared with recent experimental data, and with results of the macroscopic-microscopic mass model. [S0556-2813(99)51011-X]

PACS number(s): 21.60.Jz, 21.10.Dr, 23.50.+z, 27.60+j

The structure and decay modes of nuclei beyond the proton drip line represent one of the most active areas of experimental and theoretical studies of exotic nuclei with extreme isospin values. In the last few years many new data on ground-state and isomeric proton radioactivity have been reported. In particular, detailed studies of odd-Z ground-state proton emitters in the regions $51 \le Z \le 55$ and $69 \le Z \le 83$ have shown that the systematics of spectroscopic factors is consistent with half-lives calculated in the spherical WKB or distorted-wave Born (DWBA) approximations [1,2]. More recent data [3,4] indicate that the missing region of light rare-earth nuclei contains strongly deformed systems at the drip lines.

In the theoretical description of ground-state and isomeric proton radioactivity, two essentially complementary approaches have been reported. One possibility is to start from a spherical or deformed phenomenological single-particle potential, a Woods-Saxon potential, for instance, and to adjust the parameters of the potential well in order to reproduce the experimental one-proton separation energy. The width of the single-particle resonance is then determined by the probability of tunneling through the Coulomb and centrifugal barriers. Since the probability strongly depends on the valence proton energy and on its angular momentum, the calculated half-lives provide direct information about the spherical or deformed orbital occupied by the odd proton. For a spherical proton emitter it is relatively simple to calculate half-lives in the WKB or DWBA approximations [2]. On the other hand, it is much more difficult to quantitatively describe the process of three-dimensional quantum mechanical tunneling for deformed proton emitters. Modern reliable models for calculating proton emission rates from deformed nuclei have been developed only recently [4,5]. A shortcoming of this approach is that it does not predict proton separation energies, i.e., the models do not predict which nuclei are likely to be proton emitters. In fact, if they are used to calculate decay rates for proton emission from excited states, the depth of the central potential has to to be adjusted for each proton orbital separately. In addition, the models of Refs. [2,4,5] do not provide any information about the spectroscopic factors of the proton orbitals. Instead, experimental spectroscopic factors are defined as ratios of calculated and

measured half-lives, and the deviation from unity is attributed to nuclear structure effects.

In Refs. [6-8] we have used the relativistic Hartree-Bogoliubov (RHB) theory to calculate properties of protonrich spherical even-even nuclei with $14 \le Z \le 28$, and to describe odd-Z deformed ground-state proton emitters in the region $53 \le Z \le 69$. RHB presents a relativistic extension of the Hartree-Fock-Bogoliubov theory, and it provides a unified framework for the description of relativistic mean-field and pairing correlations. Such a unified and self-consistent formulation is especially important in applications to dripline nuclei. The RHB framework has been used to study the location of the proton drip line, the ground-state quadrupole deformations and one-proton separation energies at and beyond the drip line, the deformed single particle orbitals occupied by the odd valence proton, and the corresponding spectroscopic factors. The results of fully self-consistent calculations have been compared with experimental data on ground-state proton emitters. However, since it is very difficult to use the self-consistent ground-state wave functions in the calculation of proton emission rates, one could say that the RHB model provides information that is complementary to that obtained with the models of Refs. |2,4,5|. It should be noted that in the relativistic framework the strength and the shape of the spin-orbit term are determined self-consistently. This is essential for a correct description of spin-orbit splittings in regions of nuclei far from stability, where the extrapolation of effective strength parameters becomes questionable. The motivation for the present work is the very recent data on proton emission from the closed neutron shell nucleus ¹⁵⁵Ta [9], and the proposed experiment to search for direct proton emission from ¹⁴⁹Lu [10]. The analysis of ground-state proton radioactivity in the Lu and Ta isotopes completes our study of deformed and transitional proton emitters in the region $53 \le Z \le 73$.

A very detailed description of the relativistic Hartree-Bogoliubov theory can be found, for instance, in Ref. [7]. In the following we only outline the essential features of the model that will be used to describe nuclei at the proton drip line. The ground state of a nucleus is represented by the Slater determinant of independent single-quasiparticle states, which are obtained as solutions of the relativistic Hartree-Bogoliubov equations G. A. LALAZISSIS, D. VRETENAR, AND P. RING

$$\begin{pmatrix} \hat{h}_D - m - \lambda & \hat{\Delta} \\ -\hat{\Delta}^* & -\hat{h}_D + m + \lambda \end{pmatrix} \begin{pmatrix} U_k(\mathbf{r}) \\ V_k(\mathbf{r}) \end{pmatrix} = E_k \begin{pmatrix} U_k(\mathbf{r}) \\ V_k(\mathbf{r}) \end{pmatrix}.$$
(1)

The column vectors denote the quasiparticle spinors, and E_k are the quasiparticle energies. In the Hartree approximation for the self-consistent mean field, the single-nucleon Dirac Hamiltonian reads

$$\hat{h}_{D} = -i\alpha \cdot \nabla + \beta (m + g_{\sigma}\sigma(\mathbf{r})) + g_{\omega}\tau_{3}\omega^{0}(\mathbf{r}) + g_{\rho}\rho^{0}(\mathbf{r}) + e \frac{(1 - \tau_{3})}{2} A^{0}(\mathbf{r}).$$
(2)

It describes the motion of independent Dirac nucleons in the mean-field potentials: the isoscalar scalar σ -meson potential, the isoscalar vector ω meson, and the isovector vector ρ -meson potential. The photon field A accounts for the electromagnetic interaction. The meson potentials are determined self-consistently by the solutions of the corresponding Klein-Gordon equations. The source terms for these equations are calculated in the *no-sea* approximation. Because of charge conservation, only the third component of the isovector ρ meson contributes. For an even-even system, due to time reversal invariance, the spatial vector components ω , ρ_3 , and A of the vector meson fields vanish. In nuclei with odd numbers of protons or neutrons, time reversal symmetry is broken. The odd particle induces polarization currents and the time-odd components in the meson fields. These components play an essential role in the description of magnetic moments and of moments of inertia in rotating nuclei. However, their effect on deformations and binding energies is very small and can be neglected to a good approximation. As in our previous studies of nuclei at the proton drip lines, we choose the NL3 set of meson masses and meson-nucleon coupling constants [11] for the effective interaction in the particle-hole channel: m = 939 MeV, $m_{\sigma} = 508.194$ MeV, $m_{\omega} = 782.501$ MeV, $m_{\rho} = 763.0$ MeV, $g_{\sigma} = 10.217$, g_2 $= -10.431 \text{ fm}^{-1}$, $g_3 = -28.885$, $g_{\omega} = 12.868$, and g_{ρ} =4.474.

The pairing field $\hat{\Delta}$ is defined as

$$\Delta_{ab}(\mathbf{r},\mathbf{r}') = \frac{1}{2} \sum_{c,d} V_{abcd}(\mathbf{r},\mathbf{r}') \boldsymbol{\kappa}_{cd}(\mathbf{r},\mathbf{r}'), \qquad (3)$$

where $V_{abcd}(\mathbf{r},\mathbf{r}')$ are matrix elements of a two-body pairing interaction, and $\kappa_{cd}(\mathbf{r},\mathbf{r}')$ is the pairing tensor. The pairing part of the phenomenological Gogny force

$$V^{pp}(1,2) = \sum_{i=1,2} e^{-((\mathbf{r}_{1} - \mathbf{r}_{2})/\mu_{i})^{2}} \times (W_{i} + B_{i}P^{\sigma} - H_{i}P^{\tau} - M_{i}P^{\sigma}P^{\tau}), \quad (4)$$

with the set D1S [12] for the parameters μ_i , W_i , B_i , H_i , and M_i (*i*=1,2), is used to describe pairing correlations.

The RHB single-quasiparticle equations (1) are solved self-consistently. The iteration procedure is performed in the quasiparticle basis. The chemical potential λ has to be deter-

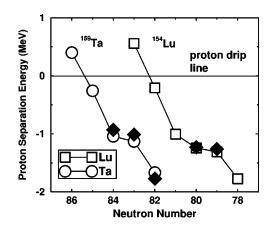


FIG. 1. Proton separation energies for Lu and Ta isotopes at and beyond the drip line. Results of self-consistent RHB calculations are compared with experimental transition energies for ground-state proton emission in ¹⁵⁰Lu, ¹⁵¹Lu [13], ¹⁵⁵Ta [9], ¹⁵⁶Ta [14], and ¹⁵⁷Ta [15]. The filled diamonds denote the negative values of the transition energies E_p .

mined by the particle number subsidiary condition so that the expectation value of the particle number operator in the ground state equals the number of nucleons. A simple blocking prescription is used in the calculation of odd-proton and/or odd-neutron systems. The blocking calculations are performed without breaking the time-reversal symmetry. The resulting eigenspectrum is transformed into the canonical basis of single-particle states, in which the RHB ground state takes the BCS form. The transformation determines the energies and occupation probabilities of the canonical states.

The one-proton separation energies

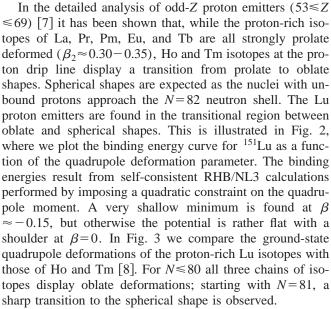
$$S_p(Z,N) = B(Z,N) - B(Z-1,N)$$
 (5)

for the Lu and Ta isotopes are displayed in Fig. 1, as a function of the number of neutrons. The predicted drip-line nuclei are ¹⁵⁴Lu and ¹⁵⁹Ta. In the process of proton emission the valence particle tunnels through the Coulomb and centrifugal barriers, and the decay probability depends strongly on the energy of the proton and on its angular momentum. In rare-earth nuclei the decay of the ground-state by direct proton emission competes with β^+ decay; for heavy nuclei fission or α decay can also be favored. In general, ground-state proton emission is not observed immediately after the drip line. For small values of the proton separation energies, the width is dominated by the β^+ decay. On the other hand, large separation energies result in extremely short protonemission half-lives, which are difficult to observe experimentally. For a typical rare-earth nucleus, the separation energy window, in which ground-state proton decay can be directly observed, is about 0.8–1.7 MeV [2]. In Fig. 1 we have compared the calculated separation energies with experimental transition energies for ground-state proton emission in ¹⁵⁰Lu, ¹⁵¹Lu [13], ¹⁵⁵Ta [9], ¹⁵⁶Ta [14], and ¹⁵⁷Ta [15]. In all five cases an excellent agreement is observed between model predictions and experimental data. In addition to ¹⁵¹Lu, which was the first ground-state proton emitter to be discovered [16], and ¹⁵⁰Lu, the self-consistent RHB

TABLE I. Lu ground-state proton emitters. The results of the RHB calculation for the one-proton separation energies S_p , quadrupole deformations β_2 , and the deformed single-particle orbitals occupied by the odd valence proton, are compared with predictions of the macroscopic-microscopic mass model, and with the experimental transition energies. All energies are in units of MeV; the RHB spectroscopic factors are displayed in the sixth column.

	Ν	S_p	$oldsymbol{eta}_2$	p orbital	u^2	Ω_p^{π} [17]	S_p [17]	β_{2} [18]	E_p expt.
¹⁴⁹ Lu	78	-1.77	-0.158	7/2 ⁻ [523]	0.60	$5/2^{-}$	-1.51	-0.175	
¹⁵⁰ Lu	79	-1.31	-0.153	7/2 ⁻ [523]	0.61	$5/2^{-}$	-1.00	-0.158	1.261(4) [13]
¹⁵¹ Lu	80	-1.24	-0.151	7/2 ⁻ [523]	0.58	$7/2^{-}$	-0.99	-0.150	1.233(3) [13]

calculation predicts ground-state proton decay in ¹⁴⁹Lu. The calculated one-proton separation energy -1.77 MeV corresponds to a half-life of a few μ s, if one assumes that the nucleus is spherical. Direct proton emission with a half-life of the order of a few μ s is just above the lower limit of observation of current experimental facilities. An experiment to search for direct proton emission from ¹⁴⁹Lu has been proposed recently [10]. For the Lu ground-state proton emitters, in Table I the results of the RHB model calculation are compared with the predictions of the finite-range droplet mass model (FRDM): the projection of the odd-proton angular momentum on the symmetry axis and the parity of the odd-proton state Ω_p^{π} [17], the one-proton separation energy [17], and the ground-state quadrupole deformation [18]. We have also included the RHB spectroscopic factors, and compared the separation energies with the experimental transition energies in ¹⁵⁰Lu and ¹⁵¹Lu. Both theoretical models predict oblate shapes for the Lu proton emitters, and similar values for the ground-state quadrupole deformations. On the other hand, while the FRDM assigns spin and parity $5/2^-$ to the deformed single-particle orbitals occupied by the odd valence proton in all three proton emitters, the RHB model predicts the $7/2^{-}$ [523] Nilsson orbital to be occupied by the odd proton. We also notice that the RHB separation energies are much closer to the experimental values. The spectroscopic factors of the $7/2^{-}[523]$ orbital are displayed in the sixth column of Table I. The spectroscopic factor of the deformed odd-proton orbital k is defined as the probability that this state is found empty in the daughter nucleus with even number of protons.

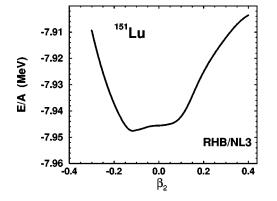


The proton-rich Ta isotopes are spherical. In Fig. 1 we compare the calculated one-proton separation energies with experimental transition energies for ¹⁵⁵Ta [9], ¹⁵⁶Ta [14], and ¹⁵⁷Ta [15]. The predictions for the spherical orbitals occupied by the odd proton and the corresponding spectroscopic factors are displayed in Table II. Results of the FRDM calculation [17] have also been included in the comparison. As in the case of the Lu ground-state proton emitters, an excellent agreement between RHB separation energies and experimental data on transition energies for proton emission is observed. In particular, our calculation reproduces the very recent data on proton emission from the

Z=69

 \mathbf{N}

82



-0.1 β, **RHB/NL3** -0.2 78 80 Neutron number

0.0

FIG. 2. Potential energy curve for ¹⁵¹Lu. The self-consistent RHB calculations are performed with constrained quadrupole deformation.

FIG. 3. Self-consistent ground-state quadrupole deformations for Ho, Tm, and Lu isotopes, at and beyond the proton drip line.

TABLE II. Spherical Ta ground-state proton emitters. RHB results for the proton separation energies, the single-particle orbitals occupied by the odd proton, and the corresponding spectroscopic factors are compared with the predictions of the finite-range droplet mass model (FRDM) and with experimental data.

		RHB/NL3	FRDM [17]	Expt.
¹⁵⁵ Ta	S_p	-1.677	-1.09	-1.765(10) [9]
	J^{π}	$h \ 11/2^{-}$	9/2 -	11/2 -
	spectr. factor	0.60		0.58(20)
¹⁵⁶ Ta	S_p	-1.129	-0.60	-1.007(5) [14]
	J^{π}	$d \ 3/2^+$	3/2 -	3/2+
	spectr. factor	0.51		
¹⁵⁷ Ta	S_p	-1.040	-0.48	-0.927(7) [15]
	J^{π}	$h \ 11/2^{-}$	9/2 -	$1/2^{+}$
	spectr. factor	0.42		0.56(24)

closed neutron shell nucleus ¹⁵⁵Ta [9]. The significant decrease in proton binding for ¹⁵⁵Ta, as compared to ^{157,156}Ta, has been associated with the N=82 closure. In comparison, the FRDM results are found to be in rather poor agreement with experimental data. Except for ¹⁵⁷Ta, the spherical orbitals predicted to be occupied by the odd proton agree with the experimental assignments, and the theoretical spectroscopic factor of the $h_{11/2}$ orbital in ¹⁵⁵Ta is very close to the experimental value. For ¹⁵⁷Ta, the RHB model predicts ground-state proton emission from the $h_{11/2}$ orbital. The experimental assignment for the ground-state configuration is $s_{1/2}$, but an alpha decaying state is identified in ¹⁵⁷Ta at an excitation energy of only 22(5) keV and assigned to an $h_{11/2}$ isomer [15]. We have also calculated the one-proton separa-

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tion energy for ¹⁵⁶Ta^{*m*}: $S_p = -1.250$ MeV; the orbital is $h_{11/2}$ and the spectroscopic factor is 0.79. This is to be compared with the experimental transition energy $E_p = 1.103(12)$ MeV [19], assigned to the $h_{11/2}$ orbital with the experimental spectroscopic factor 0.92(4) [1].

In conclusion, the relativistic Hartree-Bogoliubov model has been applied in the description of ground-state properties of transitional Lu and spherical Ta proton emitters. The NL3 effective interaction has been used for the mean-field Lagrangian, and pairing correlations have been described by the pairing part of the finite range Gogny interaction D1S. We would like to emphasize that this particular combination of effective forces has been used in most of our recent applications of the RHB model, not only for spherical and deformed β -stable nuclei, but also for nuclear systems with large isospin values on both sides of the valley of β stability. The model parameters therefore have not been adjusted to the specific properties of nuclei studied in this work, or to the properties of deformed proton emitters discussed in Refs. [7,8]. The self-consistent calculation reproduces in detail the observed transition energies for ground-state proton emission in 150 Lu, 151 Lu [13], 155 Ta [9], 156 Ta [14], and 157 Ta [15], as well as the assignments for the orbitals occupied by the valence odd proton and the corresponding spectroscopic factors. The model also predicts the one-proton separation energy of -1.77 MeV for the possible proton emitter ¹⁴⁹Lu. Oblate ground-state deformations are predicted for all Lu proton emitters, while spherical shapes are calculated for the Ta isotopes at and beyond the proton drip line. With the excellent agreement observed between the RHB results and the very recent data on proton emission from the closed neutron shell nucleus ¹⁵⁵Ta [9], we complete our study of ground-state properties of deformed and transitional proton emitters [7,8].

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