# **Transverse single-spin asymmetry and cross section for π0 and η mesons at large Feynman x in p↑+p collisions at √s=200 GeV**

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#### PHYSICAL REVIEW D 86, 051101(R) (2012)

## Transverse single-spin asymmetry and cross section for  $\bm{\pi}^0$  and  $\bm{\eta}$  mesons at large Feynman  $x$  in  $p^{\dagger} + p$  collisions at  $\sqrt{s} = 200 \text{ GeV}$

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Measurements of the differential cross section and the transverse single-spin asymmetry,  $A_N$ , vs  $x_F$  for  $\pi^0$  and  $\eta$  mesons are reported for  $0.4 \lt x_F \lt 0.75$  at an average pseudorapidity of 3.68. A data sample of approximately 6.3 ph<sup>-1</sup> was applyzed which was recorded during  $p_1^{\dagger} + p_2$  collisions at  $\sqrt{5} = 200$  GeV approximately 6.3 pb<sup>-1</sup> was analyzed, which was recorded during  $p^{\dagger} + p$  collisions at  $\sqrt{s} = 200$  GeV by

<span id="page-2-0"></span>[\\*D](#page-1-0)eceased.

the STAR experiment at RHIC. The average transverse beam polarization was 56%. The cross section for  $\pi^0$ , including the previously unmeasured region of  $x_F > 0.55$ , is consistent with a perturbative QCD prediction, and the  $\eta/\pi^0$  cross-section ratio agrees with existing midrapidity measurements. For 0.55  $\leq$  $x_F < 0.75$ , the average  $A_N$  for  $\eta$  is 0.210  $\pm$  0.056, and that for  $\pi^0$  is 0.081  $\pm$  0.016. The probability that these two asymmetries are equal is  $\sim$ 3%.

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A well-known prediction of collinearly factorized perturbative quantum chromodynamics (pQCD) is that the cross section for forward meson production in proton-proton collisions should have negligible dependence on the transverse polarization of the incident proton [\[1](#page-7-0)]. This early prediction was contradicted by measurements [[2–](#page-7-1)[6](#page-7-2)] of sizable pion transverse single-spin asymmetries  $(A<sub>N</sub>)$ , defined for a forward moving polarized beam scattering to the left and with a vertical spin quantization axis as

$$
A_N \equiv \frac{\sigma^{\dagger} - \sigma^{\dagger}}{\sigma^{\dagger} + \sigma^{\dagger}}.
$$
 (1)

In order to explain the large asymmetries, several extensions of the pQCD collinear framework have been proposed. These approaches take into account the possible spin-dependent transverse components of parton momentum (Sivers effect [[7](#page-7-3)]), the possible spin-dependent fragmentation of a scattered polarized parton (Collins effect [\[8\]](#page-7-4)), or higher-twist effects where transverse momenta related to the previous approaches are included in the hard scattering term of a collinear calculation [\[9](#page-7-5)[–11\]](#page-7-6). A wide range of high energy polarized experiments, both nucleon-nucleon  $[12-14]$  $[12-14]$  and lepton-nucleon  $[15-18]$  $[15-18]$  $[15-18]$ , have been performed to characterize the kinematic and process dependences of the asymmetries, and in the case of the latter, to directly test these approaches.

For more than 20 years, we have known that the transverse asymmetries in forward pion production depend critically on the isospin projection  $(I_3)$  of the produced mesons relative to that of the parent hadron. In proton scattering experiments, the asymmetry for the  $\pi^-$  meson, which contains a down quark and an anti-up quark, has the opposite sign relative to the asymmetries for the  $\pi^+$  and  $\pi^0$ mesons, produced from the predominant up quarks.

In this paper, we report for the first time at  $\sqrt{s} = 200 \text{ GeV}$ <br>Extensive single-spin asymmetry for the *n* meson the transverse single-spin asymmetry for the  $\eta$  meson, another member of the pseudoscalar octet that has the same isospin projection as the  $\pi^0$  ( $I_3 = 0$ ). We note that the FNAL-E704 Collaboration previously found a large  $A_N$ for the  $\eta$  for Feynman-x (longitudinal momentum of the observed particle divided by the beam energy)  $>0.4$  at  $\sqrt{s} = 19.4$  GeV [[19\]](#page-7-11). In addition, we report the differential cross section for *n* production in the region where the spin cross section for  $\eta$  production in the region where the spin asymmetry is measured.

Leading-twist collinear pQCD has been successful in describing a wide range of unpolarized cross-section measurements at the Relativistic Heavy Ion Collider (RHIC), from  $\pi^0$  at forward rapidity [[20](#page-7-12),[21\]](#page-7-13), to  $\pi^0$ [[22](#page-7-14)–[25](#page-7-15)],  $\eta$  [[25–](#page-7-15)[27\]](#page-7-16),  $\pi^{\pm}/K^{\pm}$  [[28\]](#page-7-17), and jets [\[29](#page-7-18)] at midrapidity. Such agreement is considered a strong indicator that the given process can be interpreted within the framework of pQCD. Therefore, the comparison between the unpolarized cross section and the leading-twist collinear pQCD prediction becomes the basis on which to apply the aforementioned theoretical extensions to the associated transverse spin effects.

For forward  $\pi^0$  production, recent STAR measurements of the cross section are consistent with next-to-leadingorder (NLO) pQCD calculations in the same region where a large transverse spin asymmetry is found [\[20,](#page-7-12)[21\]](#page-7-13). However, these results do not cover the large Feynman- $x$  $(x_F)$  region where the acceptance for the  $\eta$  decaying into two photons becomes large. In this paper, we have extended the analysis of the  $\pi^0$  cross section and  $A_N$  to  $x_F$  of 0.75, where its spin asymmetry and cross section can be directly compared to those of the  $\eta$  mesons.

The data were taken with the STAR forward pion detector (FPD). The FPD is a modular lead glass calorimeter located at forward rapidity in the STAR interaction region at RHIC at Brookhaven National Laboratory. Two modules were placed on either side of the beam line, covering the pseudorapidity region from approximately 3.3 to 4.0. Each module contained 49 cells (glass blocks approximately 18 radiation lengths deep), forming a  $7 \times 7$  square array. The data were collected in 2006 with transversely polarized proton beams and an integrated luminosity of  $\sim 6.3$  pb<sup>-1</sup>. The average polarization was  $(56.0 \pm 2.6)\%$  for the beam<br>facing the EPD. As A<sub>xi</sub> is a single-spin observable, the spin facing the FPD. As  $A_N$  is a single-spin observable, the spin state of the second beam [with  $(55.0 \pm 2.6)\%$  polarization]<br>was integrated over for the  $A_{\rm M}$  at positive  $x_{\rm F}$ . At negative was integrated over for the  $A_N$  at positive  $x_F$ . At negative  $x_F$ , the spin state of the first beam was integrated over. Events were recorded only when the total analog-to-digital convertor count in either of the two modules was greater than a fixed threshold, which was nominally equivalent to 30 GeV. Photons reconstructed within a quarter of a cell from the detector edge were discarded. Only those events with exactly two reconstructed photons were analyzed, with the resulting loss of yield corrected for the crosssection measurement. The STAR beam beam counter (BBC) on the away side was used to reject the singlebeam background. The near side BBC was not required to produce a signal, as most of the analyzed events already had more than half the beam energy deposited in the FPD. The efficiency for the away side BBC condition

was estimated to be  $(93 \pm 4)\%$  for all nonsingly diffractive<br>events based on previous analyses  $[30]$ events based on previous analyses [[30](#page-7-19)].

The  $x_F$  coverage of the previous analysis of  $A_N(\pi^0)$  [[12\]](#page-7-7), which included this data set, was limited by the difficulty in separating  $\pi^0$  clusters from single photons with  $x_F > 0.55$ . At this point, the typical separation of two  $\pi^0$  decay photons at the surface of the FPD becomes similar to the Molière radius of the lead glass  $(3.32 \text{ cm})$  and transverse cell size (3.81 cm). On the other hand, the  $\eta$  meson acceptance lies mostly above an  $x_F$  of 0.5 due to the larger separation of its decay photons.

With the current analysis, the  $\pi^0$ - $\gamma$  separation has been greatly improved by analyzing  $\sigma_{\text{Log}}$ , defined as

$$
\sigma_{\text{Log}} = \sqrt{\frac{\sum_{i} \text{Log}[(E_i + E_0)/\text{GeV}] \cdot (\bar{x} - x_i)^2}{\sum_{i} \text{Log}[(E_i + E_0)/\text{GeV}]}},
$$
(2)

where  $E_i$  and  $x_i$  are the energy and the location of the *i*th channel, and  $E_0 = 0.5$  GeV. The *i*th term in the sum is skipped if  $\text{Log}(E_i + E_0)$  < 0. It provides a significant sensitivity to the topological differences between single and double photon clusters at high energies, as evidenced by the clear separation between the one and two photon peaks in Fig. [1](#page-4-0). Also shown are the results from PYTHIA and GEANT simulations, which closely reproduce the  $\sigma_{\text{Log}}$  distributions for both types of clusters up to a small offset ( $\sim$  1% of the transverse cell size). As a result, the  $x_F$ coverage for  $\pi^{0}$ 's was extended from 0.55 to 0.75.

In addition, the GEANT simulation of the electromagnetic shower in the FPD is now based on the tracking of optical photons produced by the Cherenkov effect. Compared to the previous method based on charged particle energy loss, the new simulation produces a better agreement with the data on shower shape, energy resolution, and the observed shift in gain as a function of photon energy. Combined with

<span id="page-4-0"></span>

FIG. 1 (color online). The distribution of  $\sigma_{\text{Log}}$ , as defined in the text, for  $E_{\text{cluster}} > 65$  GeV for data and simulation, in units of FPD transverse cell size (3.81 cm). For comparison, the one and two photon cluster peaks from simulation were independently normalized and uniformly shifted by  $+0.01$  transverse cell size (1 bin) to account for the small difference in the average size of clusters between simulation and data.

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a more advanced parameterization of the shower shape including the effects of incident angle, it allows for a higher precision calibration needed for the cross-section measurement.

The top two panels of Fig. [2](#page-4-1) show data-simulation comparisons of the diphoton invariant mass spectra. The "center cut," so named because it covers roughly the central region of the FPD acceptance, is imposed on all event samples in order to enhance the  $\eta$  meson acceptance relative to the background. It is defined as

$$
(\eta_{\gamma\gamma} - 3.65)^2 + \tan^2(\phi_{\gamma\gamma}) < 0.15,\tag{3}
$$

<span id="page-4-2"></span>where  $\eta_{\gamma\gamma}$  is the pseudorapidity of the diphoton center of mass relative to the polarized beam, and  $\phi_{\gamma\gamma}$  is its azimuthal angle. The distributions of  $\pi^0$  and  $\eta$  events in the FPD, and the subset of each that passes the center cut are shown in Fig. [3.](#page-5-0) A full simulation based on PYTHIA 6.222 and GEANT 3 was compared to the data. The reflectivity and absorption properties of the aluminized mylar wrapped glass blocks were varied to minimize the discrepancies between the photon shower shape in the simulation and that measured in the data. While detailed knowledge of the glass-mylar interface remains a limiting factor in the

<span id="page-4-1"></span>

<span id="page-4-3"></span>FIG. 2 (color online). (a) Diphoton invariant mass,  $M_{\gamma\gamma}$ , distributions in data and simulation for  $E_{\gamma\gamma} > 45$  GeV, with the "center cut" as defined in Eq.  $(3)$  $(3)$  $(3)$ . The simulation results were normalized to have the same number of events as the data in the  $\pi^0$  mass region (0.08  $\lt M_{\gamma\gamma} \lt 0.19$  GeV/c<sup>2</sup>). The symbol  $\langle \eta \rangle$ indicates the average pseudorapidity of the photon pair. (b) Same as (a), but plotted using an expanded linear scale to illustrate the  $\eta$ mass region. For the dashed line, the  $\eta$  signal was removed from the simulation at the PYTHIA level. (c)  $A_N$  vs  $M_{\gamma\gamma}$  for the above mass distribution. The error bars are statistical uncertainties only.

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<span id="page-5-0"></span>

FIG. 3. Pseudorapidity vs tangent of the azimuthal angle of the diphoton center of mass, for  $E_{\gamma\gamma} > 50$  GeV. Left: 0.08 <  $M_{\gamma\gamma}$  < 0.19 GeV/c<sup>2</sup>. Right: 0.45  $\lt M_{\gamma\gamma}$  < 0.65 GeV/c<sup>2</sup>. The filled boxes indicate events that pass the center cut [Eq. [\(3\)](#page-4-2)].

precise modeling of the shower development, the agreement in the widths of mass peaks between the simulation and data has been improved significantly over previous analyses [\[12,](#page-7-7)[20](#page-7-12),[21](#page-7-13)]. Furthermore, the data-simulation agreement in the continuum region between the  $\pi^0$  and  $\eta$  peaks is very good, allowing for a simulation-based background estimation for the  $\eta$  signal. Corrections for the remaining data-simulation discrepancies in mass resolution were applied to the cross-section measurements. The  $\eta$  to  $\pi^0$  cross-section ratio in the simulation has been set at 0.45 to be consistent with the data. The bottom panel of Fig. [2](#page-4-1) shows the invariant mass dependence of  $A_N$ , which exhibits a suppression in the continuum region. Within the large statistical uncertainty, the asymmetry for this region does not show a significant  $x_F$  dependence. In the simulation, this mass region is dominated by approximately equal contributions from a pair of photons from two different  $\pi^0$ decays, and a charged hadron combined with a photon.

The energy resolution of the FPD is estimated to be about 7%–8% of the total energy based on the comparison of invariant mass and diphoton separation distributions between data and Cherenkov shower simulation. Coupled to the rapidly falling cross section in energy, more than half of events in any measured energy bin originate from lower true energy bins. For the cross-section measurements, we unfolded the energy smearing by applying the Bayesian iterative method [[31](#page-7-20)] to the smearing matrices obtained from the simulation. The unfolding procedure combines the statistical and systematic uncertainties from the original data points.

The upper panel of Fig. [4](#page-5-1) shows the differential cross sections for  $\pi^{\hat{0}}$  and  $\eta$ . The center cut [Eq. [\(3](#page-4-2))] was imposed on both mesons. Full pythia  $+$  geant simulations were used to obtain the detector efficiency corrections including the  $\eta \rightarrow 2\gamma$  branching ratio. Also shown are the previously<br>published STAR results for the  $\pi^0$  cross section in similar published STAR results for the  $\pi^0$  cross section in similar kinematic regions. The error band corresponds to the NLO pQCD theory prediction for the  $\pi^0$  cross section [\[32\]](#page-7-21), based on the CTEQ6M5 parton distribution function [\[33\]](#page-7-22) and the DSS fragmentation function [\[34](#page-7-23)]. The uncertainty

for the theory prediction was obtained by increasing the factorization and renormalization scales from  $\mu = p_T$  to  $\mu = 2p_T$ . We note that the DSS fragmentation function includes in the fit the previously published STAR results at pseudorapidity of 3.3 and 3.8 [[20](#page-7-12)], along with other RHIC results. The error bars include both statistical and systematic uncertainties. The major sources of systematic uncertainties are the absolute energy calibration uncertainty of 3%, which dominates the  $\pi^0$  cross section, and the uncertainty from the unfolding process, which dominates the  $\eta$ cross section at high energies. The normalization uncertainty was estimated at 12.5%, including the uncertainty of the BBC coincidence cross section of 7.6% [[30](#page-7-19)].

The lower panel of Fig. [4](#page-5-1) shows the  $\eta$  to  $\pi^0$  crosssection ratio, which is found to be around 50%. The error bars include both statistical and systematic uncertainties. The latter is dominated by the 1.5% relative energy scale uncertainty, caused by the acceptance differences for  $\pi^0$ and  $\eta$  decay photons, and the localized variations in cellto-cell calibration. The absolute calibration is common to both mesons, and largely cancels for the ratio.

In pQCD, large- $x_F$  production of both  $\pi^0$  and  $\eta$  arises from hard-scattered partons fragmenting into mesons with large momentum fraction  $\zeta$  (ratio of hadron momentum to the momentum of its parent parton). The fragmentation

<span id="page-5-1"></span>

FIG. 4 (color online). Differential production cross sections for  $\pi^0$  and  $\eta$  at average pseudorapidity of 3.68. Also shown are the previously published STAR results for similar kinematics [\[21\]](#page-7-13) and a NLO pQCD calculation of the  $\pi^0$  cross section [\[32\]](#page-7-21). The error band represents the uncertainty in the calculation due to scale variations. The  $\eta$  to  $\pi^0$  cross section ratio is shown in the bottom panel. The error bars indicate the total statistical and systematic uncertainties.

<span id="page-6-0"></span>

FIG. 5 (color online).  $A_N$  vs  $x_F$  at average pseudorapidity of 3.68 for  $\pi^0$  and  $\eta$ . Also shown are the previously published results for  $\pi^0$  at lower  $x_F$ , derived from the same data set but without the center cut [[12\]](#page-7-7). The error bars are statistical uncertainties only. The error boxes indicate the systematic uncertainties.

process generally does not depend on the details of the hard scattering, and a single set of pion fragmentation functions explains a wide variety of RHIC data [[22,](#page-7-14)[25,](#page-7-15)[35](#page-7-24)]. While there are currently no NLO pQCD predictions for the forward  $\eta$  production cross section, we note that our measurement of the  $\pi^0$  cross section is consistent with the NLO prediction, and the  $\eta/\pi^0$  cross-section ratio is consistent with the recent NLO pQCD extraction of the  $\eta$ fragmentation function [\[36\]](#page-7-25).

Figure [5](#page-6-0) shows the  $A_N$ , calculated using the "cross" ratio" formula [\[12](#page-7-7)[,37\]](#page-7-26), as a function of  $x_F$  for  $\pi^0$  and  $\eta$ after correcting for the underlying background. Also shown is the previous STAR result [[12](#page-7-7)] for  $A_N(\pi^0)$  at lower  $x_F$ , which utilized the same data set as the current analysis but without the center cut. The two  $\pi^0$  results are consistent within their correlated errors. The background correction, which only significantly affects the  $\eta$  asymmetry at medium energy, is obtained from a simulation sample corrected for the  $\eta$  yield and mass resolution, and the assumed background  $A_N$  of 0.005  $\pm$  0.016 extracted from<br>Fig. 2(c). The error bars indicate statistical uncertainties Fig.  $2(c)$ . The error bars indicate statistical uncertainties only, while the error boxes indicate the systematic uncertainties. The main source of the systematic uncertainty is the background correction; the polarization uncertainty is negligible in comparison. The  $A_N$  for negative  $x_F$  is consistent with zero for both mesons.

For the data points between  $x_F$  of 0.55 and 0.75, a fourpoint Z test results in 2.8% confidence level for the

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hypothesis that  $A_N(\eta) - A_N(\pi^0)$  is consistent with zero. Alternatively, the Kolmogorov-Smirnov test returns 3.3% confidence level for the same hypothesis. The comparison of  $A_N$  for  $\pi^0$  and  $\eta$  mesons is of particular interest given their similar up and down quark content, with wave functions of both mesons containing  $u\bar{u}$  and  $d\bar{d}$  pairs. The  $\eta$ <br>differs from the  $\pi^0$  mainly in that it is in an isosnin singlet differs from the  $\pi^0$  mainly in that it is in an isospin singlet state, and that it contains  $s\bar{s}$  in the wave function. The latter results in *n* being significantly more massive than the  $\pi^0$ results in  $\eta$  being significantly more massive than the  $\pi^0$ .

In conclusion, STAR has measured the  $x_F$  dependences of the cross section and transverse single-spin asymmetries for  $\pi^0$  and  $\eta$  mesons produced at an average pseudorapidity of 3.68 in  $\sqrt{s} = 200$  GeV polarized proton collisions.<br>In this kinematic region both the  $\pi^0$  cross section and the In this kinematic region, both the  $\pi^0$  cross section and the  $\eta/\pi^0$  cross-section ratio are consistent with NLO pQCD expectations. This suggests that the measured  $\eta$  asymmetry can be understood within the framework of pQCD. While several calculations exist for pion and kaon asym-metries [\[10,](#page-7-27)[38–](#page-7-28)[41](#page-7-29)], the first pQCD calculation of  $A_N$  for the  $\eta$  meson was performed only recently [\[42\]](#page-7-30). This model generates an  $\eta$  asymmetry that is substantially larger than that for the  $\pi^0$  via a sizable initial-state twist-3 effect for strange quarks. The calculated  $\eta$  asymmetry rises to about 12% at  $x_F$  of 0.4, well above our measured asymmetry, but then agrees quantitatively with the data for  $x_F > 0.5$ . It is yet unknown if a similar difference can arise from the fragmentation process via the Collins effect. A higher statistics measurement of the  $A_N$  for the  $\eta$  meson in this kinematic region is necessary to make a precise comparison to that for the  $\pi^0$ . Understanding the exact nature of these asymmetries can be further aided by complementary measurements of  $A_N$  for final states that lack Collins contributions, such as jets and prompt photons.

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