Inclusive cross section and double-helicity asymmetry for π0 production at midrapidity in p + p collisions at √s=510 GeV

(PHENIX Collaboration) Adare, A.; ...; Makek, Mihael; ...; Zou, L.

Source / Izvornik: **Physical Review D, 2016, 93**

Journal article, Published version Rad u časopisu, Objavljena verzija rada (izdavačev PDF)

<https://doi.org/10.1103/PhysRevD.93.011501>

Permanent link / Trajna poveznica: <https://urn.nsk.hr/urn:nbn:hr:217:712662>

Rights / Prava: [In copyright](http://rightsstatements.org/vocab/InC/1.0/) / [Zaštićeno autorskim pravom.](http://rightsstatements.org/vocab/InC/1.0/)

Download date / Datum preuzimanja: **2025-02-23**

Repository / Repozitorij:

[Repository of the Faculty of Science - University o](https://repozitorij.pmf.unizg.hr)f [Zagreb](https://repozitorij.pmf.unizg.hr)

PHYSICAL REVIEW D 93, 011501(R) (2016)

Inclusive cross section and double-helicity asymmetry for π^0 production at ss section and double-helicity asymmetry for π^0 j
midrapidity in $p + p$ collisions at $\sqrt{s} = 510 \text{ GeV}$

A. Adare,¹³ C. Aidala,^{38,42} N. N. Ajitanand,⁶⁰ Y. Akiba,^{55,56} R. Akimoto,¹² J. Alexander,⁶⁰ M. Alfred,²² K. Aoki,^{31,55} N. Apadula,^{27,61} Y. Aramaki,⁵⁵ H. Asano,^{34,55} E. T. Atomssa,⁶¹ T. C. Awes,⁵¹ B. Azmoun,⁷ V. Babintsev,²³ M. Bai,⁶ X. Bai,¹¹ N. S. Bandara,⁴¹ B. Bannier,⁶¹ K. N. Barish,⁸ S. Bathe,^{5,56} V. Baublis,⁵⁴ C. Baumann,⁷ S. Baumgart,⁵⁵ A. Bazilevsky,⁷ M. Beaumier, ⁸ S. Beckman, ¹³ R. Belmont, ^{13,42,65} A. Berdnikov, ⁵⁸ Y. Berdnikov, ⁵⁸ D. Black, ⁸ D. S. Blau, ³³ J. S. Bok, ⁴⁹ K. Boyle,⁵⁶ M. L. Brooks,³⁸ J. Bryslawskyj,⁵ H. Buesching,⁷ V. Bumazhnov,²³ S. Butsyk,⁴⁸ S. Campbell,^{14,27} C.-H. Chen,⁵⁶ C. Y. Chi,¹⁴ M. Chiu,⁷ I. J. Choi,²⁴ J. B. Choi,¹⁰ S. Choi,⁵⁹ P. Christiansen,³⁹ T. Chujo,⁶⁴ V. Cianciolo,⁵¹ Z. Citron,⁶⁶ B. A. Cole,¹⁴ N. Cronin,^{43,61} N. Crossette,⁴³ M. Csanád,¹⁶ T. Csörgő,⁶⁷ T. W. Danley,⁵⁰ A. Datta,⁴⁸ M. S. Daugherity,¹ G. David,⁷ K. DeBlasio,⁴⁸ K. Dehmelt,⁶¹ A. Denisov,²³ A. Deshpande,^{56,61} E. J. Desmond,⁷ L. Ding,²⁷ A. Dion,⁶¹ P. B. Diss,⁴⁰ J. H. Do,⁶⁸ L. D'Orazio,⁴⁰ O. Drapier,³⁵ A. Drees,⁶¹ K. A. Drees,⁶ J. M. Durham,³⁸ A. Durum,²³ T. Engelmore,¹⁴ A. Enokizono,^{55,57} H. En'yo,^{55,56} S. Esumi,⁶⁴ K. O. Eyser,⁷ B. Fadem,⁴³ N. Feege,⁶¹ D. E. Fields,⁴⁸ M. Finger,⁹ M. Finger, Jr.,⁹ F. Fleuret,³⁵ S. L. Fokin,³³ J. E. Frantz,⁵⁰ A. Franz,⁷ A. D. Frawley,¹⁸ Y. Fukao,³¹ T. Fusayasu,⁴⁵ K. Gainey, ¹ C. Gal, ⁶¹ P. Gallus, ¹⁵ P. Garg, ³ A. Garishvili, ⁶² I. Garishvili, ³⁷ H. Ge, ⁶¹ F. Giordano, ²⁴ A. Glenn, ³⁷ X. Gong, ⁶⁰ M. Gonin,³⁵ Y. Goto,^{55,56} R. Granier de Cassagnac,³⁵ N. Grau,² S. V. Greene,⁶⁵ M. Grosse Perdekamp,²⁴ Y. Gu,⁶⁰ T. Gunji,¹² H. Guragain,¹⁹ T. Hachiya,⁵⁵ J. S. Haggerty,⁷ K. I. Hahn,¹⁷ H. Hamagaki,¹² H. F. Hamilton,¹ S. Y. Han,¹⁷ J. Hanks,⁶¹ S. Hasegawa,²⁸ T. O. S. Haseler,¹⁹ K. Hashimoto,^{55,57} R. Hayano,¹² X. He,¹⁹ T. K. Hemmick,⁶¹ T. Hester,⁸ J. C. Hill,²⁷ R. S. Hollis, ⁸ K. Homma, ²¹ B. Hong, ³² T. Hoshino, ²¹ N. Hotvedt, ²⁷ J. Huang, ^{7,38} S. Huang, ⁶⁵ T. Ichihara, ^{55,56} Y. Ikeda, ⁵⁵ K. Imai,²⁸ Y. Imazu,⁵⁵ M. Inaba,⁶⁴ A. Iordanova,⁸ D. Isenhower,¹ A. Isinhue,⁴³ D. Ivanishchev,⁵⁴ B. V. Jacak,⁶¹ S. J. Jeon,⁴⁴ M. Jezghani,¹⁹ J. Jia,^{7,60} X. Jiang,³⁸ B. M. Johnson,⁷ E. Joo,³² K. S. Joo,⁴⁴ D. Jouan,⁵² D. S. Jumper,²⁴ J. Kamin,⁶¹ S. Kanda,^{12,31,55} B. H. Kang,²⁰ J. H. Kang,⁶⁸ J. S. Kang,²⁰ J. Kapustinsky,³⁸ D. Kawall,⁴¹ A. V. Kazantsev,³³ J. A. Key,⁴⁸ V. Khachatryan, ⁶¹ P. K. Khandai,³ A. Khanzadeev, ⁵⁴ K. Kihara, ⁶⁴ K. M. Kijima, ²¹ C. Kim, ³² D. H. Kim, ¹⁷ D. J. Kim, ²⁹ E.-J. Kim, 10 G. W. Kim, 17 H.-J. Kim, 68 M. Kim, 59 Y.-J. Kim, 24 Y. K. Kim, 20 B. Kimelman, 43 E. Kistenev, 7 R. Kitamura, 12 J. Klatsky,¹⁸ D. Kleinjan,⁸ P. Kline,⁶¹ T. Koblesky,¹³ M. Kofarago,¹⁶ B. Komkov,⁵⁴ J. Koster,⁵⁶ D. Kotchetkov,⁵⁰ D. Kotov,^{54,58} F. Krizek,²⁹ K. Kurita,⁵⁷ M. Kurosawa,^{55,56} Y. Kwon,⁶⁸ R. Lacey,⁶⁰ Y. S. Lai,¹⁴ J. G. Lajoie,²⁷ A. Lebedev,²⁷ D. M. Lee,³⁸ G. H. Lee,¹⁰ J. Lee,¹⁷ K. B. Lee,³⁸ K. S. Lee,³² S. Lee,⁶⁸ S. H. Lee,⁶¹ M. J. Leitch,³⁸ M. Leitgab,²⁴ B. Lewis,⁶¹ X. Li,¹¹ S. H. Lim,⁶⁸ M. X. Liu,³⁸ D. Lynch,⁷ C. F. Maguire,⁶⁵ Y. I. Makdisi,⁶ M. Makek,^{66,69} A. Manion,⁶¹ V. I. Manko,³³ E. Mannel,⁷ T. Maruyama,²⁸ M. McCumber,^{13,38} P. L. McGaughey,³⁸ D. McGlinchey,^{13,18} C. McKinney,²⁴ A. Meles,⁴⁹ M. Mendoza, ⁸ B. Meredith, ^{14,24} Y. Miake, ⁶⁴ T. Mibe, ³¹ A. C. Mignerey, ⁴⁰ A. J. Miller, ¹ A. Milov, ⁶⁶ D. K. Mishra, ⁴ J. T. Mitchell,⁷ S. Miyasaka,^{55,63} S. Mizuno,^{55,64} A. K. Mohanty,⁴ S. Mohapatra,⁶⁰ P. Montuenga,²⁴ T. Moon,⁶⁸ D. P. Morrison,^{[7,*](#page-3-0)} M. Moskowitz,⁴³ T. V. Moukhanova,³³ T. Murakami,^{34,55} J. Murata,^{55,57} A. Mwai,⁶⁰ T. Nagae,³⁴ S. Nagamiya,^{31,55} K. Nagashima,²¹ J. L. Nagle,^{13,[†](#page-3-1)} M. I. Nagy,¹⁶ I. Nakagawa,^{55,56} H. Nakagomi,^{55,64} Y. Nakamiya,²¹ K. R. Nakamura,^{34,55} T. Nakamura,⁵⁵ K. Nakano,^{55,63} C. Nattrass,⁶² P. K. Netrakanti,⁴ M. Nihashi,^{21,55} T. Niida,⁶⁴ S. Nishimura, 12,31 R. Nouicer, 7,56 T. Novák, 30,67 N. Novitzky, 29,61 A. S. Nyanin, 33 E. O'Brien, 7 C. A. Ogilvie, 27 H. Oide, 12 K. Okada,⁵⁶ J. D. Orjuela Koop,¹³ J. D. Osborn,⁴² A. Oskarsson,³⁹ H. Ozaki,⁶⁴ K. Ozawa,³¹ R. Pak,⁷ V. Pantuev,²⁵ V. Papavassiliou,⁴⁹ I. H. Park,¹⁷ J. S. Park,⁵⁹ S. Park,⁵⁹ S. K. Park,³² S. F. Pate,⁴⁹ L. Patel,¹⁹ M. Patel,²⁷ J.-C. Peng,²⁴ D. V. Perepelitsa,^{7,14} G. D. N. Perera,⁴⁹ D. Yu. Peressounko,³³ J. Perry,²⁷ R. Petti,^{7,61} C. Pinkenburg,⁷ R. Pinson,¹ R. P. Pisani,⁷ M. L. Purschke,⁷ H. Qu,¹ J. Rak,²⁹ B. J. Ramson,⁴² I. Ravinovich,⁶⁶ K. F. Read,^{51,62} D. Reynolds,⁶⁰ V. Riabov, $47,54$ Y. Riabov, $54,58$ E. Richardson, 40 T. Rinn, 27 N. Riveli, 50 D. Roach, 65 S. D. Rolnick, 8 M. Rosati, 27 Z. Rowan, 5 J. G. Rubin,⁴² M. S. Ryu,²⁰ B. Sahlmueller,⁶¹ N. Saito,³¹ T. Sakaguchi,⁷ H. Sako,²⁸ V. Samsonov,^{47,54} M. Sarsour,¹⁹ S. Sato,²⁸ S. Sawada,³¹ B. Schaefer,⁶⁵ B. K. Schmoll,⁶² K. Sedgwick,⁸ J. Seele,⁵⁶ R. Seidl,^{55,56} Y. Sekiguchi,¹² A. Sen,^{19,62} R. Seto, 8 P. Sett, 4 A. Sexton, 40 D. Sharma, 61 A. Shaver, 27 I. Shein, 23 T.-A. Shibata, $55,63$ K. Shigaki, 21 M. Shimomura, $27,46,64$ K. Shoji,⁵⁵ P. Shukla,⁴ A. Sickles,^{7,24} C. L. Silva,³⁸ D. Silvermyr,^{39,51} B. K. Singh,³ C. P. Singh,³ V. Singh,³ M. Skolnik,⁴³ M. Slunečka,⁹ M. Snowball,³⁸ S. Solano,⁴³ R. A. Soltz,³⁷ W. E. Sondheim,³⁸ S. P. Sorensen,⁶² I. V. Sourikova,⁷ P. W. Stankus,⁵¹ P. Steinberg,⁷ E. Stenlund,³⁹ M. Stepanov,^{41,[‡](#page-3-2)} A. Ster,⁶⁷ S. P. Stoll,⁷ M. R. Stone,¹³ T. Sugitate,²¹ A. Sukhanov,⁷ T. Sumita,⁵⁵ J. Sun,⁶¹ J. Sziklai,⁶⁷ A. Takahara,¹² A. Taketani,^{55,56} Y. Tanaka,⁴⁵ K. Tanida,^{56,59} M. J. Tannenbaum, ⁷ S. Tarafdar, ^{3,66} A. Taranenko, ^{47,60} E. Tennant, ⁴⁹ R. Tieulent, ¹⁹ A. Timilsina, ²⁷ T. Todoroki, ^{55,64} M. Tomášek,^{15,26} H. Torii,¹² C. L. Towell,¹ M. Towell,¹ R. Towell,¹ R. S. Towell,¹ I. Tserruya,⁶⁶ H. W. van Hecke,³⁸ M. Vargyas,^{16,67} E. Vazquez-Zambrano,¹⁴ A. Veicht,¹⁴ J. Velkovska,⁶⁵ R. Vértesi,⁶⁷ M. Virius,¹⁵ V. Vrba,^{15,26} E. Vznuzdaev, ⁵⁴ X. R. Wang, ^{49,56} D. Watanabe, ²¹ K. Watanabe, ^{55,57} Y. Watanabe, ^{55,56} Y. S. Watanabe, ^{12,31} F. Wei, ⁴⁹ S. Whitaker,²⁷ A. S. White,⁴² S. Wolin,²⁴ C. L. Woody,⁷ M. Wysocki,⁵¹ B. Xia,⁵⁰ L. Xue,¹⁹ S. Yalcin,⁶¹ Y. L. Yamaguchi,^{12,61} A. Yanovich,²³ S. Yokkaichi,^{55,56} J. H. Yoo,³² I. Yoon,⁵⁹ Z. You,³⁸ I. Younus,^{36,48} H. Yu,⁵³ I. E. Yushmanov,³³ W. A. Zajc, 14 A. Zelenski, 6 S. Zhou, 11 and L. Zou⁸

(PHENIX Collaboration)

A. ADARE *et al.* **PHYSICAL REVIEW D 93,** 011501(R) (2016)

¹Abilene Christian University, Abilene, Texas 79699, USA
²Department of Physics, Augustana University, Sigur Falle, South Dako

 2 Department of Physics, Augustana University, Sioux Falls, South Dakota 57197, USA

 3 Department of Physics, Banaras Hindu University, Varanasi 221005, India

⁴Bhabha Atomic Research Centre, Bombay 400 085, India

⁵Baruch College, City University of New York, New York, New York 10010 USA

⁶Collider-Accelerator Department, Brookhaven National Laboratory, Upton, New York 11973-5000, USA

⁷Physics Department, Brookhaven National Laboratory, Upton, New York 11973-5000, USA

⁸ University of California-Riverside, Riverside, California 92521, USA
⁹ Charles University, Ovocný trh 5, Praha 1, 116 36, Prague, Czech Republic

¹⁰Chonbuk National University, Jeonju, 561-756, Korea
¹¹Science and Technology on Nuclear Data Laboratory, China Institute of Atomic Energy, Beijing 102413,

People's Republic of China
¹²Center for Nuclear Study, Graduate School of Science, University of Tokyo, 7-3-1 Hongo,

Bunkyo, Tokyo 113-0033, Japan
¹³University of Colorado, Boulder, Colorado 80309, USA
¹⁴Columbia University, New York, New York 10027 and Nevis Laboratories,
Irvington, New York 10533, USA

¹⁵Czech Technical University, Zikova 4, 166 36 Prague 6, Czech Republic
¹⁶ELTE, Eötvös Loránd University, H-1117 Budapest, Pázmány P. s. 1/A, Hungary
¹⁷Ewha Womans University, Seoul 120-750, Korea
¹⁸Florida State

¹⁹Georgia State University, Atlanta, Georgia 30303, USA
²¹Hiroshima University, Kagamiyama, Higashi-Hiroshima 739-8526, Japan
²¹Hiroshima University, Kagamiyama, Higashi-Hiroshima 739-8526, Japan
²²Department of P

Protvino, 142281, Russia
²⁴University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, USA

²⁵Institute for Nuclear Research of the Russian Academy of Sciences, prospekt 60-letiva Oktyabrya 7a, Moscow 117312, Russia

 26 Institute of Physics, Academy of Sciences of the Czech Republic, Na Slovance 2,

182 21 Prague 8, Czech Republic
²⁷Iowa State University, Ames, Iowa 50011, USA²⁸
²⁸Advanced Science Research Center, Japan Atomic Energy Agency, 2-4 Shirakata Shirane, Tokai-mura,
Naka-gun, Ibaraki-ken 319-1195, Japa

²⁹Helsinki Institute of Physics and University of Jyväskylä, P.O.Box 35, FI-40014 Jyväskylä, Finland
³⁰Károly Róberts University College, H-3200 Gyöngyös, Mátraiút 36, Hungary
³¹KEK, High Energy Accelerator Research

Route de Saclay, F-91128, Palaiseau, France
³⁶Physics Department, Lahore University of Management Sciences, Lahore 54792, Pakistan
³⁷Lawrence Livermore National Laboratory, Livermore, California 94550, USA
³⁸Los Alam

³⁹Department of Physics, Lund University, Box 118, SE-221 00 Lund, Sweden
⁴⁰University of Maryland, College Park, Maryland 20742, USA
⁴¹Department of Physics, University of Massachusetts, Amherst, Massachusetts 0100

Moscow 115409, Russia
⁴⁸University of New Mexico, Albuquerque, New Mexico 87131, USA
⁴⁹New Mexico State University, Las Cruces, New Mexico 88003, USA
⁵⁰Department of Physics and Astronomy, Ohio University, Athens, Oh

INCLUSIVE CROSS SECTION AND DOUBLE-HELICITY … PHYSICAL REVIEW D 93, 011501(R) (2016)

⁵²IPN-Orsay, Université Paris-Sud, CNRS/IN2P3, Université Paris-Saclay, BP1, F-91406, Orsay, France
⁵³Peking University, Beijing 100871, People's Republic of China
⁵⁴PNPI, Petersburg Nuclear Physics Institute, Gatch

⁵⁶RIKEN BNL Research Center, Brookhaven National Laboratory, Upton, New York 11973-5000, USA

⁵⁷Physics Department, Rikkyo University, 3-34-1 Nishi-Ikebukuro, Toshima, Tokyo 171-8501, Japan
⁵⁸Saint Petersburg State Polytechnic University, St. Petersburg, 195251 Russia
⁵⁹Department of Physics and Astronomy, S

⁶⁰Chemistry Department, Stony Brook University, SUNY, Stony Brook, New York 11794-3400, USA
⁶¹Department of Physics and Astronomy, Stony Brook University,
SUNY, Stony Brook, New York 11794-3800, USA

⁶²University of Tennessee, Knoxville, Tennessee 37996, USA
⁶³Department of Physics, Tokyo Institute of Technology, Oh-okayama, Meguro, Tokyo 152-8551, Japan
⁶⁴Center for Integrated Research in Fundamental Science an

University of Tsukuba, Tsukuba, Ibaraki 305, Japan
⁶⁵Vanderbilt University, Nashville, Tennessee 37235, USA
⁶⁶Weizmann Institute, Rehovot 76100, Israel
⁶⁷Institute for Particle and Nuclear Physics, Wigner Research Ce

Hungarian Academy of Sciences (Wigner RCP, RMKI) H-1525 Budapest 114,

P.O. Box 49, Budapest, Hungary ⁶⁸Yonsei University, IPAP, Seoul 120-749, Korea

 69 University of Zagreb, Faculty of Science, Department of Physics,

Bijenička 32, HR-10002 Zagreb, Croatia

(Received 8 October 2015; published 7 January 2016)

PHENIX measurements are presented for the cross section and double-helicity asymmetry (A_{LL}) in PHENIX measurements are presented for the cross section and double-helicity asymmetry (A_{LL}) in
inclusive π^0 production at midrapidity from $p + p$ collisions at $\sqrt{s} = 510$ GeV from data taken in 2012 and 2013 at the Relativistic Heavy Ion Collider. The next-to-leading-order perturbative-quantumchromodynamics theory calculation is in excellent agreement with the presented cross section results. The calculation utilized parton-to-pion fragmentation functions from the recent DSS14 global analysis, which prefer a smaller gluon-to-pion fragmentation function. The $\pi^0 A_{LL}$ results follow an increasingly which prefer a smaller gluon-to-pion fragmentation function. The $\pi^{\circ} A_{LL}$ results follow an increasingly positive asymmetry trend with p_T and \sqrt{s} with respect to the predictions and are in excellent agreement with the latest global analysis results. This analysis incorporated earlier results on π^0 and jet A_{LL} and suggested a positive contribution of gluon polarization to the spin of the proton ΔG for the gluon momentum fraction range $x > 0.05$. The data presented here extend to a currently unexplored region, down to $x \sim 0.01$, and thus provide additional constraints on the value of ΔG .

DOI: [10.1103/PhysRevD.93.011501](http://dx.doi.org/10.1103/PhysRevD.93.011501)

In the late 1980s, the EMC experiment [\[1\]](#page-7-0) showed that the spins of quarks and antiquarks might contribute only a fraction of the proton spin (about $1/3$ from the recent global analyses of world spin polarized scattering data [\[2](#page-7-1)–6]). This sparked several decades of worldwide effort to understand the proton spin structure in terms of quark and gluon polarizations and their orbital angular momentum, as evidenced by experimental programs at CERN, SLAC, DESY, JLAB, and BNL.

A key component of the Relativistic Heavy Ion Collider (RHIC) spin program is the determination of the gluon spin contribution to the spin of the proton. High-energy polarized proton collisions provide direct access to the gluon polarization ΔG within the proton through several gluondominated hard scattering processes, such as high p_T jet

and hadron production [\[7\]](#page-8-0). RHIC results on the double and hadron production [7]. RHIC results on the double
helicity asymmetry A_{LL} in inclusive π^0 production at $\sqrt{s} =$ 62.4 and 200 GeV from PHENIX [8–[11\]](#page-8-1) and jet production 62.4 and 200 GeV from PHENIX [8–11] and jet production
at $\sqrt{s} = 200$ GeV from STAR [\[12,13\]](#page-8-2) have made a significant contribution to the ΔG determination [\[2,3\]](#page-7-1). Inclusion ficant contribution to the ΔG determination [2,3]. Inclusion
of the recent RHIC results from $\sqrt{s} = 200$ GeV data collected in 2009 [\[14,15\]](#page-8-3) in the global next-to-leading-order (NLO) perturbative-quantum-chromodynamics (pQCD) analysis provided evidence for positive gluon polarization within the proton, with the integral of $\Delta G(x, Q^2 =$ 10 GeV²) in the gluon momentum fraction $x > 0.05$ being $0.20^{+0.06}_{-0.07}$ at 90% C.L. [\[16\]](#page-8-4). The RHIC high luminosity data 0.20⁻⁻-0.07 at 90% C.L. [16]. The RHIC high luminosity data
at \sqrt{s} = 510 GeV allow probing ΔG in the overlapping x range at higher momentum transfer and extend our understanding of ΔG to the unexplored lower x region.

In this paper, we present the PHENIX π^0 A_{LL} results at \sqrt{s} = 510 GeV from the RHIC 2012 and 2013 data sets, with an integrated luminosity of 20 and 108 pb^{-1} , respectively. We also present and discuss our results on π^0

[^{*}](#page-1-0) Deceased

[[†]](#page-1-1) morrison@bnl.gov

[[‡]](#page-1-2) jamie.nagle@colorado.edu

unpolarized cross section measurements, which serve as an important test for the applicability of the NLO pQCD theory calculations in the accessed kinematic range. The theory is used to connect the measured asymmetries to gluon polarization in the proton [\[2,3,16\].](#page-7-1)

The PHENIX experimental setup is described elsewhere [\[17\]](#page-8-5). In this analysis, π^0 s were reconstructed via $\pi^0 \rightarrow \gamma \gamma$ decays using a highly segmented electromagnetic calorimeter (EMCal), covering a pseudorapidity range of $|\eta|$ < 0.35. The EMCal comprises two calorimeter types, a lead-scintillator (PbSc) sampling calorimeter and a leadglass (PbGl) Čerenkov calorimeter, with granularity $\Delta \eta \times$ $\Delta \phi \sim 0.011 \times 0.011$ and 0.008×0.008 , respectively. Eight EMCal sectors (six PbSc and two PbGl) are located in two nearly back-to-back arms, each covering $\Delta \phi \sim 90^{\circ}$ in azimuth. The PHENIX EMCal also generates a high p_T photon (HPP) trigger when the deposited energy in any set of 4×4 towers exceeds a pre-defined threshold. Thin multiwire proportional chambers located in front of the EMCal were used as a veto to suppress the charged hadron background in π^0 reconstruction [\[14\]](#page-8-3). Beam-beam counters (BBC), positioned at ± 144 cm from the nominal interaction point along the beam line and covering $\eta = \pm 3.0 - 3.9$, defined the minimum-bias (MB) collision trigger and determined the location of the collision vertex. Only events with collision vertices within ± 10 cm $(\pm 30 \text{ cm})$ of the nominal interaction point were used in the cross section (asymmetry) analysis. The BBCs were also used to calculate the integrated luminosity of the collected data sample and relative luminosity between colliding bunches with different spin configurations. Zero-degree calorimeters (ZDC), located at ± 18 m and covering $|\eta| > 6$, were used as another relative luminosity monitor. Equipped with a shower-maximum detector, the ZDC also provided monitoring of the transverse polarization component of colliding bunches in the PHENIX interaction region, utilizing the azimuthal asymmetry in forward neutron production in transversely polarized $p + p$ collisions [\[18\].](#page-8-6)

As described in detail in Ref. [\[9\],](#page-8-7) π^0 s were reconstructed from two-photon invariant mass distributions. A time-of-flight cut and shower profile evaluation (energy distribution among EMCal towers) were used for photon identification. A minimal photon energy cut of 0.3 GeV and an energy asymmetry between the two photons $\alpha =$ $|E1 - E2|/(E1 + E2) < 0.8$ were applied. The π^0 peak width in the invariant mass distribution varied between 9 and 12 MeV/ c^2 over the measured p_T range. The resulting background fraction in the mass window of $\pm 25 \text{ MeV}/c^2$ around the π^0 peak varied from ~20% at $p_T \sim 2 \text{ GeV}/c$ to $< 8\%$ at $p_T > 5$ GeV/c. The two decay photons start merging in the PbSc (PbGl) EMCal at π^0 $p_T > 10 \text{ GeV}/c$ ($> 15 \text{ GeV}/c$). A 50% merging probability is reached at $p_T \sim 17 \text{ GeV}/c$ (25 GeV/c) in the PbSc (PbGl), as shown in Fig. [1.](#page-4-0) For $p_T > 24 \text{ GeV}/c$, the majority of photon pairs

FIG. 1. The probability for two photons from π^0 decay to be separated by the PHENIX EMCal clustering algorithm vs π^0 p_T ; obtained from GEANT [\[19\]](#page-8-8) simulation for the two-photon energy asymmetry cut α < 0.8.

are merged in the PbSc; in this p_T range, only the PbGl data were used.

The invariant differential cross section for π^0 production is calculated as

$$
E\frac{d^3\sigma}{dp^3} = \frac{1}{\mathcal{L}} \cdot \frac{1}{2\pi p_T^*} \cdot \frac{C \cdot N}{\Delta p_T \Delta y},\tag{1}
$$

where N is the number of π^0 's observed in a Δp_T wide bin at p_T^* defined as the p_T for which the cross section equals its average over the bin; Δy is the rapidity range; C includes corrections for trigger efficiency, geometrical acceptance, π^0 reconstruction efficiency, and detector resolution effects; $\mathcal L$ is the integrated luminosity for the analyzed data sample.

Two data samples were used for the π^0 cross section measurements, one collected with a MB trigger and the other with the HPP in coincidence with MB trigger. The MB trigger efficiency was obtained from the data collected with a dedicated HPP trigger operated without coincidence with MB trigger, and found to be 0.91 ± 0.01 independent of p_T . It accounts for the fact that only a fraction of inelastic $p + p$ collisions producing π^0 meson(s) fires the MB trigger. The HPP trigger efficiency vs p_T was calculated in each arm separately from a set of events triggered by a high-energy cluster in the opposite arm. It showed a characteristic threshold behavior with efficiency increasing from ∼1% at $p_T = 2$ GeV/c to 93% at $p_T > 8$ GeV/c. For the cross section calculation, the MB triggered data sample was used at $p_T < 6$ GeV/c, and HPP triggered data sample at higher p_T .

The reconstructed π^0 yields in each p_T bin were corrected for geometrical acceptance, reconstruction efficiencies (e.g. due to the two-photon energy asymmetry cut), and smearing effects (due to the finite detector resolutions). The corrections were calculated with a

INCLUSIVE CROSS SECTION AND DOUBLE-HELICITY … PHYSICAL REVIEW D 93, 011501(R) (2016)

simulation containing the EMCal geometry, known detector inefficiencies, and photon energy and position smearing based on the known EMCal resolutions.

The major systematic uncertainties in the π^0 cross section measurement are the energy scale (1.2% uncertainty in the EMCal energy calibration translates to ∼7% in cross section uncertainty), energy nonlinearity (up to 10% for cross section depending on p_T), and merging corrections (up to 30% in the bins with the highest probability for two photons to merge). The large uncertainty at high p_T reflects the sensitivity of the merging correction to shower-shape fluctuations and background conditions for asymmetric two-photon decays, having higher probability to survive the merging in the EMCal. The other uncertainties, contributing $< 6\%$ altogether, are related to π^0 yield extraction and background subtraction, trigger efficiencies, geometrical acceptance calculation, smearing corrections, and photon conversion. The uncertainties are assigned separately for the PbSc and the PbGl measurements.

A comparison of the results obtained from the PbSc and the PbGl is a key cross check, because the two calorimeters have a different response to hadrons (hence different background contamination in π^0 reconstruction), and considerably different merging corrections versus p_T . The π^0 cross section results from the PbSc and the PbGl were in agreement within uncertainties in the overlapping p_T range. The final spectrum was obtained from the combined PbSc and PbGl results, while for $p_T > 24$ GeV/c the PbGl results were used. The total systematic uncertainties associated with the results vary from 8%–10% at $p_T < 14$ GeV/c to ∼30% at the highest p_T .

The integrated luminosity $\mathcal L$ in Eq. [\(1\)](#page-4-1) was calculated from the accumulated number of MB triggers in the analyzed data sample normalized by the cross section of the processes firing the MB trigger in $p + p$ collisions. Similar to our previous analyses [\[10,20\]](#page-8-9), the cross section was defined using a vernier scan technique and found to be 32.5 mb with $\pm 10\%$ uncertainty.

In the 2013 RHIC run, the instantaneous luminosity delivered to PHENIX was so high that up to a third of all bunch crossings had more than one $p + p$ collision. To correct for this multiple-collision effect, we studied the ratio of the π^0 yield to the number of MB triggers [which is proportional to the measured N/L in Eq. [\(1\)\]](#page-4-1) as a function of instantaneous MB trigger rate.

Figure [2](#page-5-0) shows the π^0 cross section versus p_T compared to NLO pQCD calculations performed with MSTW [\[21\]](#page-8-10) parton distribution functions (PDF) and DSS14 [\[22\]](#page-8-11) fragmentation functions (FF). Compared to earlier FF analysis [\[23\]](#page-8-12) the DSS14 recent global fit results preferred a smaller fraction of pions produced from gluon hadronization, driven mainly by the latest data from the Large Hadron Collider. This theoretical calculation is in excellent agreement with the presented data.

FIG. 2. The neutral pion production cross section at midrapidity FIG. 2. The neutral pion production cross section at midrapidity
in $p + p$ collisions at $\sqrt{s} = 510$ GeV as a function of p_T and NLO pQCD calculations for theory scales $\mu = p_T/2$ (dotted line), p_T (solid line) and $2p_T$ (dashed line), with μ representing equal factorization, renormalization, and fragmentation scales. Note that the error bars, representing the combined statistical and point-to-point systematic uncertainties, are smaller than the points. (bottom panel) Relative difference between the data and theory for the three theory scales. Experimental uncertainties are shown for the $\mu = p_T$ curve.

In 2012 and 2013, RHIC provided PHENIX with colliding bunches of longitudinally polarized protons at \sqrt{s} = 510 GeV. The bunch spin pattern was predefined in such a way that the colliding bunch pair helicity state alternated every bunch crossing, spaced 106 ns apart. This greatly suppressed the possibility of false asymmetries between colliding bunches with different helicity configuration, due to variation in detector performance. To remove possible systematic effects associated with particular bunch (es) in the process of filling, ramping up, and storing the beams in RHIC rings, eight bunch spin patterns were used alternating every RHIC store, typically lasting eight hours. Beam polarizations were measured by RHIC polarimeters [\[24\]](#page-8-13) three to four times during the store. For the two RHIC collider rings, labeled "Blue" (B) and "Yellow" (Y), the luminosity-weighted average polarizations in 2012 (2013) were $\langle P_B \rangle = 0.55 \pm 0.02$ (0.55 \pm 0.02) and $\langle P_Y \rangle =$ 0.57 ± 0.02 (0.56 ± 0.02) . The degree of longitudinal polarization in the PHENIX interaction region was

monitored by local polarimeters, based on the ZDC and shower-maximum detectors, which measured the residual transverse polarization of colliding bunches. The longitudinal component P_L/P in both 2012 and 2013 was > 0.998, for both RHIC rings.

The π^0 A_{LL} analysis technique is described in detail in Ref. [\[14\]](#page-8-3). The A_{LL} for inclusive π^0 production, defined as the difference between cross sections for colliding bunches with the same helicity and opposite helicity, divided by the sum, is experimentally calculated as

$$
A_{LL}^{\pi^0} = \frac{1}{P_B \cdot P_Y} \cdot \frac{N_{++} - R \cdot N_{+-}}{N_{++} + R \cdot N_{+-}}; \qquad R = \frac{L_{++}}{L_{+-}}, \quad (2)
$$

where N is the number of π^0 's from the colliding bunches with the same $(++)$ and opposite $(+-)$ helicities, R is the relative luminosity between bunches with the same and opposite helicities, and P_B and P_Y are the two RHIC beam polarizations.

The π^0 yields were extracted from the HPP triggered sample in which the maximal energy photon of each pair candidate was explicitly required to fire the HPP trigger. This test, along with a time-of-flight cut, suppressed the possibility of contamination from the neighboring bunch crossings to a negligible level. As in the cross section analysis, the π^0 candidates were counted within a ± 25 MeV/ c^2 window around the π^0 peak in the twophoton invariant mass distribution. The A_{LL} was then corrected for the background A_{LL} measured in the side bands on either side of the π^0 peak; this background asymmetry was found to be consistent with zero in all p_T bins.

The relative luminosity R was defined from the number of MB triggers in each bunch crossing, and cross checked using the number of collisions firing the ZDCs on both sides of the IR. The pile-up correction due to the high collision rate had a negligible effect on R . The resulting contribution of the relative luminosity uncertainty to $A_{LL}^{\pi^0}$ for the 2012 (2013) data was $\delta A_{LL}^{\pi^0}|_R = 2.0 \times 10^{-4}$ (3.8×10^{-4}) , affecting all p_T bins in the same way.

 A_{LL} was measured for each PHENIX data-taking segment (up to 90 min long) to minimize the systematic effects from variation in R , beam polarization (decreasing during a store by $\Delta P = 0.005{\text -}0.010$ per hour), and HPP trigger performance. These asymmetries were averaged separately for the 2012 and 2013 data. Results from 2012 and 2013 were consistent within statistical uncertainties and the final result presented in this paper is the average of these data sets.

The resulting π^0 A_{LL} systematic uncertainties are (a) a correlated uncertainty from relative luminosity of 3.6×10^{-4} , (b) a correlated uncertainty from polarization measurements of 6.5% (scale uncertainty), and (c) point-topoint uncertainty from background fraction determination under the π^0 peak in the two-photon invariant-mass

A. ADARE *et al.* **PHYSICAL REVIEW D 93,** 011501(R) (2016)

FIG. 3. A_{LL} vs p_T for π^0 production at midrapidity in $p + p$ FIG. 3. A_{LL} vs p_T for π^0 production at midrapidity in $p + p$ collisions at $\sqrt{s} = 510$ GeV. Error bars are combined statistical and point-to-point systematic uncertainties. The $A_{LL} = 0$ (yellow) line is uncertainty from relative luminosity. The theoretical curve with 90% C.L. band (green) is from a DSSV14 calculation [\[16\]](#page-8-4).

distribution. The point-to-point uncertainties were found to be smaller than 10% of the statistical uncertainty in all p_T bins. As in the previous PHENIX analysis [\[14\]](#page-8-3), the contribution of other potential sources of systematic uncertainties was negligible.

certainties was negligible.
Figure [3](#page-6-0) shows the $\pi^0 A_{LL}$ asymmetries at $\sqrt{s} = 510$ GeV compared with the DSSV14 calculation [\[16\]](#page-8-4) based on a global fit of the world helicity asymmetry data. Comparing the data to the DSSV14 curve we obtain $\chi^2/NDF = 8.0/14$, while comparing to the $A_{LL} = 0$ hypothesis we obtain $\chi^2/NDF = 18.2/14$; the data prefer the DSSV14 curve by a little more than 3 standard deviations.

Figure [4](#page-7-2) shows π^0 A_{LL} data from PHENIX at both \sqrt{s} = 200 GeV [\[14\]](#page-8-3) and 510 GeV, along with NLO pQCD analyses from three groups [\[5,6,16\].](#page-7-3) All three analyses predict an increase in $\pi^0 A_{LL}$ at the same x_T due to pQCD predict an increase in $\pi^0 A_{LL}$ at the same x_T due to pQCD
evolution, with $x_T = 2p_T/\sqrt{s}$. Our data are consistent with such an increase.

In summary, we have presented the unpolarized cross section and double helicity asymmetry for π^0 production at section and double helicity asymmetry for π^0 production at midrapidity for $p + p$ collisions at $\sqrt{s} = 510$ GeV. The NLO pQCD calculation is in excellent agreement with the presented cross section results. The calculation utilized the recent DSS14 set of fragmentation functions, which prefer the reduced fraction of pions produced from gluon hadronization. The π^0 A_{LL} results follow a positive asymmetry mization. The π^0 A_{LL} results follow a positive asymmetry
trend with p_T and \sqrt{s} predicted by NLO pQCD and are in excellent agreement with the latest global fit results, which suggested a nonzero gluon polarization in the proton for the gluon momentum fraction range $x > 0.05$. These global fit gluon momentum fraction range $x > 0.05$. These global fit
results included RHIC π^0 A_{LL} data at $\sqrt{s} = 62.4$ and results included RHIC π^0 A_{LL} data at $\sqrt{s} = 62.4$ and 200 GeV and jet A_{LL} data at $\sqrt{s} = 200$ GeV. The presented

FIG. 4. A_{LL} vs x_T for π^0 production at midrapidity at $\sqrt{s} =$ 200 GeV (blue) from [\[14\]](#page-8-3) and 510 GeV (red) from this analysis. Error bars are combined statistical and point-to-point systematic uncertainties. Note that the relative luminosity uncertainties from two data samples are about the same, hence are indistinguishable in the plot in the overlapping x_T range. Theoretical curves are from recent NLO global analyses [\[5,6,16\],](#page-7-3) with the lower curves from recent NLO global analyses [5,6,16], with the lower curves
(blue) for $\sqrt{s} = 200$ GeV and the higher curves (red) for \sqrt{s} = 510 GeV.

data at \sqrt{s} = 510 GeV extend the x range probed down to $x \sim 0.01$ and provide an additional constraint on ΔG in this x range [\[25\]](#page-8-14), which is a crucial step in the nearly two decades of worldwide efforts to understand the contribution of gluon polarization to the spin of the proton. We note the of gluon polarization to the spin of the proton. We note the recent π^0 A_{LL} results at $\sqrt{s} = 200$ GeV and forward pseudorapidity $0.8 < \eta < 2$ from STAR covering the gluon x range down to $x \sim 0.01$ (although with large uncertainties) [\[26\].](#page-8-15) Data collected by PHENIX with forward EMCal ties) [26]. Data collected by PHENIX with forward EMCal
at pseudorapidity $3.1 < \eta < 3.9$ and $\sqrt{s} = 510$ GeV will further extend the x range probed down to $x \sim 0.001$.

We thank the staff of the Collider-Accelerator and Physics Departments at Brookhaven National Laboratory

and the staff of the other PHENIX participating institutions for their vital contributions. We also thank M. Stratmann for providing the theoretical calculations and for informative discussions, and E. Nocera, E. Leader and D. B. Stamenov for information regarding their polarized-partondistribution functions. We acknowledge support from the Office of Nuclear Physics in the Office of Science of the Department of Energy, the National Science Foundation, Abilene Christian University Research Council, Research Foundation of SUNY, and Dean of the College of Arts and Sciences, Vanderbilt University (U.S.A), the Ministry of Education, Culture, Sports, Science, and Technology and the Japan Society for the Promotion of Science (Japan), the Conselho Nacional de Desenvolvimento Científico e Tecnológico and Fundação de Amparo à Pesquisa do Estado de São Paulo (Brazil), the Natural Science Foundation of China (P. R. China), Croatian Science Foundation and Ministry of Science, Education, and Sports (Croatia), the Ministry of Education, Youth and Sports (Czech Republic), the Centre National de la Recherche Scientifique, Commissariat à l'Énergie Atomique and Institut National de Physique Nucléaire et de Physique des Particules (France), the Bundesministerium für Bildung und Forschung, Deutscher Akademischer Austausch Dienst, and Alexander von Humboldt Stiftung (Germany), the National Science Fund, OTKA, Károly Róbert University College and the Ch. Simonyi Fund (Hungary), the Department of Atomic Energy and Department of Science and Technology (India), the Israel Science Foundation (Israel), the Basic Science Research Program through NRF of the Ministry of Education (Korea), the Physics Department, Lahore University of Management Sciences (Pakistan), the Ministry of Education and Science, Russian Academy of Sciences, Federal Agency of Atomic Energy (Russia), the VR and Wallenberg Foundation (Sweden), the U.S. Civilian Research and Development Foundation for the Independent States of the Former Soviet Union, the Hungarian American Enterprise Scholarship Fund, and the US-Israel Binational Science Foundation.

- [1] J. Ashman et al. (European Muon Collaboration), An investigation of the spin structure of the proton in deep inelastic scattering of polarized muons on polarized protons, [Nucl. Phys.](http://dx.doi.org/10.1016/0550-3213(89)90089-8) B328, 1 (1989).
- [2] D. de Florian, R. Sassot, M. Stratmann, and W. Vogelsang, Global Analysis of Helicity Parton Densities and Their Uncertainties, Phys. Rev. Lett. 101[, 072001 \(2008\).](http://dx.doi.org/10.1103/PhysRevLett.101.072001)
- [3] D. de Florian, R. Sassot, M. Stratmann, and W. Vogelsang, Extraction of spin-dependent parton densities and their uncertainties, Phys. Rev. D 80[, 034030 \(2009\)](http://dx.doi.org/10.1103/PhysRevD.80.034030).
- [4] J. Blumlein and H. Bottcher, QCD analysis of polarized deep inelastic scattering data, [Nucl. Phys.](http://dx.doi.org/10.1016/j.nuclphysb.2010.08.005) B841, 205 [\(2010\).](http://dx.doi.org/10.1016/j.nuclphysb.2010.08.005)
- [5] E. Leader, A. V. Sidorov, and D. B. Stamenov, Determination of polarized PDFs from a QCD analysis of inclusive and semi-inclusive deep inelastic scattering data, [Phys. Rev.](http://dx.doi.org/10.1103/PhysRevD.82.114018) D **82**[, 114018 \(2010\)](http://dx.doi.org/10.1103/PhysRevD.82.114018).
- [6] R. D. Ball et al. (NNPDF Collaboration), Unbiased determination of polarized parton distributions and their uncertainties, [Nucl. Phys.](http://dx.doi.org/10.1016/j.nuclphysb.2013.05.007) B874, 36 (2013).
- [7] G. Bunce, N. Saito, J. Soffer, and W. Vogelsang, Prospects for spin physics at RHIC, [Annu. Rev. Nucl. Part. Sci.](http://dx.doi.org/10.1146/annurev.nucl.50.1.525) 50, [525 \(2000\)](http://dx.doi.org/10.1146/annurev.nucl.50.1.525).
- [8] S. S. Adler et al. (PHENIX Collaboration), Improved measurement of double helicity asymmetry in inclusive midrapidity pi0 production for polarized $p + p$ collisions at \sqrt{s} = 200 GeV, Phys. Rev. D 73[, 091102 \(2006\)](http://dx.doi.org/10.1103/PhysRevD.73.091102).
- [9] A. Adare et al. (PHENIX Collaboration), Inclusive crosssection and double helicity asymmetry for pi0 production in section and double helicity asymmetry for pi0 production in
 $p + p$ collisions at $\sqrt{s} = 200$ GeV: Implications for the polarized gluon distribution in the proton, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.76.051106) 76, [051106 \(2007\).](http://dx.doi.org/10.1103/PhysRevD.76.051106)
- [10] A. Adare et al. (PHENIX Collaboration), Inclusive cross section and double helicity asymmetry for π^0 production in section and double helicity asymmetry for π^0 production in $p + p$ collisions at $\sqrt{s} = 62.4$ GeV, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.79.012003) 79, [012003 \(2009\).](http://dx.doi.org/10.1103/PhysRevD.79.012003)
- [11] A. Adare et al. (PHENIX Collaboration), The Polarized Gluon Contribution to the Proton Spin from the Double Helicity Asymmetry in Inclusive π^0 Production in Polarized Helicity Asymmetry in Inclusive π^0 Production in Polarized $p + p$ Collisions at $\sqrt{s} = 200$ GeV, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.103.012003) 103, [012003 \(2009\).](http://dx.doi.org/10.1103/PhysRevLett.103.012003)
- [12] B. I. Abelev et al. (STAR Collaboration), Longitudinal Double-Spin Asymmetry and Cross Section for Inclusive Jet Production in Polarized Proton Collisions Inclusive Jet Production in Polarized Proton Collisions
at $\sqrt{s} = 200 \text{ GeV}$, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.97.252001) **97**, 252001 [\(2006\).](http://dx.doi.org/10.1103/PhysRevLett.97.252001)
- [13] B. I. Abelev et al. (STAR Collaboration), Longitudinal Double-Spin Asymmetry for Inclusive Jet Production in Double-Spin Asymmetry for Inclusive Jet Production in $p + p$ Collisions at $\sqrt{s} = 200$ GeV, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.100.232003) 100, [232003 \(2008\).](http://dx.doi.org/10.1103/PhysRevLett.100.232003)
- [14] A. Adare et al. (PHENIX Collaboration), Inclusive doublehelicity asymmetries in neutral-pion and eta-meson produchelicity asymmetries in neutral-pion and eta-meson production in $\vec{p} + \vec{p}$ collisions at $\sqrt{s} = 200$ GeV, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.90.012007) 90, [012007 \(2014\).](http://dx.doi.org/10.1103/PhysRevD.90.012007)

A. ADARE *et al.* **PHYSICAL REVIEW D 93,** 011501(R) (2016)

- [15] L. Adamczyk et al. (STAR Collaboration), Precision Measurement of the Longitudinal Double-spin Asymmetry for Inclusive Jet Production in Polarized Proton Collisions at \sqrt{s} = 200 GeV, Phys. Rev. Lett. 115[, 092002 \(2015\)](http://dx.doi.org/10.1103/PhysRevLett.115.092002).
- [16] D. de Florian, R. Sassot, M. Stratmann, and W. Vogelsang, Evidence for Polarization of Gluons in the Proton, [Phys.](http://dx.doi.org/10.1103/PhysRevLett.113.012001) Rev. Lett. 113[, 012001 \(2014\).](http://dx.doi.org/10.1103/PhysRevLett.113.012001)
- [17] K. Adcox et al. (PHENIX Collaboration), PHENIX detector overview, [Nucl. Instrum. Methods Phys. Res., Sect. A](http://dx.doi.org/10.1016/S0168-9002(02)01950-2) 499, [469 \(2003\)](http://dx.doi.org/10.1016/S0168-9002(02)01950-2).
- [18] A. Adare et al. (PHENIX Collaboration), Inclusive cross section and single transverse spin asymmetry for very forward neutron production in polarized $p + p$ collisions forward neutron production in polarized $p + p$ collisting that $\sqrt{s} = 200$ GeV, Phys. Rev. D **88**[, 032006 \(2013\)](http://dx.doi.org/10.1103/PhysRevD.88.032006).
- [19] GEANT 3.2.1 Manual, CERN, Geneva (1993).
- [20] S. S. Adler et al. (PHENIX Collaboration), Mid-rapidity Neutral Pion Production in Proton Proton Collisions at \sqrt{s} = 200 GeV, Phys. Rev. Lett. **91**[, 241803 \(2003\).](http://dx.doi.org/10.1103/PhysRevLett.91.241803)
- [21] A. D. Martin, W. J. Stirling, R. S. Thorne, and G. Watt, Parton distributions for the LHC, [Eur. Phys. J. C](http://dx.doi.org/10.1140/epjc/s10052-009-1072-5) 63, 189 (2009).
- [22] D. de Florian, R. Sassot, M. Epele, R. J. Hernandez-Pinto, and M. Stratmann, Parton-to-pion fragmentation reloaded, Phys. Rev. D 91[, 014035 \(2015\)](http://dx.doi.org/10.1103/PhysRevD.91.014035).
- [23] D. de Florian, R. Sassot, and M. Stratmann, Global analysis of fragmentation functions for protons and charged hadrons, Phys. Rev. D 76[, 074033 \(2007\)](http://dx.doi.org/10.1103/PhysRevD.76.074033).
- [24] B. Schmidke et al. (RHIC Polarimetry Group), Run-13 Polarimetry Measurements, RHIC/CAD Accelerator Physics Note 490 (2013).
- [25] R. Sassot (DSSV Group) (private communication).
- [26] L. Adamczyk et al. (STAR Collaboration), Neutral pion cross section and spin asymmetries at intermediate pseucross section and spin asymmetries at intermediate pseudorapidity in polarized proton collisions at $\sqrt{s} = 200$ GeV, Phys. Rev. D 89[, 012001 \(2014\)](http://dx.doi.org/10.1103/PhysRevD.89.012001).