T-dependence of the Axion Mass when the U_A(1) and Chiral Symmetry Breaking Are Tied

Klabučar, D.; Horvatić, D.; Kekez, D.

Source / Izvornik: Acta Physica Polonica B: Proceedings Supplement, 2020, 13, 65 - 70

Journal article, Published version Rad u časopisu, Objavljena verzija rada (izdavačev PDF)

https://doi.org/10.5506/APhysPolBSupp.13.65

Permanent link / Trajna poveznica: https://urn.nsk.hr/urn:nbn:hr:217:922468

Rights / Prava: Attribution 4.0 International/Imenovanje 4.0 međunarodna

Download date / Datum preuzimanja: 2025-02-03



Repository / Repozitorij:

Repository of the Faculty of Science - University of Zagreb



T-DEPENDENCE OF THE AXION MASS WHEN THE $U_A(1)$ AND CHIRAL SYMMETRY BREAKING ARE TIED*

Dubravko Klabučar, Davor Horvatić

Physics Department, Faculty of Science — PMF, University of Zagreb, Croatia

Dalibor Kekez

Ruđer Bošković Institute, Zagreb, Croatia

(Received June 24, 2019)

Modulo the scale of spontaneous breaking of Peccei–Quinn symmetry, the axion mass $m_a(T)$ is given by the QCD topological susceptibility $\chi(T)$ at all temperatures T. From an approach tying the $\mathrm{U}_A(1)$ and chiral symmetry breaking and getting good T-dependence of η and η' mesons, we get $\chi(T)$ for an effective Dyson–Schwinger model of nonperturbative QCD. Comparison with lattice results for $\chi(T)$, and thus also for $m_a(T)$, shows good agreement for temperatures ranging from zero up to the double of the chiral restoration temperature T_{c} .

DOI:10.5506/APhysPolBSupp.13.65

1. Introduction

The fundamental theory of strong interactions, QCD, has the so-called Strong CP problem. Namely, there is no experimental evidence of any CP-symmetry violation in strong interactions, although there is in principle no reason why the QCD Lagrangian should not include the so-called Θ -term \mathcal{L}^{Θ} , where gluon fields $F_{\mu\nu}^{b}(x)$ comprise the CP-violating combination Q(x)

$$\mathcal{L}^{\Theta}(x) = \Theta \frac{g^2}{64 \pi^2} \epsilon^{\mu\nu\rho\sigma} F^b_{\mu\nu}(x) F^b_{\rho\sigma}(x) \equiv \Theta Q(x). \tag{1}$$

Admittedly, \mathcal{L}^{Θ} can be rewritten as a total divergence, but, unlike in QED, this does not enable discarding it in spite of the gluon fields vanishing sufficiently fast as $|x| \to \infty$. This is because of nontrivial topological structures in QCD, such as instantons, which are important for, e.g. solving of the $U_A(1)$ problem and yielding the anomalously large mass of the η' meson.

^{*} Presented at "Excited QCD 2019", Schladming, Austria, January 30–February 3, 2019.

Thus, there is no reason why the coefficient Θ of this term should be of a very different magnitude from the coefficients of the other, CP-symmetric terms comprising the usual CP-symmetric QCD Lagrangian. Nevertheless, the experimental bound on the coefficient of the term is extremely low, $|\Theta| < 10^{-10}$ [1], and consistent with zero. This is the mystery of the missing strong CP violation: why is Θ so small?

Various proposed theoretical solutions stood the test of time with varying success. A long-surviving solution, which is actually the preferred solution nowadays, is a new particle beyond the Standard Model — the axion. Important is also that axions turned out to be very interesting also for cosmology, as promising candidates for dark matter. (See, e.g., [2, 3].)

2. Axion mass from the non-Abelian axial anomaly

Peccei and Quinn introduced [4, 5] a new axial global symmetry U(1)_{PQ} which is broken spontaneously at some scale f_a . This presumably huge [6] but otherwise presently unknown scale is the key free parameter of axion theories, which determines the absolute value of the axion mass m_a . However, this constant cancels from combinations such as $m_a(T)/m_a(0)$. Hence, useful insights and applications are possible in spite of f_a being not known.

We have often, including applications at T > 0 [7–11], employed a chirally well-behaved relativistic bound-state approach to modeling nonperturbative QCD through Dyson–Schwinger equations (DSE) for Green's functions of the theory. (For reviews, see [12–14] for example.) Such calculations can yield model predictions on the QCD topological susceptibility, including its temperature dependence $\chi(T)$, which are correctly related to the QCD dynamical chiral symmetry breaking (DChSB) and restoration. It turns out that $\chi(T)$ is precisely that factor in the axion mass $m_a(T)$, which carries the nontrivial T-dependence.

2.1. Axions as quasi-Goldstone bosons

The pseudoscalar axion field a(x) arises as the (would-be massless) Goldstone boson of the spontaneous breaking of the Peccei–Quinn symmetry [15, 16]. The axion contributes to the total Lagrangian its kinetic term and its interaction with the Standard-Model fermions. However, what is important for the resolution of the strong CP problem, is that the axion also couples to the topological charge density operator Q(x) in Eq. (1). Then, the Θ -term in the QCD Lagrangian gets modified to

$$\mathcal{L}_{\text{axion}}^{\Theta +} = \mathcal{L}^{\Theta} + \frac{a(x)}{f_a} Q(x) = \left(\Theta + \frac{a}{f_a}\right) \frac{g^2}{64\pi^2} \epsilon^{\mu\nu\rho\sigma} F_{\mu\nu}^b F_{\rho\sigma}^b. \tag{2}$$

Through this coupling of the axion to gluons, the $U(1)_{PQ}$ symmetry is also broken *explicitly* by the $U_A(1)$ non-Abelian, gluon axial anomaly, so that the axion has a nonvanishing mass, $m_a \neq 0$ [15, 16].

Gluons generate an effective axion potential, and its minimization leads to the axion expectation value $\langle a \rangle$ such that the modified coefficient, multiplying the topological charge density Q(x), should vanish

$$\Theta + \frac{\langle a \rangle}{f_a} = 0. \tag{3}$$

The strong CP problem is thereby solved, irrespective of the initial value of Θ . Relaxation from any Θ -value in the early Universe towards the minimum at Eq. (3) is known as misalignment production, and the resulting axion oscillation energy is a cold dark matter candidate (e.g., see [2, 3]).

2.2. Axion mass from anomalous $U_A(1)$ breaking driven by DChSB

A direct measure of the $U_A(1)$ symmetry breaking is the topological susceptibility χ , given by the convolution of the time-ordered product \mathcal{T} of the topological charge densities Q(x) defined by Eq. (1) [or Eq. (2)]

$$\chi = \int d^4x \langle 0 | \mathcal{T} Q(x) Q(0) | 0 \rangle. \tag{4}$$

The expansion of the effective axion potential reveals in its quadratic term that the axion mass squared (times f_a^2) is equal¹ to the QCD topological susceptibility. This holds for all temperatures T

$$m_a^2(T) f_a^2 = \chi(T)$$
. (5)

On the other hand, in our study [11] of the T-dependence of the η and η' masses and the influence of the anomalous $U_A(1)$ breaking and restoration, we used the light-quark-sector result [17–19]

$$\chi(T) = \frac{-1}{\frac{1}{m_u \langle \bar{u}u(T) \rangle} + \frac{1}{m_d \langle \bar{d}d(T) \rangle} + \frac{1}{m_s \langle \bar{s}s(T) \rangle}} + C_m, \qquad (6)$$

where C_m is a very small correction term of higher orders in the small current quark masses m_q (q=u,d,s), and in the present context, we do not consider it further. Thus, the overwhelming part, namely the leading term of χ , is given by the quark condensates $\langle \bar{q}q \rangle$ (q=u,d,s), which arise as order parameters of DChSB. Their temperature dependence determines that

To a high level of accuracy, since corrections to Eq. (5) are of the order of M_{π}^2/f_a^2 [20], where the pion mass M_{π} is negligible.

of $\chi(T)$, which in turn determines the T-dependence of the anomalous part of the pseudoscalar meson masses in the η - η' complex. This is the mechanism of Ref. [11], how DChSB and chiral restoration drive, respectively, the anomalous breaking and restoration of the $U_A(1)$ symmetry of QCD.

Now, Eqs. (5) and (6) show that this mechanism determines also the T-dependence of the axion mass.

To describe η' and η mesons, it is essential to include $U_A(1)$ symmetry breaking at least at the level of the masses. This could be done simply [23–25], by adding the anomalous contribution to isoscalar meson masses as a perturbation, thanks to the fact that the $U_A(1)$ anomaly is suppressed in the limit of large number of QCD colors N_c [26, 27]. Concretely, Ref. [25] adopted Shore's equations [28], where the $U_A(1)$ -anomalous contribution to the light pseudoscalar masses is expressed through the condensates of light quarks with nonvanishing current masses. They are thus used also in $\chi(T)$ (6), since this approach has recently been extended [11] to T>0. This gave us our results for $\chi(T)$ depicted in Fig. 1.

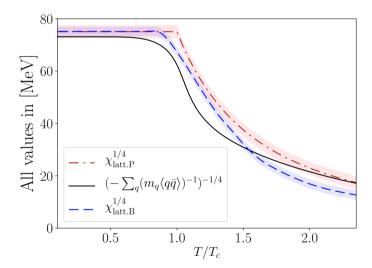


Fig. 1. The relative temperature T/T_c dependence of (the leading term of) $\chi(T)$ from our oft-adopted [7–11] chirally well-behaved DSE model (solid curve), and from lattice: dash-dotted curve extracted from Petreczky *et al.* [21] and dashed curve extracted from Borsany *et al.* [22].

Indeed, the now established smooth, crossover behavior around the pseudocritical temperature T_c for the chiral transition, is obtained for the DChSB condensates of realistically massive light quarks — *i.e.*, the quarks with realistic explicit chiral symmetry breaking [11]. In contrast, using in Eq. (6) the massless quark condensate $\langle \bar{q}q \rangle_0$ (which drops sharply to zero at T_c) instead

of the "massive" ones, would dictate a sharp transition of the second order at $T_{\rm c}$ [10, 11] also for $\chi(T)$. Obviously, this would imply that axions are massless for $T > T_{\rm c}$.

In Fig. 1, we present (the leading term of) our model-calculated [11] $\chi(T)^{1/4}$, depicted as the solid curve. Due to Eq. (5), this is our model prediction for $\sqrt{m_a(T) f_a}$. For temperatures up to $T \approx 2.3 T_c$, we compare it to the lattice results of Petreczky *et al.* [21] and of Borsany *et al.* [22], rescaled to the relative temperature T/T_c .

3. Summary

The axion mass and its temperature dependence $m_a(T)$ can be calculated in an effective model of nonperturbative QCD (up to the constant scale parameter f_a) as the square root of the topological susceptibility $\chi(T)$. We obtained it from the condensates of u-, d- and s-quarks and antiquarks calculated in the SDE approach using a simplified nonperturbative model interaction [11]. Our prediction on $m_a(T)$ is thus supported by the fact that our topological susceptibility also yields the T-dependence of the $U_A(1)$ anomaly-influenced masses of η' and η mesons which is consistent with experimental evidence [11].

Our result on $\chi(T)$ and the related axion mass is qualitatively similar to the one obtained in the framework of the NJL model [29]. Our topological susceptibility is also qualitatively similar to the pertinent lattice results [21, 22], except that our dynamical model could so far access only much smaller range of temperatures, $T < 2.4\,T_{\rm c}$. On the other hand, the lattice supports the smooth crossover transition of $\chi(T)$, which is, in our approach, the natural consequence of employing the massive-quark condensates exhibiting crossover around the chiral restoration temperature $T_{\rm c}$. Hence, the (partial) $U_A(1)$ restoration observed in Ref. [11] must also be a crossover, which in the present work, as well as in its longer counterpart [30] containing a detailed analysis of the model parameter dependence, translates into the corresponding smooth T-dependence of the axion mass.

REFERENCES

- [1] C.A. Baker et al., Phys. Rev. Lett. 97, 131801 (2006).
- [2] O. Wantz, E.P.S. Shellard, *Phys. Rev. D* 82, 123508 (2010).
- [3] J.E. Kim, S. Nam, Y.K. Semetzidis, Int. J. Mod. Phys. A 33, 1830002 (2018).
- [4] R.D. Peccei, H.R. Quinn, Phys. Rev. Lett. 38, 1440 (1977).
- [5] R.D. Peccei, H.R. Quinn, *Phys. Rev. D* 16, 1791 (1977).

- [6] M. Tanabashi et al. [Particle Data Group], Phys. Rev. D 98, 030001 (2018).
- [7] D. Horvatić, D. Klabučar, A. Radzhabov, Phys. Rev. D 76, 096009 (2007).
- [8] D. Horvatić, D. Blaschke, D. Klabučar, A.E. Radzhabov, *Phys. Part. Nucl.* 39, 1033 (2008).
- [9] D. Horvatić et al., Eur. Phys. J. A 38, 257 (2008).
- [10] S. Benić, D. Horvatić, D. Kekez, D. Klabučar, *Phys. Rev. D* 84, 016006 (2011).
- [11] D. Horvatić, D. Kekez, D. Klabučar, *Phys. Rev. D* **99**, 014007 (2019).
- [12] R. Alkofer, L. von Smekal, *Phys. Rep.* **353**, 281 (2001).
- [13] C.D. Roberts, S.M. Schmidt, *Prog. Part. Nucl. Phys.* 45, S1 (2000).
- [14] C.S. Fischer, J. Phys. G 32, R253 (2006).
- [15] S. Weinberg, Phys. Rev. Lett. 40, 223 (1978).
- [16] F. Wilczek, *Phys. Rev. Lett.* **40**, 279 (1978).
- [17] P. Di Vecchia, G. Veneziano, Nucl. Phys. B 171, 253 (1980).
- [18] H. Leutwyler, A.V. Smilga, Phys. Rev. D 46, 5607 (1992).
- [19] S. Dürr, Nucl. Phys. B **611**, 281 (2001).
- [20] M. Gorghetto, G. Villadoro, J. High Energy Phys. 1903, 033 (2019).
- [21] P. Petreczky, H.P. Schadler, S. Sharma, Phys. Lett. B 762, 498 (2016).
- [22] S. Borsanyi et al., Nature **539**, 69 (2016).
- [23] D. Klabučar, D. Kekez, *Phys. Rev. D* 58, 096003 (1998).
- [24] D. Kekez, D. Klabučar, *Phys. Rev. D* **73**, 036002 (2006).
- [25] S. Benić, D. Horvatić, D. Kekez, D. Klabučar, Phys. Lett. B 738, 113 (2014).
- [26] E. Witten, Nucl. Phys. B 156, 269 (1979).
- [27] G. Veneziano, Nucl. Phys. B 159, 213 (1979).
- [28] G.M. Shore, Nucl. Phys. B **744**, 34 (2006).
- [29] Z.Y. Lu, M. Ruggieri, Phys. Rev. D 100, 014013 (2019) [arXiv:1811.05102 [hep-ph]].
- [30] D. Horvatić, D. Kekez, D. Klabučar, *Universe* 5, 208 (2019) [arXiv:1909.09879 [hep-ph]].