# Supporting information - Choosing the Right Electrode Representation for Modeling Real Bioelectronic Interfaces: A Comprehensive Guide

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## Supplement / Prilog

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# **Supporting information**

# Choosing the Right Electrode Representation for Modeling Real Bioelectronic Interfaces: A Comprehensive Guide

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## **Table of Contents**

### 1.Convergence of the CPE integral

#### 2. Additional implementation details

**Figure S1** Additional geometry for mapping the potential from time to space via the Stabilized Convection-Diffusion Equation.

#### 3. EIS measurements and fits

**Figures S2 – S7** Electrochemical impedance spectroscopy measured and fitted data to a single domain Randles (CPE) circuit for studied materials.

### 4. CV measurements

Figure S8 Cyclic Voltammetry measurements for studied materials

### 5. Relative error for RC and CPE implementation

Figure S9 Relative error for RC and CPE implementation for each material and pulse voltage.

#### 1. Convergence of the CPE integral

The CPE integral:

$$\sigma_{CPE}(t) = \int_0^t \frac{Q_{SPEC}}{\Gamma(1-\alpha)} \frac{V_{WE}}{(t-\tau)^{\alpha}} d\tau \qquad t > 0; \ 0 < \alpha < 1$$

Is a convergent integral of a divergent function for  $\tau = t$  which creates problems for COMSOL's numerical integration algorithm and yields an error for division with zero. To solve this problem, we separate the integral in two parts:

$$\sigma_{CPE}(t) = \int_0^{t-\Delta t} \frac{Q_{SPEC}}{\Gamma(1-\alpha)} \frac{V_{WE}}{(t-\tau)^{\alpha}} d\tau + \int_{t-\Delta t}^t \frac{Q_{SPEC}}{\Gamma(1-\alpha)} \frac{V_{WE}}{(t-\tau)^{\alpha}} d\tau$$

Where  $\Delta t$  is a small time interval comparable with the time stepping of the simulation. Now the first integral does not have divergence issues as we got rid of the  $\tau = t$  point. For the second integral, because  $\Delta t$  is a very small time interval comparable to the time resolution of the simulation, we can assume the functions  $Q_{SPEC}$ ,  $V_{WE}$  and  $\alpha$  are constant for the time  $\Delta t$  and assign them the value for  $\tau = t$ . We can thus take the functions out of the integral to obtain:

$$\sigma_{CPE}(t) = \int_0^{t-\Delta t} \frac{Q_{SPEC}}{\Gamma(1-\alpha)} \frac{V_{WE}}{(t-\tau)^{\alpha}} d\tau + \frac{Q_{SPEC}(t) V_{WE}(t)}{\Gamma(1-\alpha(t))} \int_{t-\Delta t}^t \frac{1}{(t-\tau)^{\alpha}} d\tau$$

The second integral can now be solved analytically for  $\alpha < 1$  to get the final expression:

$$\sigma_{CPE}(t) = \int_0^{t-\Delta t} \frac{Q_{SPEC}}{\Gamma(1-\alpha)} \frac{V_{WE}}{(t-\tau)^{\alpha}} d\tau + \frac{Q_{SPEC}(t) V_{WE}(t)}{\Gamma(1-\alpha(t))} \frac{\Delta t^{1-\alpha}}{1-\alpha} \qquad t > \Delta t; \ 0 < \alpha < 1$$

That is numerically stable and does not cause problems in COMSOL Multiphysics. Care must be taken to make sure that the time  $\Delta t$  is much smaller than the time scale relevant for the evolution of the system in question.

#### 2. Additional implementation details



Figure S1 Additional geometry (highlighted in blue) for mapping the potential from time to space via the Stabilized Convection-Diffusion Equation. The entire electrode computed potential history at each electrode node is mapped vertically to spatial geometry

We use a convection (advection) differential equation for mapping the calculated potential history. The convection equation is a special case of the generalized convection–diffusion differential equation:

$$\frac{\partial U}{\partial t} + \nabla \cdot (\beta \ U) = \nabla \cdot (c \nabla U) + F$$

where U is the mapping variable, c is the diffusion coefficient,  $\beta$  is the convection velocity, F represents sources or sinks of the quantity U and  $\nabla$  and  $\nabla$  · represent gradient and divergence operator respectively. We obtain the desired mapping equation by setting the diffusion coefficient and sources term to zero and by setting the value of the convection velocity to be constant.

#### 3. EIS measurements and fits



S5



S6



Figures S2 – S7 Electrochemical impedance spectroscopy measured and fitted data to a single domain Randles (CPE) circuit (Figure 2b) for studied materials. Measured data is marked by points and fitted data by lines. Impedance values are depicted with circles and negative phase values with squares. Raw data in .csv form is available from the institutional repository referenced in the Supporting Information section. Color legend is the DC bias in V vs Ag/AgCl reference electrode.

#### 4. CV measurements



*Figure S8 Cyclic Voltammetry measurements for the studied materials. Measurements are performed in the voltage range from -900 mV to 800 mV vs. Ag/AgCI reference with a scan rate of 1 V/s.* 

#### 5. Relative error for RC and CPE implementation



Figure S9 Relative error for RC and CPE implementation for each material and pulse voltage.