Extrinsic Spin Hall Effect Induced by Iridium Impurities in Copper

Niimi, Y.; Morota, M.; Wei, D. H.; Deranlot, Cyrile; Basletić, Mario; Hamzić, Amir; Fert, A.; Otani, Y.

Source / Izvornik: **Physical Review Letters, 2011, 106**

Journal article, Published version Rad u časopisu, Objavljena verzija rada (izdavačev PDF)

<https://doi.org/10.1103/PhysRevLett.106.126601>

Permanent link / Trajna poveznica: <https://urn.nsk.hr/urn:nbn:hr:217:994299>

Rights / Prava: [In copyright](http://rightsstatements.org/vocab/InC/1.0/) / [Zaštićeno autorskim pravom.](http://rightsstatements.org/vocab/InC/1.0/)

Download date / Datum preuzimanja: **2024-07-10**

Repository / Repozitorij:

[Repository of the Faculty of Science - University o](https://repozitorij.pmf.unizg.hr)f [Zagreb](https://repozitorij.pmf.unizg.hr)

Extrinsic Spin Hall Effect Induced by Iridium Impurities in Copper

Y. Niimi,^{1[,*](#page-4-0)} M. Morota,¹ D. H. Wei,¹ C. Deranlot,² M. Basletic,³ A. Hamzic,³ A. Fert,² and Y. Otani^{1,4}

¹Institute for Solid State Physics, University of Tokyo, 5-1-5 Kashiwa-no-ha, Kashiwa, Chiba 277-8581, Japan
²Unité Mixte de Physique CNRS/Thales, 91767 Palaiseau France associée à l'Université de Paris Sud, 91405 Orsa

 2 Unité Mixte de Physique CNRS/Thales, 91767 Palaiseau France associée à l'Université de Paris-Sud, 91405 Orsay, France

 3 Department of Physics, Faculty of Science, University of Zagreb, P.O. Box 331, HR-10002 Zagreb, Croatia

RIKEN-ASI, 2-1 Hirosawa, Wako, Saitama 351-0198, Japan (Received 12 January 2011; published 22 March 2011)

We study the extrinsic spin Hall effect induced by Ir impurities in Cu by injecting a pure spin current into a CuIr wire from a lateral spin valve structure. While no spin Hall effect is observed without Ir impurity, the spin Hall resistivity of CuIr increases linearly with the impurity concentration. The spin Hall angle of CuIr, (2.1 ± 0.6) % throughout the concentration range between 1% and 12%, is practically independent of temperature. These results represent a clear example of predominant skew scattering extrinsic contribution to the spin Hall effect in a nonmagnetic alloy.

DOI: [10.1103/PhysRevLett.106.126601](http://dx.doi.org/10.1103/PhysRevLett.106.126601) PACS numbers: 72.25.Ba, 72.25.Mk, 75.70.Cn, 75.75.-c

The generation of pure spin currents, flows of only spin angular momentum without charge current, should play an important role in the next generation spintronic devices [[1\]](#page-4-1). The spin Hall effect (SHE) is one of the promising ways to create pure spin currents in nonmagnetic materials without using external magnetic fields or ferromagnets. The SHE was first predicted theoretically a long time ago [[2\]](#page-4-2) and has recently received renewed interest which came from several theoretical predictions of SHE in nonmagnetic materials [\[3,](#page-4-3)[4](#page-4-4)] and from the first experimental observation of the SHE in semiconductor systems using an optical method [\[5\]](#page-4-5). By flowing the electric current into GaAs samples, spin-up and down electrons are accumulated on the opposite sides of the samples, which can be seen by scanning Kerr rotation microscopy. This is referred to as the direct spin Hall effect (DSHE). However, the spin Hall (SH) angle, which is defined as the ratio of the SH conductivity to the charge conductivity and represents the maximum yield of the transformation of charge into spin current density, is extremely small in semiconductors. Therefore an important challenge is to find more efficient materials for this transformation. Larger SHEs have been recently found in noble metals such as Pt [\[6](#page-4-6)–[10](#page-4-7)] and Au [\[9](#page-4-8)[,11](#page-4-9)[,12\]](#page-4-10) and this has triggered an important effort of research on the SHE in metallic materials.

The SHE relies on spin-orbit (SO) interactions in materials and can be generated by intrinsic or extrinsic mechanisms. Recent theoretical works predict that the large SH angles of 4d and 5d transition metals, about 1% in recent results on Pt, for example [[9](#page-4-8)[,10\]](#page-4-7), stem from the intrinsic mechanism based on the degeneracy of d orbits by SO coupling [[13](#page-4-11)–[15](#page-4-12)]. This scenario has been supported by recent systematic experiments on the SHEs in 4d and 5d transition metals [\[10\]](#page-4-7). The extrinsic SHE, on the other hand, relies on scattering by impurities (or other defects) presenting strong SO interactions [\[16–](#page-4-13)[18\]](#page-4-14). There are two types of mechanisms, namely, the skew scattering [[19\]](#page-4-15) and the side jump [\[20\]](#page-4-16). In the former case, the SH resistivity (ρ_{SHE}) is proportional to the resistivity induced by the impurities (ρ_{imp}), while, for side-jump effects, $\rho_{\text{SHE}} \propto$ $\rho_{\rm imp}^2$ when the impurities are the only source of resistivity or $\rho_{\text{SHE}} \propto \rho_{\text{imp}} \rho_{\text{total}}$ when ρ_{total} includes an additional contribution from scattering potentials with weak SO interactions. A definite interest of the extrinsic SHE is that one can control the SH angle by changing the combination of host and impurity metals as well as by tuning the impurity concentration. In particular, the relation between the SHE and the resistivity can be studied not only by varying the temperature but also, in a much wider range, by changing the concentration of impurities.

A series of pioneering works to this end had been performed in the 1980s by a part of the present authors using a ternary system consisting of a Cu matrix doped with a Mn spin polarizer and 5d impurities such as Lu, Ta, and Ir [[21\]](#page-4-17). Large SH angles had been obtained, positive for CuIr (2.6%) or negative for CuLu (-1.2%) , and had been as-
cribed to resonant scattering on 5*d* impurity states split into cribed to resonant scattering on $5d$ impurity states split into $5/2$ and $3/2$ levels by SO interaction. Therefore we put our focus on Ir as a strong SO scatterer. In order to determine the SH angle, either DSHE or inverse SHE (ISHE) is measured as follows: in DSHE experiments, the spins accumulated on the side surfaces of materials with strong SO interactions are detected with ferromagnetic contacts. In ISHE experiments, spin currents are converted into charge currents and then the potential drop along the current direction is detected. ISHE measurements have been intensively carried out in recent years by means of the pure spin current injection $[7,8,10-12,22]$ $[7,8,10-12,22]$ $[7,8,10-12,22]$ $[7,8,10-12,22]$ $[7,8,10-12,22]$ $[7,8,10-12,22]$ $[7,8,10-12,22]$ or the microwave driven spin pumping techniques [\[6](#page-4-6),[9](#page-4-8)]. In the present study we have adopted the spin absorption method using a lateral spin valve structure to measure the ISHE induced in Cu by Ir impurities. The final goal of the present study is to identify if the major contribution to the SHE is the skew scattering by the Ir impurities and what is the magnitude of the SH angle

0031-9007/11/106(12)/126601(4) 126601-1 © 2011 American Physical Society

that can be obtained with such type of heavy impurity. We find that introducing Ir impurities to pure Cu which exhibits no SHE, increases the SH resistivity in proportion of the Ir concentration throughout the concentration range from 1% to 12%. This linear variation clearly shows that the skew scattering is the dominant mechanism in the CuIr alloys. The slope of a ρ_{SHE} vs ρ_{imp} plot gives the SH angle α_H of (2.1 ± 0.6) % for CuIr.

Samples have been fabricated on a thermally oxidized silicon substrate using electron beam lithography on polymethyl-methacrylate resist and a subsequent lift-off process. We have used a lateral spin valve structure which consists of two Permalloy ($Ni₈₁Fe₁₉$; hereafter Py) wires (30 nm thick and 100 nm wide) and a CuIr middle wire (20 nm thick and 250 nm wide) bridged by a Cu wire (100 nm thick and 100 nm wide), as shown in Fig. [1\(a\)](#page-2-0). In this work, the distance between the two Py wires (L) is fixed to 1 μ m and the CuIr wire is placed just in the middle of the two Py wires. To induce a difference between the switching fields of the two Py wires, one of them [Py1 in Fig. $1(a)$] has two large pads at the edges. The Py wires were grown by electron beam evaporation, while the middle CuIr wires with different Ir concentrations (0%, 1%, 3%, 6%, 9%, and 12%) were deposited by magnetron sputtering. The Cu bridge was fabricated by a Joule heating

FIG. 1 (color online). (a) Scanning electron microscopy image of a spin Hall device consisting of two Py wires and a CuIr middle wire bridged by a Cu wire. (b) Schematic of the mechanism of ISHE due to the spin absorption effect. (c) Inverse spin Hall resistance of CuIr with different Ir concentrations measured at $T = 10$ K. For comparison, the direct spin Hall resistance of CuIr (9%) is also shown in the inset. The bottom panel shows a typical AMR signal of Py1.

evaporator using a 99.9999% purity source. Prior to Cu evaporation a careful Ar ion beam etching (600 V beam voltage) was carried out for 1 min in order to clean the surfaces of Py and CuIr wires and to obtain highly transparent Ohmic contacts. Transport measurements were performed using a standard ac lock-in technique and a 4He flow cryostat. The magnetic field is applied along the hard and easy axes of Py for ISHE and nonlocal spin valve (NLSV) measurements, respectively. For each Ir concentration, at least three different samples from the same batch have been measured to check the reproducibility.

First we discuss the ISHE results for CuIr with different Ir concentrations. The measurement circuit is depicted in Fig. [1\(b\).](#page-2-0) When the electric current flows from Py1 to the left side of the Cu wire, the resulting spin accumulation induces a pure spin current on the right side of the Cu wire. As we discuss in the next paragraph, a major part of the pure spin current is absorbed in the CuIr middle wire below the Cu wire since the spin diffusion length of CuIr $($ \sim 10 nm) is much smaller than that of Cu. The deflection in the same direction of the opposite spin-up and down vertical currents by skew scattering on the Ir impurities generates the ISHE signal. The ISHE resistance R_{ISHE} (equal to the ISHE voltage V_{ISHE} divided by the charge current I_{C}), is plotted in Fig. [1\(c\)](#page-2-0) as a function of the magnetic field applied perpendicularly to the Py wires. R_{ISHE} increases linearly with the magnetic field up to \sim 2000 Oe and then flattens off at the saturation of the

FIG. 2 (color online). (a) NLSV signals measured at $T = 10$ K with a CuIr (6%) middle wire (red) and without CuIr wire (blue). (b) Spin diffusion length λ_M of CuIr at 10 K as a function of Ir concentration.

magnetization of Py1 [see the anisotropic magnetoresistance (AMR) curve of Py1 in the bottom panel of Fig. [1\(c\)\]](#page-2-0). It can also be seen in Fig. [1\(c\)](#page-2-0) that R_{ISHE} increases with increasing Ir. The inversion of the probe configuration [i.e., $I_+ \Leftrightarrow V_+$, $I_- \Leftrightarrow V_-$ in Fig. [1\(a\)\]](#page-2-0) ena-
bles one to measure the DSHE as previously reported [7.8] bles one to measure the DSHE as previously reported [[7](#page-4-18),[8\]](#page-4-19). We could confirm that the SH resistance due to the DSHE is exactly the same as R_{ISHE} [see the inset of Fig. [1\(c\)](#page-2-0)]. This verifies the Onsager reciprocal relation in our system.

In order to estimate the spin diffusion length of CuIr and to use it in the evaluation of the spin current absorbed into the CuIr wire, we have measured the NLSV signal of our device. Note that in this case the magnetic field is applied along the easy axis of the two Py wires. As can be seen in Fig. $2(a)$, by inserting the CuIr middle wire, the spin accumulation signal $\Delta R_{\rm S}^{\rm with} \equiv \Delta V_{\rm S}^{\rm with}/I_{\rm C}$) is reduced to 0.15A $R_{\rm W}^{\rm without}$ is the spin accumulation $0.15\Delta R_{\rm S}^{\rm without}$ where $\Delta R_{\rm S}^{\rm without}$ is the spin accumulation signal without middle wires. This indicates that most of the pure spin current injected from Py1 is absorbed in the CuIr wire. From the one-dimensional spin diffusion model [\[23\]](#page-4-21), the normalized spin signal $\Delta R_S^{\text{with}}/\Delta R_S^{\text{without}}$ can be expressed as follows;

$$
\frac{\Delta R_S^{\text{with}}}{\Delta R_S^{\text{without}}} \approx \frac{2R_M \sinh(L/\lambda_N)}{R_N \{\cosh(L/\lambda_N) - 1\} + 2R_M \sinh(L/\lambda_N)}
$$
(1)

where $R_{\rm N}$ and $R_{\rm M}$ are the spin resistances of Cu and CuIr middle wire, respectively. The spin resistance R_X of material "X" is defined as $\rho_X \lambda_X/(1 - p_X^2) A_X$, where ρ_X , λ_X , ρ_X and A_X are respectively the electrical resistivity the p_X and A_X are, respectively, the electrical resistivity, the spin diffusion length, the spin polarization, and the effective cross sectional area involved in the equations of the one-dimensional spin diffusion model [[24](#page-4-22)]. As reported previously [[25](#page-4-23)], we can determine λ_{N} , λ_{F} , and p_{F} by measuring the NLSV signal without middle wire as a function of L. In the present study, $\lambda_N = 1.3 \mu m$, $\lambda_F =$ 5 nm, and $p_F = 0.23$ at $T = 10$ K. Thus, we can extract the spin diffusion length λ_M of the CuIr middle wire from Eq. ([1\)](#page-3-0). As can be seen in Fig. [2\(b\)](#page-2-1), λ_M drastically decreases with increasing the Ir atom.

We then calculate ρ_{SHE} as follows [\[1](#page-4-1),[26](#page-4-24)]:

$$
\rho_{\text{SHE}} = \frac{w_{\text{M}}}{x} \left(\frac{I_{\text{C}}}{\bar{I}_{\text{S}}}\right) \Delta R_{\text{ISHE}},\tag{2}
$$

where \bar{I}_S is the effective spin current injected (vertically for $\lambda_M \ll w_N$) into the CuIr wire and generating the ISHE, w_M is the width of CuIr wire and x is a correction factor taking into account the fact that the horizontal current driven by the ISHE voltage balancing the SO deflections is partially shunted by the Cu wire above the CuIr/Cu interface. The correction factor x is derived from additional measurements of the resistance of the CuIr wire with and without the interface with Cu and is found to be 0.36 ± 0.08 for all the samples (see supplemental material [[27](#page-4-25)]); for the DSHE the same factor accounts for the shunting of the current through Cu. ΔR_{ISHE} is defined as the difference between R_{ISHE} at saturation field (above \sim 2000 Oe) and R_{ISHE} at zero field [see Fig. [1\(c\)\]](#page-2-0). In our case λ_M is generally smaller than the thickness of the CuIr middle wire. The spin current injected from the interface with Cu decreases in the CuIr wire, exponentially in the limit $\lambda_M \ll t_M \ll w_N$, linearly down to zero at the bottom of CuIr for $t_M \ll \lambda_M \ll w_N$, the general expression of \overline{I} for values of t_M (20 nm) and λ_M [5–27 nm in Fig. $\bar{I}_\text{S}/I_\text{C}$ for values of t_M (20 nm) and λ_M [5–27 nm in Fig. [2\(b\)\]](#page-2-1) much smaller than w_N ([10](#page-4-7)0 nm) being [10];

$$
\frac{\bar{I}_{S}}{I_{C}} = \frac{\int_{0}^{t_{M}} I_{S}(z)dz}{t_{M}I_{C}} = \frac{\lambda_{M}}{t_{M}} \frac{(1 - e^{-t_{M}/\lambda_{M}})^{2}}{1 - e^{-2t_{M}/\lambda_{M}}} \frac{I_{S}(z = 0)}{I_{C}}
$$
\n
$$
\approx \frac{\lambda_{M}}{t_{M}} \frac{(1 - e^{-t_{M}/\lambda_{M}})^{2}}{1 - e^{-2t_{M}/\lambda_{M}}} \frac{2p_{F}R_{F}\sinh(L/2\lambda_{N})}{[R_{N}\{\cosh(L/\lambda_{N}) - 1\} + 2R_{F}(e^{L/\lambda_{N}} - 1)] + 2R_{M}\sinh(L/\lambda_{N})}.
$$
\n(3)

By using Eqs. [\(2\)](#page-3-1) and ([3\)](#page-3-2) we can derive the SH resistivity ρ_{SHE} from ΔR_{ISHE} . In Fig. [3](#page-4-26) we plot ρ_{SHE} of CuIr as a function of the resistivity induced by the Ir impurities, i.e., ρ_{CuIr} - ρ_{Cu} . It nicely follows a simple linear dependence up to Ir concentration of 12%. This clearly shows that the dominant mechanism of the extrinsic SHE induced by the Ir impurities is the skew scattering. The SH angle characteristic of this skew scattering, $\alpha_H = \rho_{SHE}/\rho_{imp}$, is $(2.1 \pm 0.6)\%$. In the previous measurements of the ISHE due to 0.6 %. In the previous measurements of the ISHE due to the skew scattering induced by Ir impurities in Cu after spin-polarization of the current by dilute Mn impurities (Mn impurities alone not contributing to the Hall effect), $\alpha_{\rm H}$ was 2.6%, which is quantitatively consistent with our result [[21](#page-4-17)].

As shown in Fig. [4](#page-4-27), the SH angle changes only weakly as a function of temperature. This is an additional proof for the mechanism of skew scattering by impurities since the contributions from intrinsic SHE or impurity scattering with side jump would be affected by the temperature dependence of the total resistivity. Finally, let us mention some results we obtained on the SH resistivity of AgIr. In this case, the estimated SH angle is definitely smaller, 0.6%. This large reduction is probably due to the very small solubility of Ir in Ag [[28](#page-4-28)].

In conclusion, we have measured the SH resistivity of the SHE induced by Ir impurities in Cu. The SH resistivity ρ_{SHE} is approximately proportional to the impurityinduced resistivity ρ_{imp} and practically temperature

FIG. 3 (color online). Spin Hall resistivity ρ_{SHE} as a function of the resistivity induced by Ir impurities, i.e., $\rho_{\text{CuIr}} - \rho_{\text{Cu}}$ at $T = 10$ K. The error har along the y axis is found by calculating $T = 10$ K. The error bar along the y axis is found by calculating the standard deviation among at least three different samples on the same batch. The error bar for x axis is within the dot. The inset shows $\rho_{\text{CuIr}} - \rho_{\text{Cu}}$ vs Ir concentration in Cu.

independent, which allows us to ascribe it to skew scattering on the Ir impurities. For the SH angle, characteristic parameter of the transformation of charge into spin current, we find 2.1%, which is quantitatively consistent with the value derived in previous experiments on CuIr, 2.6% [[21\]](#page-4-17). Such values of the SH angle are larger than those obtained with pure metals $[6–10]$ $[6–10]$ $[6–10]$ and confirm that scattering by impurities is a very promising way to obtain large SH angles, as it is predicted by several recent skew scattering calculations papers [\[16–](#page-4-13)[18](#page-4-14)]. Fert and Levy [\[18\]](#page-4-14) have calculated the contributions from both skew scattering and scattering with side jump on impurities in Cu. For Ir impurities, they predict predominant skew scattering effects in the concentration range of our experiments, in agreement with our results. However, for other types of impurities (Os, Ta) in Cu, they find that the side-jump contribution to the SH angle can be definitely larger, that is a few percent for concentrations in the 1% range and

FIG. 4 (color online). Temperature dependence of spin Hall angle of CuIr with different Ir concentrations.

therefore above 10% for concentrations in the 10% range [\[18\]](#page-4-14). Alloys combining side-jump and skew scattering effects in such a concentration range are promising to obtain a large SH angle and an efficient transformation of charge current into spin current in devices without magnetic components.

We acknowledge helpful discussions with H. Jaffres, S. Takahashi, and S. Maekawa, and numerical simulations performed by P. Metaxas and P. Bortoloti. We would also like to thank Y. Iye and S. Katsumoto for the use of the lithography facilities. This work was supported by KAKENHI and a Grant-in-Aid for Scientific Research in Priority Area from MEXT.

[*n](#page-1-0)iimi@issp.u-tokyo.ac.jp

- [1] See, for example, S. Maekawa, Concepts in Spin Electronics (Oxford University Press, Oxford, 2006).
- [2] M. I. Dyakonov and V. I. Perel, [Phys. Lett. A](http://dx.doi.org/10.1016/0375-9601(71)90196-4) 35, 459 [\(1971\)](http://dx.doi.org/10.1016/0375-9601(71)90196-4).
- [3] J. E. Hirsch, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.83.1834) **83**, 1834 (1999).
- [4] S. Zhang, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.85.393) 85, 393 (2000).
- [5] Y. K. Kato et al., Science 306[, 1910 \(2004\).](http://dx.doi.org/10.1126/science.1105514)
- [6] E. Saitoh et al., [Appl. Phys. Lett.](http://dx.doi.org/10.1063/1.2199473) 88, 182509 (2006).
- [7] T. Kimura et al., Phys. Rev. Lett. 98[, 156601 \(2007\)](http://dx.doi.org/10.1103/PhysRevLett.98.156601).
- [8] L. Vila, T. Kimura, and Y. Otani, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.99.226604) 99, [226604 \(2007\).](http://dx.doi.org/10.1103/PhysRevLett.99.226604)
- [9] O. Mosendz et al., [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.104.046601) **104**, 046601 [\(2010\)](http://dx.doi.org/10.1103/PhysRevLett.104.046601); Phys. Rev. B 82[, 214403 \(2010\)](http://dx.doi.org/10.1103/PhysRevB.82.214403).
- [10] M. Morota et al., [arXiv:1008.0158.](http://arXiv.org/abs/1008.0158)
- [11] T. Seki et al., [Nature Mater.](http://dx.doi.org/10.1038/nmat2098) 7, 125 (2008).
- [12] G. Mihajlović et al., Phys. Rev. Lett. **103**[, 166601 \(2009\).](http://dx.doi.org/10.1103/PhysRevLett.103.166601)
- [13] H. Kontani et al., [J. Phys. Soc. Jpn.](http://dx.doi.org/10.1143/JPSJ.76.103702) **76**, 103702 (2007).
- [14] T. Tanaka et al., Phys. Rev. B 77[, 165117 \(2008\)](http://dx.doi.org/10.1103/PhysRevB.77.165117).
- [15] H. Kontani et al., Phys. Rev. Lett. **102**[, 016601 \(2009\)](http://dx.doi.org/10.1103/PhysRevLett.102.016601).
- [16] M. Gradhand et al., Phys. Rev. Lett. **104**[, 186403 \(2010\).](http://dx.doi.org/10.1103/PhysRevLett.104.186403)
- [17] B. Gu et al., Phys. Rev. Lett. **105**[, 216401 \(2010\).](http://dx.doi.org/10.1103/PhysRevLett.105.216401)
- [18] A. Fert and P.M. Levy, [arXiv:1012.3657.](http://arXiv.org/abs/1012.3657)
- [19] J. Smit, [Physica \(Amsterdam\)](http://dx.doi.org/10.1016/S0031-8914(58)93541-9) **24**, 39 (1958).
- [20] L. Berger, Phys. Rev. B 2[, 4559 \(1970\)](http://dx.doi.org/10.1103/PhysRevB.2.4559).
- [21] A. Fert et al., [J. Magn. Magn. Mater.](http://dx.doi.org/10.1016/0304-8853(81)90079-2) **24**, 231 (1981).
- [22] S.O. Valenzuela and M. Tinkham, [Nature \(London\)](http://dx.doi.org/10.1038/nature04937) 442 , [176 \(2006\)](http://dx.doi.org/10.1038/nature04937).
- [23] S. Takahashi and S. Maekawa, [Phys. Rev. B](http://dx.doi.org/10.1103/PhysRevB.67.052409) 67, 052409 [\(2003\)](http://dx.doi.org/10.1103/PhysRevB.67.052409).
- [24] p_N and p_M are zero since Cu and CuIr are nonmagnetic metals. $A_N = w_N t_N$ for $\lambda_N \gg t_N$, $A_F = w_F w_N$ for $\lambda_F \ll$ t_F , and $A_M = w_M w_N \tanh(t_M/\lambda_M)$ for t_M , $\lambda_M \ll w_N$. The product $A_N \lambda_N$ ($A_F \lambda_F$, $A_M \lambda_M$) characterizes the effective volume of spin relaxation in N (F, M).
- [25] T. Kimura, T. Sato, and Y. Otani, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.100.066602) 100, [066602 \(2008\).](http://dx.doi.org/10.1103/PhysRevLett.100.066602)
- [26] S. Takahashi and S. Maekawa, [Sci. Tech. Adv. Mater.](http://dx.doi.org/10.1088/1468-6996/9/1/014105) 9, [014105 \(2008\).](http://dx.doi.org/10.1088/1468-6996/9/1/014105)
- [27] See supplemental material at [http://link.aps.org/](http://link.aps.org/supplemental/10.1103/PhysRevLett.106.126601) [supplemental/10.1103/PhysRevLett.106.126601](http://link.aps.org/supplemental/10.1103/PhysRevLett.106.126601) for detailed information about how to estimate x experimentally.
- [28] I. Karakaya and W.T. Thompson, [Bull. Alloy Phase](http://dx.doi.org/10.1007/BF02873021) Diagrams 7[, 359 \(1986\)](http://dx.doi.org/10.1007/BF02873021).