

# Measurements of mass-dependent azimuthal anisotropy in central p+Au, d+Au, and 3He+Au collisions at $\sqrt{s_{NN}}=200$ GeV

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Adare, A.; ...; Makek, Mihael; ...; Vukman, Nikola; ...; Zou, L.

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**Measurements of mass-dependent azimuthal anisotropy in central  $p + \text{Au}$ ,  $d + \text{Au}$ ,  
and  $^3\text{He} + \text{Au}$  collisions at  $\sqrt{s_{NN}} = 200 \text{ GeV}$**

A. Adare,<sup>13</sup> C. Aidala,<sup>41</sup> N. N. Ajitanand,<sup>57,\*</sup> Y. Akiba,<sup>52,53,†</sup> M. Alfred,<sup>23</sup> V. Andrieux,<sup>41</sup> N. Apadula,<sup>28,58</sup> H. Asano,<sup>34,52</sup> B. Azmoun,<sup>7</sup> V. Babintsev,<sup>24</sup> A. Bagoly,<sup>17</sup> M. Bai,<sup>6</sup> N. S. Bandara,<sup>40</sup> B. Bannier,<sup>58</sup> K. N. Barish,<sup>8</sup> S. Bathe,<sup>5,53</sup> A. Bazilevsky,<sup>7</sup> M. Beaumier,<sup>8</sup> S. Beckman,<sup>13</sup> R. Belmont,<sup>13,41</sup> A. Berdnikov,<sup>55</sup> Y. Berdnikov,<sup>55</sup> D. S. Blau,<sup>33,44</sup> M. Boer,<sup>36</sup> J. S. Bok,<sup>46</sup> K. Boyle,<sup>53</sup> M. L. Brooks,<sup>36</sup> J. Bryslawskij,<sup>5,8</sup> V. Bumazhnov,<sup>24</sup> S. Campbell,<sup>14,28</sup> V. Canoa Roman,<sup>58</sup> R. Cervantes,<sup>58</sup> C.-H. Chen,<sup>53</sup> C. Y. Chi,<sup>14</sup> M. Chiu,<sup>7</sup> I. J. Choi,<sup>25</sup> J. B. Choi,<sup>10,\*</sup> T. Chujo,<sup>61</sup> Z. Citron,<sup>63</sup> M. Connors,<sup>21,53</sup> N. Cronin,<sup>42,58</sup> M. Csanád,<sup>17</sup> T. Csörgő,<sup>18,64</sup> T. W. Danley,<sup>47</sup> A. Datta,<sup>45</sup> M. S. Daugherty,<sup>1</sup> G. David,<sup>7,58</sup> K. DeBlasio,<sup>45</sup> K. Dehmelt,<sup>58</sup> A. Denisov,<sup>24</sup> A. Deshpande,<sup>53,58</sup> E. J. Desmond,<sup>7</sup> A. Dion,<sup>58</sup> P. B. Diss,<sup>39</sup> D. Dixit,<sup>58</sup> J. H. Do,<sup>65</sup> A. Drees,<sup>58</sup> K. A. Drees,<sup>6</sup> J. M. Durham,<sup>36</sup> A. Durum,<sup>24</sup> A. Enokizono,<sup>52,54</sup> H. En'yo,<sup>52</sup> S. Esumi,<sup>61</sup> B. Fadem,<sup>42</sup> W. Fan,<sup>58</sup> N. Feege,<sup>58</sup> D. E. Fields,<sup>45</sup> M. Finger,<sup>9</sup> M. Finger, Jr.,<sup>9</sup> S. L. Fokin,<sup>33</sup> J. E. Frantz,<sup>47</sup> A. Franz,<sup>7</sup> A. D. Frawley,<sup>20</sup> Y. Fukuda,<sup>61</sup> C. Gal,<sup>58</sup> P. Gallus,<sup>15</sup> P. Garg,<sup>3,58</sup> H. Ge,<sup>58</sup> F. Giordano,<sup>25</sup> A. Glenn,<sup>35</sup> Y. Goto,<sup>52,53</sup> N. Grau,<sup>2</sup> S. V. Greene,<sup>62</sup> M. Grosse Perdekamp,<sup>25</sup> T. Gunji,<sup>12</sup> H. Guragain,<sup>21</sup> T. Hachiya,<sup>52,53</sup> J. S. Haggerty,<sup>7</sup> K. I. Hahn,<sup>19</sup> H. Hamagaki,<sup>12</sup> H. F. Hamilton,<sup>1</sup> S. Y. Han,<sup>19</sup> J. Hanks,<sup>58</sup> S. Hasegawa,<sup>29</sup> T. O. S. Haseler,<sup>21</sup> K. Hashimoto,<sup>52,54</sup> X. He,<sup>21</sup> T. K. Hemmick,<sup>58</sup> J. C. Hill,<sup>28</sup> K. Hill,<sup>13</sup> A. Hodges,<sup>21</sup> R. S. Hollis,<sup>8</sup> K. Homma,<sup>22</sup> B. Hong,<sup>32</sup> T. Hoshino,<sup>22</sup> N. Hotvedt,<sup>28</sup> J. Huang,<sup>7</sup> S. Huang,<sup>62</sup> K. Imai,<sup>29</sup> J. Imrek,<sup>16</sup> M. Inaba,<sup>61</sup> A. Iordanova,<sup>8</sup> D. Isenhower,<sup>1</sup> D. Ivanishchev,<sup>51</sup> B. V. Jacak,<sup>58</sup> M. Jezghani,<sup>21</sup> Z. Ji,<sup>58</sup> J. Jia,<sup>7,57</sup> X. Jiang,<sup>36</sup> B. M. Johnson,<sup>7,21</sup> V. Jorjadze,<sup>58</sup> D. Jouan,<sup>49</sup> D. S. Jumper,<sup>25</sup> S. Kanda,<sup>12</sup> J. H. Kang,<sup>65</sup> D. Kapukchyan,<sup>8</sup> S. Karthas,<sup>58</sup> D. Kawall,<sup>40</sup> A. V. Kazantsev,<sup>33</sup> J. A. Key,<sup>45</sup> V. Khachatryan,<sup>58</sup> A. Khanzadeev,<sup>51</sup> C. Kim,<sup>8,32</sup> D. J. Kim,<sup>30</sup> E.-J. Kim,<sup>10</sup> G. W. Kim,<sup>19</sup> M. Kim,<sup>56</sup> M. H. Kim,<sup>32</sup> B. Kimelman,<sup>42</sup> D. Kincses,<sup>17</sup> E. Kistenev,<sup>7</sup> R. Kitamura,<sup>12</sup> J. Klatsky,<sup>20</sup> D. Kleinjan,<sup>8</sup> P. Kline,<sup>58</sup> T. Koblesky,<sup>13</sup> B. Komkov,<sup>51</sup> D. Kotov,<sup>51,55</sup> S. Kudo,<sup>61</sup> B. Kurgyis,<sup>17</sup> K. Kurita,<sup>54</sup> M. Kurosawa,<sup>52,53</sup> Y. Kwon,<sup>65</sup> R. Lacey,<sup>57</sup> J. G. Lajoie,<sup>28</sup> A. Lebedev,<sup>28</sup> S. Lee,<sup>65</sup> S. H. Lee,<sup>28,58</sup> M. J. Leitch,<sup>36</sup> Y. H. Leung,<sup>58</sup> N. A. Lewis,<sup>41</sup> X. Li,<sup>11</sup> X. Li,<sup>36</sup> S. H. Lim,<sup>36,65</sup> M. X. Liu,<sup>36</sup> V.-R. Loggins,<sup>25</sup> S. Lökös,<sup>17,18</sup> K. Lovasz,<sup>16</sup> D. Lynch,<sup>7</sup> T. Majoros,<sup>16</sup> Y. I. Makdisi,<sup>6</sup> M. Makek,<sup>66</sup> A. Manion,<sup>58</sup> V. I. Manko,<sup>33</sup> E. Mannel,<sup>7</sup> H. Masuda,<sup>54</sup> M. McCumber,<sup>36</sup> P. L. McGaughey,<sup>36</sup> D. McGlinchey,<sup>13,36</sup> C. McKinney,<sup>25</sup> A. Meles,<sup>46</sup> M. Mendoza,<sup>8</sup> W. J. Metzger,<sup>18</sup> A. C. Mignerey,<sup>39</sup> D. E. Mihalik,<sup>58</sup> A. Milov,<sup>63</sup> D. K. Mishra,<sup>4</sup> J. T. Mitchell,<sup>7</sup> G. Mitsuka,<sup>53</sup> S. Miyasaka,<sup>52,60</sup> S. Mizuno,<sup>52,61</sup> A. K. Mohanty,<sup>4</sup> P. Montuenga,<sup>25</sup> T. Moon,<sup>65</sup> D. P. Morrison,<sup>7</sup> S. I. Morrow,<sup>62</sup> T. V. Moukhanova,<sup>33</sup> T. Murakami,<sup>34,52</sup> J. Murata,<sup>52,54</sup> A. Mwai,<sup>57</sup> K. Nagai,<sup>60</sup> K. Nagashima,<sup>22</sup> T. Nagashima,<sup>54</sup> J. L. Nagle,<sup>13</sup> M. I. Nagy,<sup>17</sup> I. Nakagawa,<sup>52,53</sup> H. Nakagomi,<sup>52,61</sup> K. Nakano,<sup>52,60</sup> C. Nattrass,<sup>59</sup> P. K. Netrakanti,<sup>4</sup> T. Niida,<sup>61</sup> S. Nishimura,<sup>12</sup> R. Nouicer,<sup>7,53</sup> T. Novák,<sup>18,64</sup> N. Novitzky,<sup>30,58</sup> A. S. Nyanin,<sup>33</sup> E. O'Brien,<sup>7</sup> C. A. Ogilvie,<sup>28</sup> J. D. Orjuela Koop,<sup>13</sup> J. D. Osborn,<sup>41</sup> A. Oskarsson,<sup>37</sup> G. J. Ottino,<sup>45</sup> K. Ozawa,<sup>31,61</sup> R. Pak,<sup>7</sup> V. Pantuev,<sup>26</sup> V. Papavassiliou,<sup>46</sup> J. S. Park,<sup>56</sup> S. Park,<sup>52,56,58</sup> S. F. Pate,<sup>46</sup> M. Patel,<sup>28</sup> J.-C. Peng,<sup>25</sup> W. Peng,<sup>62</sup> D. V. Perepelitsa,<sup>7,13</sup> G. D. N. Perera,<sup>46</sup> D. Yu. Peressouko,<sup>33</sup> C. E. PerezLara,<sup>58</sup> J. Perry,<sup>28</sup> R. Petti,<sup>7,58</sup> M. Phipps,<sup>7,25</sup> C. Pinkenburg,<sup>7</sup> R. Pinson,<sup>1</sup> R. P. Pisani,<sup>7</sup> A. Pun,<sup>47</sup> M. L. Purschke,<sup>7</sup> P. V. Radzevich,<sup>55</sup> J. Rak,<sup>30</sup> B. J. Ramson,<sup>41</sup> I. Ravinovich,<sup>63</sup> K. F. Read,<sup>48,59</sup> D. Reynolds,<sup>57</sup> V. Riabov,<sup>44,51</sup> Y. Riabov,<sup>51,55</sup> D. Richford,<sup>5</sup> T. Rinn,<sup>28</sup> S. D. Rolnick,<sup>8</sup> M. Rosati,<sup>28</sup> Z. Rowan,<sup>5</sup> J. G. Rubin,<sup>41</sup> J. Runchey,<sup>28</sup> A. S. Safonov,<sup>55</sup> B. Sahlmueller,<sup>58</sup> N. Saito,<sup>31</sup> T. Sakaguchi,<sup>7</sup> H. Sako,<sup>29</sup> V. Samsonov,<sup>44,51</sup> M. Sarsour,<sup>21</sup> K. Sato,<sup>61</sup> S. Sato,<sup>29</sup> B. Schaefer,<sup>62</sup> B. K. Schmoll,<sup>59</sup> K. Sedgwick,<sup>8</sup> R. Seidl,<sup>52,53</sup> A. Sen,<sup>28,59</sup> R. Seto,<sup>8</sup> P. Sett,<sup>4</sup> A. Sexton,<sup>39</sup> D. Sharma,<sup>58</sup> I. Shein,<sup>24</sup> T.-A. Shibata,<sup>52,60</sup> K. Shigaki,<sup>22</sup> M. Shimomura,<sup>28,43</sup> T. Shioya,<sup>61</sup> P. Shukla,<sup>4</sup> A. Sickles,<sup>7,25</sup> C. L. Silva,<sup>36</sup> D. Silvermyr,<sup>37,48</sup> B. K. Singh,<sup>3</sup> C. P. Singh,<sup>3</sup> V. Singh,<sup>3</sup> M. J. Skoby,<sup>41</sup> M. Slunečka,<sup>9</sup> M. Snowball,<sup>36</sup> R. A. Soltz,<sup>35</sup> W. E. Sondheim,<sup>36</sup> S. P. Sorensen,<sup>59</sup> I. V. Sourikova,<sup>7</sup> P. W. Stankus,<sup>48</sup> M. Stepanov,<sup>40,\*</sup> S. P. Stoll,<sup>7</sup> T. Sugitate,<sup>22</sup> A. Sukhanov,<sup>7</sup> T. Sumita,<sup>52</sup> J. Sun,<sup>58</sup> J. Sziklai,<sup>64</sup> A. Takeda,<sup>43</sup> A. Taketani,<sup>52,53</sup> K. Tanida,<sup>29,53,56</sup> M. J. Tannenbaum,<sup>7</sup> S. Tarafdar,<sup>62,63</sup> A. Taranenko,<sup>44,57</sup> G. Tarnai,<sup>16</sup> R. Tieulent,<sup>21,38</sup> A. Timilsina,<sup>28</sup> T. Todoroki,<sup>52,61</sup> M. Tomášek,<sup>15</sup> C. L. Towell,<sup>1</sup> R. Towell,<sup>1</sup> R. S. Towell,<sup>1</sup> I. Tserruya,<sup>63</sup> Y. Ueda,<sup>22</sup> B. Ujvari,<sup>16</sup> H. W. van Hecke,<sup>36</sup> S. Vazquez-Carson,<sup>13</sup> J. Velkovska,<sup>62</sup> M. Virius,<sup>15</sup> V. Vrba,<sup>15,27</sup> N. Vukman,<sup>66</sup> X. R. Wang,<sup>46,53</sup> Z. Wang,<sup>5</sup> Y. Watanabe,<sup>52,53</sup> Y. S. Watanabe,<sup>12,31</sup> F. Wei,<sup>46</sup> A. S. White,<sup>41</sup> C. P. Wong,<sup>21</sup> C. L. Woody,<sup>7</sup> M. Wysocki,<sup>48</sup> B. Xia,<sup>47</sup> C. Xu,<sup>46</sup> Q. Xu,<sup>62</sup> L. Xue,<sup>21</sup> S. Yalcin,<sup>58</sup> Y. L. Yamaguchi,<sup>12,53,58</sup> H. Yamamoto,<sup>61</sup> A. Yanovich,<sup>24</sup> P. Yin,<sup>13</sup> J. H. Yoo,<sup>32</sup> I. Yoon,<sup>56</sup> H. Yu,<sup>46,50</sup> I. E. Yushmanov,<sup>33</sup> W. A. Zajc,<sup>14</sup> A. Zelenski,<sup>6</sup> S. Zharko,<sup>55</sup> S. Zhou,<sup>11</sup> and L. Zou<sup>8</sup>

(PHENIX Collaboration)

<sup>1</sup>Abilene Christian University, Abilene, Texas 79699, USA

<sup>2</sup>Department of Physics, Augustana University, Sioux Falls, South Dakota 57197, USA

<sup>3</sup>Department of Physics, Banaras Hindu University, Varanasi 221005, India

<sup>4</sup>Bhabha Atomic Research Centre, Bombay 400 085, India

<sup>5</sup>Baruch College, City University of New York, New York, New York 10010, USA

<sup>6</sup>Collider-Accelerator Department, Brookhaven National Laboratory, Upton, New York 11973-5000, USA

<sup>7</sup>Physics Department, Brookhaven National Laboratory, Upton, New York 11973-5000, USA

<sup>8</sup>University of California-Riverside, Riverside, California 92521, USA

<sup>9</sup>Charles University, Ovocný trh 5, Praha 1, 116 36, Prague, Czech Republic

- <sup>10</sup>Chonbuk National University, Jeonju, 561-756, Korea
- <sup>11</sup>Science and Technology on Nuclear Data Laboratory, China Institute of Atomic Energy, Beijing 102413, People's Republic of China
- <sup>12</sup>Center for Nuclear Study, Graduate School of Science, University of Tokyo, 7-3-1 Hongo, Bunkyo, Tokyo 113-0033, Japan
- <sup>13</sup>University of Colorado, Boulder, Colorado 80309, USA
- <sup>14</sup>Columbia University, New York, New York 10027 and Nevis Laboratories, Irvington, New York 10533, USA
- <sup>15</sup>Czech Technical University, Zikova 4, 166 36 Prague 6, Czech Republic
- <sup>16</sup>Debrecen University, H-4010 Debrecen, Egyetem tér 1, Hungary
- <sup>17</sup>ELTE, Eötvös Loránd University, H-1117 Budapest, Pázmány P. s. 1/A, Hungary
- <sup>18</sup>Eszterházy Károly University, Károly Róbert Campus, H-3200 Gyöngyös, Mátrai út 36, Hungary
- <sup>19</sup>Ewha Womans University, Seoul 120-750, Korea
- <sup>20</sup>Florida State University, Tallahassee, Florida 32306, USA
- <sup>21</sup>Georgia State University, Atlanta, Georgia 30303, USA
- <sup>22</sup>Hiroshima University, Kagamiyama, Higashi-Hiroshima 739-8526, Japan
- <sup>23</sup>Department of Physics and Astronomy, Howard University, Washington, DC 20059, USA
- <sup>24</sup>IHEP Protvino, State Research Center of Russian Federation, Institute for High Energy Physics, Protvino, 142281, Russia
- <sup>25</sup>University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, USA
- <sup>26</sup>Institute for Nuclear Research of the Russian Academy of Sciences, prospekt 60-letiya Oktyabrya 7a, Moscow 117312, Russia
- <sup>27</sup>Institute of Physics, Academy of Sciences of the Czech Republic, Na Slovance 2, 182 21 Prague 8, Czech Republic
- <sup>28</sup>Iowa State University, Ames, Iowa 50011, USA
- <sup>29</sup>Advanced Science Research Center, Japan Atomic Energy Agency, 2-4 Shirakata Shirane, Tokai-mura, Naka-gun, Ibaraki-ken 319-1195, Japan
- <sup>30</sup>Helsinki Institute of Physics and University of Jyväskylä, P.O.Box 35, FI-40014 Jyväskylä, Finland
- <sup>31</sup>KEK, High Energy Accelerator Research Organization, Tsukuba, Ibaraki 305-0801, Japan
- <sup>32</sup>Korea University, Seoul, 136-701, Korea
- <sup>33</sup>National Research Center "Kurchatov Institute," Moscow, 123098, Russia
- <sup>34</sup>Kyoto University, Kyoto 606-8502, Japan
- <sup>35</sup>Lawrence Livermore National Laboratory, Livermore, California 94550, USA
- <sup>36</sup>Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA
- <sup>37</sup>Department of Physics, Lund University, Box 118, SE-221 00 Lund, Sweden
- <sup>38</sup>IPNL, CNRS/IN2P3, Univ Lyon, Université Lyon 1, F-69622, Villeurbanne, France
- <sup>39</sup>University of Maryland, College Park, Maryland 20742, USA
- <sup>40</sup>Department of Physics, University of Massachusetts, Amherst, Massachusetts 01003-9337, USA
- <sup>41</sup>Department of Physics, University of Michigan, Ann Arbor, Michigan 48109-1040, USA
- <sup>42</sup>Muhlenberg College, Allentown, Pennsylvania 18104-5586, USA
- <sup>43</sup>Nara Women's University, Kita-uoya Nishi-machi Nara 630-8506, Japan
- <sup>44</sup>National Research Nuclear University, MEPHI, Moscow Engineering Physics Institute, Moscow 115409, Russia
- <sup>45</sup>University of New Mexico, Albuquerque, New Mexico 87131, USA
- <sup>46</sup>New Mexico State University, Las Cruces, New Mexico 88003, USA
- <sup>47</sup>Department of Physics and Astronomy, Ohio University, Athens, Ohio 45701, USA
- <sup>48</sup>Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA
- <sup>49</sup>IPN-Orsay, Univ. Paris-Sud, CNRS/IN2P3, Université Paris-Saclay, BPI, F-91406, Orsay, France
- <sup>50</sup>Peking University, Beijing 100871, People's Republic of China
- <sup>51</sup>PNPI, Petersburg Nuclear Physics Institute, Gatchina, Leningrad region, 188300, Russia
- <sup>52</sup>RIKEN Nishina Center for Accelerator-Based Science, Wako, Saitama 351-0198, Japan
- <sup>53</sup>RIKEN BNL Research Center, Brookhaven National Laboratory, Upton, New York 11973-5000, USA
- <sup>54</sup>Physics Department, Rikkyo University, 3-34-1 Nishi-Ikebukuro, Toshima, Tokyo 171-8501, Japan
- <sup>55</sup>Saint Petersburg State Polytechnic University, St. Petersburg, 195251, Russia
- <sup>56</sup>Department of Physics and Astronomy, Seoul National University, Seoul 151-742, Korea
- <sup>57</sup>Chemistry Department, Stony Brook University, SUNY, Stony Brook, New York 11794-3400, USA
- <sup>58</sup>Department of Physics and Astronomy, Stony Brook University, SUNY, Stony Brook, New York 11794-3800, USA
- <sup>59</sup>University of Tennessee, Knoxville, Tennessee 37996, USA
- <sup>60</sup>Department of Physics, Tokyo Institute of Technology, Oh-okayama, Meguro, Tokyo 152-8551, Japan
- <sup>61</sup>Tomonaga Center for the History of the Universe, University of Tsukuba, Tsukuba, Ibaraki 305, Japan
- <sup>62</sup>Vanderbilt University, Nashville, Tennessee 37235, USA
- <sup>63</sup>Weizmann Institute, Rehovot 76100, Israel
- <sup>64</sup>Institute for Particle and Nuclear Physics, Wigner Research Centre for Physics, Hungarian Academy of Sciences (Wigner RCP, RMKI) H-1525 Budapest 114, POBox 49, Budapest, Hungary
- <sup>65</sup>Yonsei University, IPAP, Seoul 120-749, Korea
- <sup>66</sup>Department of Physics, Faculty of Science, University of Zagreb, Bijenička c. 32 HR-10002 Zagreb, Croatia



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We present measurements of the transverse-momentum dependence of elliptic flow  $v_2$  for identified pions and (anti)protons at midrapidity ( $|\eta| < 0.35$ ), in 0%–5% central  $p + \text{Au}$  and  ${}^3\text{He} + \text{Au}$  collisions at  $\sqrt{s_{NN}} = 200$  GeV. When taken together with previously published measurements in  $d + \text{Au}$  collisions at  $\sqrt{s_{NN}} = 200$  GeV, the results cover a broad range of small-collision-system multiplicities and intrinsic initial geometries. We observe a clear mass-dependent splitting of  $v_2(p_T)$  in  $d + \text{Au}$  and  ${}^3\text{He} + \text{Au}$  collisions, just as in large nucleus-nucleus ( $A + A$ ) collisions, and a smaller splitting in  $p + \text{Au}$  collisions. Both hydrodynamic and transport model calculations successfully describe the data at low  $p_T$  ( $< 1.5$  GeV/ $c$ ), but fail to describe various features at higher  $p_T$ . In all systems, the  $v_2$  values follow an approximate quark-number scaling as a function of the hadron transverse kinetic energy per constituent quark ( $KE_T/n_q$ ), which was also seen previously in  $A + A$  collisions.

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## I. INTRODUCTION

Recent years have seen a paradigm shift in our understanding of the minimum conditions required for the production of the quark-gluon plasma (QGP). In large nucleus-nucleus ( $A + A$ ) collisions, signals of collective behavior—such as the azimuthal momentum anisotropy of final-state particles relative to the event plane—have been successfully understood in the context of nearly inviscid hydrodynamic calculations, thus establishing the notion of a strongly interacting, nearly perfect fluid being formed in this class of collisions [1].

However, the discovery of the same azimuthal anisotropy signals in a variety of small collision systems (i.e.,  $p, d, {}^3\text{He} + \text{Au}$  at  $\sqrt{s_{NN}} = 200$  GeV [2–4];  $p + \text{Pb}$  at  $\sqrt{s_{NN}} = 5.02$  TeV;  $p + p$  at  $\sqrt{s} = 2.76, 5.02$ , and 13 TeV [5–11]; and an earlier observation of long-range two-particle correlations in  $p + p$  collisions at  $\sqrt{s} = 7$  TeV [10]) pose a challenge. It was believed that the system size in this class of collisions is too small to create any significant amount of hot nuclear matter, which in any case would be very short lived. There are also alternative explanations for these anisotropy signals based on momentum space domains and color recombination, such as in [12,13], although they lack quantitative predictions for small-system observables at the BNL Relativistic Heavy Ion Collider (RHIC). Therefore, in small collision systems, the identification of collective behavior with the hydrodynamic expansion of any potential QGP requires further scrutiny.

Measurements of elliptic and triangular flow ( $v_2, v_3$ ) at RHIC in  ${}^3\text{He} + \text{Au}$  collisions, as well as of  $v_2$  in  $d + \text{Au}$  and  $p + \text{Au}$  collisions, demonstrated that the observed collective response in small collision systems is directly correlated with the event geometry [3,4,14], just as in  $A + A$  collisions where the geometric configuration of the overlapping nuclei determines the pressure gradients that drive the expansion of the resulting QGP. Viscous hydrodynamic calculations successfully describe the measurements in the geometry-controlled experiments at RHIC [15–18], as well as those made at the CERN Large Hadron Collider (LHC) in  $p + \text{Pb}$ , and even in  $p + p$  collisions [19]. The success of hydrodynamics in describing small-system collectivity over such a wide range of energies and for a variety of systems is taken as evidence

for the claim that the QGP is formed in these collisions and through its expansion translates initial geometry into final-state momentum anisotropy.

If collectivity in small systems can indeed be understood as arising from the expansion of QGP droplets along pressure gradients determined by geometry, there should necessarily be a mass ordering of  $v_2(p_T)$  for identified final-state hadrons. Strong radial expansion in the hydrodynamic evolution results in a shifting of the anisotropy pattern to higher  $p_T$  for higher mass hadrons due to a common velocity boost [1]. This fingerprint of hydrodynamic expansion on the  $v_2(m, p_T)$  is one of the key signatures of the nearly inviscid fluid nature of the QGP formed in  $A + A$  collisions; see for example [20]. Recently, such mass ordering has been observed in  $d + \text{Au}$  collisions at RHIC [3] and in  $p + \text{Pb}$  collisions at the LHC [21,22].

It is notable that a multiphase transport model (AMPT), an instance of a broader family of kinetic transport models [23], also finds a mass ordering of  $v_2(p_T)$  in both  $A + A$  and small systems, despite having only a modest number of parton scatterings and thus nothing close to a radial velocity field as in hydrodynamics [24]. Within AMPT the mass ordering is found to arise from the hadronic rescattering phase, after all partons have coalesced into hadrons, incorporating the different inelastic cross sections for different hadrons [24]. There are other approaches with fragmentation of saturated gluon states [25] and with color strings followed by hydrodynamics [26] that achieve some degree of mass ordering, though currently lacking in any predictions for small systems at RHIC energies.

The present study completes the set of small-system projectile geometry results at top RHIC energy by providing  $v_2$  measurements for pions and (anti)protons (henceforth referred to as “protons”) in central  $p + \text{Au}$  and  ${}^3\text{He} + \text{Au}$  collisions at  $\sqrt{s_{NN}} = 200$  GeV, and compares to  $v_2$  measurements for pions and (anti)protons in central  $d + \text{Au}$  collisions at the same energy [3]. Detailed comparisons are then made with theory calculations from viscous hydrodynamics, as encoded in the SUPERSONIC [27] and the iEBE-VISHNU models [18], and the kinetic transport model AMPT.

## II. METHODS

The PHENIX collaboration has measured the  $v_2(p_T)$  of identified particles in  $p + \text{Au}$ ,  $d + \text{Au}$ , and  ${}^3\text{He} + \text{Au}$  collisions. We apply the same analysis procedure to all three

\*Deceased.

†PHENIX spokesperson: akiba@rcf.thic.bnl.gov

systems in the same centrality class to provide a controlled comparison from which to draw conclusions.

A complete description of the PHENIX detector and its subsystems can be found in [28,29]. Charged particles are reconstructed with the two central arm spectrometers, comprising drift chambers (DCs) and multiwire proportional pad chambers (PCs). Each arm covers an acceptance of  $|\eta| < 0.35$  in pseudorapidity and  $\pi/2$  in azimuth. Tracks in the drift chamber are matched to hits in the outer detectors. The distribution of differences between hits and projections is approximately Gaussian, with an additional underlying background caused by random associations. To suppress background from particle weak decays and photon conversions, tracks reconstructed with the DCs and the first layer of PCs are required to be matched to the third layer of PCs within three  $\sigma$  in the longitudinal and transverse planes, where  $p_T$  and charge sign dependent  $\sigma$  values are determined from Gaussian fits to residual distributions between PC clusters and the tracks extrapolated to the PC surface. Particle identification is performed using the time-of-flight (TOF) subsystem, which comprises two separate arms (east and west), constructed using scintillators [30] and multigap resistive plate chambers [31], and covers  $\pi/4$  and  $\pi/8$ , respectively. The timing resolutions for the east and west TOF are 130 ps and 95 ps, respectively. Particle identification (PID) is based on the particle mass with  $p_T$ -dependent selections in mass-squared calculated using the particle momentum, time of flight, and path length. After track matching and PID selections, some residual background remains in the proton sample at low  $p_T$  ( $< 1$  GeV/ $c$ ). In this  $p_T$  range, up to 15% of the reconstructed protons are secondary particles that originate from interactions of energetic particles produced in the collisions with detector material, primarily the silicon vertex tracker (VTX), which covers the pseudorapidity range  $|\eta| < 1.2$ . Detector simulations using GEANT3 [32] indicate that the contamination in the proton sample is negligible for  $p_T > 1$  GeV/ $c$ , not present in the antiproton distributions, and negligible in the charged-pion sample at all  $p_T$ . To remove the background in the proton sample, the VTX detector [33] is used in conjunction with the DC to select proton tracks with  $p_T < 1$  GeV/ $c$  based on their distance of closest approach (DCA) to the primary vertex in the  $x$ - $y$  plane transverse to the beam direction. The tracks are required to be within two standard deviations of the mean value of the DCA distribution. This additional selection is not applied at higher  $p_T$  nor for particle species for which the secondary-particle contamination is negligible. The pions and protons selected for the analysis are identified with purity of over 98% for  $p_T$  up to 3 GeV/ $c$  in all collision systems.

The beam-beam counters (BBCs) comprise two arrays of 64 quartz radiator Čerenkov detectors, placed longitudinally  $\pm 1.44$  m away from the center of the interaction region (IR), covering  $3.0 < |\eta| < 3.9$  and  $2\pi$  in azimuth. The forward vertex detector (FVTX) is a silicon detector comprised of two identical end-cap assemblies symmetrically arranged in the longitudinal direction around the IR, covering the pseudorapidity acceptance  $1.0 < |\eta| < 3.0$ . Using hit clusters, it can detect charged particles with an efficiency greater than 95%. The arms of the BBC and FVTX in the Au-going direction (i.e.,  $\eta < 0$ ) are designated as the *south* arms and designated BBC-S

and FVTX-S, respectively. We use the south arm of each of these detectors to determine the event plane of the collision. In addition, timing information from the BBC is used to determine the  $z$  vertex of the collision. In this analysis, a  $\pm 10$  cm cut on the collision  $z$  vertex is applied.

The  $p + \text{Au}$  data set for this analysis, taken during the 2015 run at RHIC, comprises  $0.84 \times 10^9$  minimum-bias (MB) triggered events and  $1.4 \times 10^9$  high-multiplicity (HM) triggered events. The MB trigger is defined as a coincidence in the same event between both arms of the BBC detector [34], requiring that at least one photomultiplier tube (PMT) fire in each. This definition allows  $84 \pm 4\%$  of the total inelastic  $p + \text{Au}$  cross section to be captured. The HM trigger is based on the MB trigger, but with the additional requirement of more than 35 photomultiplier tubes firing in the BBC-S. Events that satisfy this trigger condition correspond roughly to the 5% most central event class. The use of this high-multiplicity trigger allows us to increase our central  $p + \text{Au}$  event sample size by a factor of 25. The  $^3\text{He} + \text{Au}$  data set for this analysis were recorded during the 2014 run at RHIC, and comprises  $1.6 \times 10^9$  MB events and  $480 \times 10^6$  HM events. The HM trigger used in  $^3\text{He} + \text{Au}$  is also based on the MB trigger, but with the additional requirement of more than 48 photomultiplier tubes firing in the BBC-S. The  $d + \text{Au}$  data set was recorded during the 2008 run, and comprises  $1.56 \times 10^9$  MB events.

In this analysis, we select the 0%–5% most central events in all collision systems, where centrality classes are defined as percentiles of the total charged-particle multiplicity as measured in the BBC-S, following the procedure presented in [35]. We follow the identical analysis procedure that was previously used in  $^3\text{He} + \text{Au}$  and  $p + \text{Au}$  collisions [4,14] to measure  $v_2$  for inclusive charged hadrons. Namely, we measure  $v_2$  for final-state single hadrons at midrapidity with respect to the event plane [36] of the collision, as follows:

$$v_2(p_T) = \frac{\langle \cos 2[\phi_{\text{Particle}}(p_T) - \Psi_2^{\text{FVTX-S}}] \rangle}{\text{Res}(\Psi_2^{\text{FVTX-S}})}. \quad (1)$$

The event-plane angle is determined by the event flow vector  $Q_2$  measured in the Au-going direction where the particle multiplicity is higher. The  $Q$  vectors are recentered according to the standard procedure described in [36]. The raw event-plane angle is estimated by

$$\Psi_n^{\text{raw}} = \text{atan2}(Q_2^y, Q_2^x)/2, \quad (2)$$

where  $Q_2^x$  and  $Q_2^y$  are the  $x$  and  $y$  projections of the flow vector. A standard flattening procedure described in [36] is applied to the  $\Psi_2^{\text{raw}}$  distributions to remove detector acceptance effects. The second-order event-plane angle  $\Psi_2^{\text{FVTX-S}}$  is determined using the FVTX-S detector. Its resolution  $\text{Res}(\Psi_2)$  is evaluated using the standard three-subevent method [36], correlating independent measurements made in the BBC-S, FVTX-S, and the central arms. The resolution of the event plane is found to be  $\text{Res}(\Psi_2^{\text{FVTX-S}, p + \text{Au}}) = 0.171$  in  $p + \text{Au}$  collisions, and  $\text{Res}(\Psi_2^{\text{FVTX-S}, ^3\text{He} + \text{Au}}) = 0.274$  in  $^3\text{He} + \text{Au}$  collisions. If the event plane is instead measured using the BBC-S detector, we obtain a lower resolution  $\text{Res}(\Psi_2^{\text{BBC-S}, p + \text{Au}}) = 0.062$  in  $p + \text{Au}$  and  $\text{Res}(\Psi_2^{\text{BBC-S}, ^3\text{He} + \text{Au}}) = 0.070$  in  $^3\text{He} + \text{Au}$  collisions.

The event-plane resolution depends on the particle multiplicity registered in the detectors used for event-plane determination, which results in better resolution in the FVTX-S than in the BBC-S.

### III. SYSTEMATIC UNCERTAINTIES

We identify the following as the main sources of systematic uncertainty in the  $v_2(p_T)$  measurement:

*Background tracks from weak decays, photon conversions, and misreconstructed tracks.* We estimate the magnitude of this uncertainty by narrowing the spatial matching windows of the tracks and the hits in the outermost layer of the PC, from  $3\sigma$  to  $2\sigma$  and comparing the resulting values of  $v_2(p_T)$ . The relative uncertainty in  $v_2$  is 2% in both  $p + \text{Au}$  and  ${}^3\text{He} + \text{Au}$  collisions.

*Multiple collisions per bunch crossing.* Also referred to as event pile-up, these are observed to occur at an average rate of 8% (4%–5%) in the centrality class of interest in  $p + \text{Au}$  ( ${}^3\text{He} + \text{Au}$ ) collisions. We estimate the associated systematic uncertainty by analyzing low- and high-luminosity subsets of the data. The measured  $v_2$  was found to decrease in events with higher pile-up rates, and an asymmetric systematic uncertainty of  ${}^{+4}_{-0}\%$  was assigned in  $p + \text{Au}$ , and  ${}^{+5}_{-0}\%$  was assigned in  ${}^3\text{He} + \text{Au}$  collisions.

*Nonflow correlations from elementary processes.* There are many sources of correlations among particles which enhance the measured  $v_2$ , yet are unrelated to collective flow, such as momentum conservation. We use a reference method previously employed in PHENIX analyses of small-system collectivity [14] to assign a  $p_T$ -dependent asymmetric uncertainty with a maximum value of  ${}^{+0}_{-23}\%$  for the highest  $p_T$  bin in  $p + \text{Au}$  collisions. This can be compared to the corresponding values of  ${}^{+0}_{-9}\%$  [3] and  ${}^{+0}_{-7}\%$  [4] in  $d + \text{Au}$  and  ${}^3\text{He} + \text{Au}$  collisions, respectively. The nonflow effect has a larger relative contribution in  $p + \text{Au}$  collisions due to the smaller multiplicity in this system.

*Detector acceptance asymmetry.* In  $p + \text{Au}$  collisions, there exists an asymmetry between the east ( $\pi/2 < \phi < 3\pi/2$ ) and west ( $-\pi/2 < \phi < \pi/2$ ) acceptance of the detectors, originating from a 3.6 mrad offset between the beams at the collision point and the longitudinal axis of PHENIX. This offset is necessary to compare to  $p + \text{Au}$  collisions at the same momentum per nucleon. We account for this effect by performing a counter-rotation on every central arm track and detector element in the FVTX and the BBC, taking care to restore their azimuthal anisotropy by re-weighting. There remains a small residual asymmetry after applying these corrections in  $p + \text{Au}$ . Meanwhile in  ${}^3\text{He} + \text{Au}$  collisions this beam angle is negligible and we assign a value of 5% for this systematic uncertainty by taking the difference of  $v_2$  when measured exclusively in the east or west arms in both  $p + \text{Au}$  and  ${}^3\text{He} + \text{Au}$  collisions.

*Event plane measured with different detectors.* We observe the measured  $v_2(p_T)$  to differ when using the event plane as determined using the BBC-S or the FVTX-S detectors. Despite the large difference in event-plane resolution in these two detectors, the differences in the measured  $v_2(p_T)$  values are only of the order 3% in  $p + \text{Au}$ , and 5% in  ${}^3\text{He} + \text{Au}$

TABLE I. Systematic uncertainties given as a percent of the  $v_2$  measurement. Note that the nonflow contribution is  $p_T$  dependent and the quoted values correspond to the highest measured  $p_T$ .

Source	$p + \text{Au}$	${}^3\text{He} + \text{Au}$	Type
Track background	2%	2%	A
Event pile-up	${}^{+4}_{-0}\%$	${}^{+5}_{-0}\%$	B
Nonflow	${}^{+0}_{-23}\%$	${}^{+0}_{-7}\%$	B
Acceptance asymmetry	5%	5%	C
Event-plane detectors	3%	5%	C
Particle purity	2%	2%	B

collisions, which demonstrates that the corrections for event-plane resolution are well understood.

*Particle identification purity.* The effect of particle identification purity on the measured  $v_2$  values is evaluated by varying the width of particle selection windows in the mass-squared vs  $p_T$  space from  $2\sigma$  to  $1.5\sigma$ . The uncertainty is found to be at most 2% for both pions and protons in both collision systems.

Table I summarizes all these systematic uncertainties, categorized by type: A, point-to-point uncorrelated between  $p_T$  bins; B, point-to-point correlated between  $p_T$  bins; and C, overall normalization uncertainty in which all data points are scaled by the same multiplicative factor.

### IV. RESULTS AND DISCUSSION

Figure 1 shows  $v_2(p_T)$  for identified pions and protons in 0%–5% central  $p + \text{Au}$ ,  $d + \text{Au}$  [3], and  ${}^3\text{He} + \text{Au}$  collisions. For both pions and protons the  $v_2(p_T)$  values are higher in  $d + \text{Au}$  and  ${}^3\text{He} + \text{Au}$  collisions than in  $p + \text{Au}$  collisions, as previously observed for inclusive charged hadrons [14]. These values follow the ordering of the initial geometric eccentricity  $\varepsilon_2(p + \text{Au}) < \varepsilon_2({}^3\text{He} + \text{Au}) \approx \varepsilon_2(d + \text{Au})$ .

In the  $d + \text{Au}$  and  ${}^3\text{He} + \text{Au}$  systems, there is a clear separation between the pion and proton  $v_2$ , with the pion  $v_2$  being larger than the proton  $v_2$  for  $p_T \lesssim 1.5 \text{ GeV}/c$  and this order being reversed at higher  $p_T$ . In the  $p + \text{Au}$  system, the pion and proton  $v_2(p_T)$  values show smaller overall splitting. The splitting pattern and the reversal of the mass ordering above  $p_T \gtrsim 1.5 \text{ GeV}/c$  is qualitatively the same as has been observed in  $\text{Au} + \text{Au}$  collisions at  $\sqrt{s_{NN}} = 200 \text{ GeV}$  [20,37].

Figure 1 compares the measured  $v_2(p_T)$  with hydrodynamic calculations using the SUPERSONIC model [38]. This model comprises standard Monte Carlo Glauber initial conditions followed by a viscous hydrodynamic expansion stage with  $\eta/s = 0.08$ , Cooper-Frye hadronization at  $T = 170 \text{ MeV}$ , and a subsequent hadronic cascade code, B3D [39]. The SUPERSONIC model additionally incorporates pre-equilibrium dynamics via a calculation in the context of the anti-de Sitter-space/conformal-field-theory (AdS/CFT) correspondence [40–42]. These hydrodynamic calculations are matched to the measured charged-particle density at midrapidity in the 0%–5% centrality class for  $d + \text{Au}$  and  ${}^3\text{He} + \text{Au}$  (i.e.,  $dN_{\text{ch}}/d\eta = 20.0$  and  $27.0$ , respectively [43]). Because  $dN_{\text{ch}}/d\eta$  has not yet been measured in  $p + \text{Au}$  collisions, a value of  $dN_{\text{ch}}/d\eta = 10.0$  was extrapolated for this system [38].

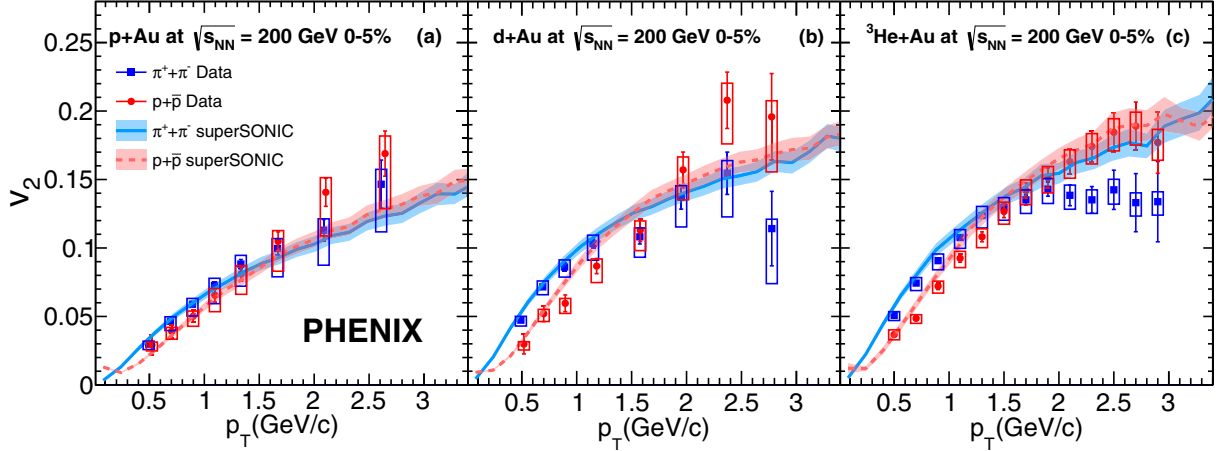


FIG. 1. Transverse momentum dependence of  $v_2$  for identified pions and protons within  $|\eta| < 0.35$  in 0%–5% central  $p + Au$ ,  $d + Au$  [3], and  ${}^3\text{He} + Au$  collisions. The measurements are compared to hydrodynamic calculations using the SUPERSONIC model [38], matched to the same multiplicity at midrapidity as the data. Note that the data points shown include nonflow contributions, whose estimated magnitude is accounted for in the asymmetric systematic uncertainties.

We observe that the hydrodynamic calculations agree with the data within uncertainties at low  $p_T$ , but fail to describe the reversal of the pion and proton  $v_2$  ordering for  $p_T > 1.5$  GeV/ $c$ . Viscous hydrodynamic calculations similarly describe Au + Au  $v_2$  data at low  $p_T$  but do not match the strong reverse ordering at higher  $p_T$ . For  $p_T < 1.5$  GeV/ $c$ , the mass splitting increases in going from  $p + Au$  to  $d + Au$  and  ${}^3\text{He} + Au$  as also seen in the data. Within the context of hydrodynamic calculations, this is due to the increased radial flow and consequently larger velocity boost when going from the smaller and lower multiplicity systems to the larger and higher multiplicity systems.

In the case of ideal hydrodynamics, i.e., with zero viscosity, the  $v_2$  values for all hadrons asymptotically approach each other at high  $p_T$  [44]. However, viscous effects and the incorporation of late-stage hadronic rescattering have the effect of lowering the high  $p_T$   $v_2$  values, more strongly so for pions. This can be seen in the SUPERSONIC calculations. However, the

predicted high  $p_T$  splitting is much smaller than that seen in the  $d + Au$  and  ${}^3\text{He} + Au$  data. It is in this high  $p_T$  region in  $A + A$  collisions that proposals of hadronization via recombination [45] have been set forth to explain the  $v_2$  splitting as well as the observation of enhanced baryon yields [46,47].

Figure 2 shows results from another viscous hydrodynamic calculation, iEBE-VISHNU [18]. The calculation includes event-by-event fluctuating initial conditions via Monte Carlo Glauber simulation and then viscous hydrodynamics starting at  $\tau_0 = 0.6$  fm/ $c$ . The hydrodynamic evolution utilizes an  $\eta/s = 0.08$  for RHIC energies and ends at  $T = 155$  MeV. After that point, hadronization occurs and hadronic rescattering is implemented using URQMD 3.4 [48,49]. The calculation results with viscous hydrodynamics followed by hadronic rescattering show good agreement with the experimental data for all three small systems. Also shown are results with no hadronic rescattering that reveal almost no change in the  $v_2$  for pions and protons for  $p_T < 1.5$  GeV/ $c$ . The authors [18] conclude that hadronic

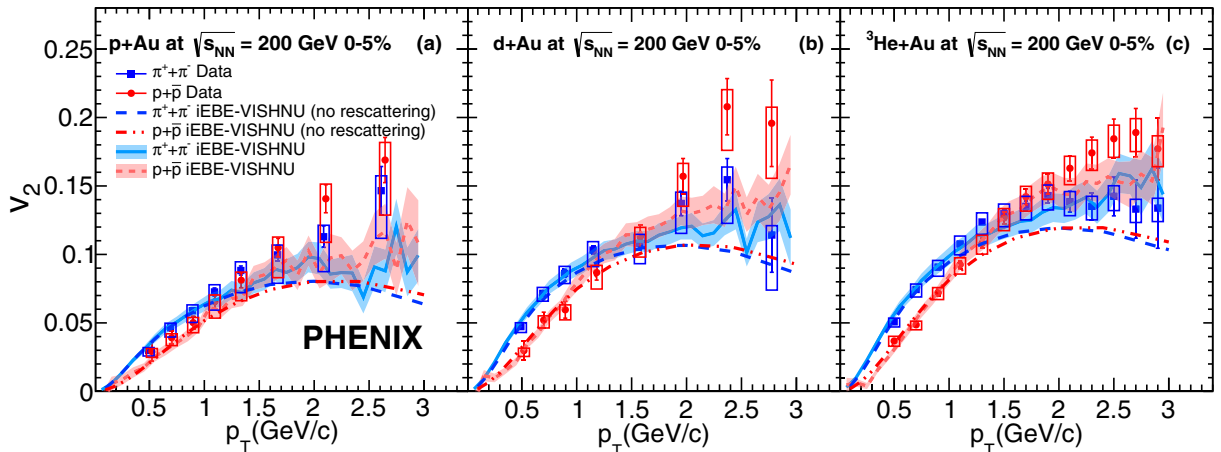


FIG. 2. Same as Fig. 1, but also shown are  $v_2(p_T)$  calculations using the iEBE-VISHNU hydrodynamic model [18], illustrating the effect of hadronic rescattering on the mass-dependent  $v_2$  values.

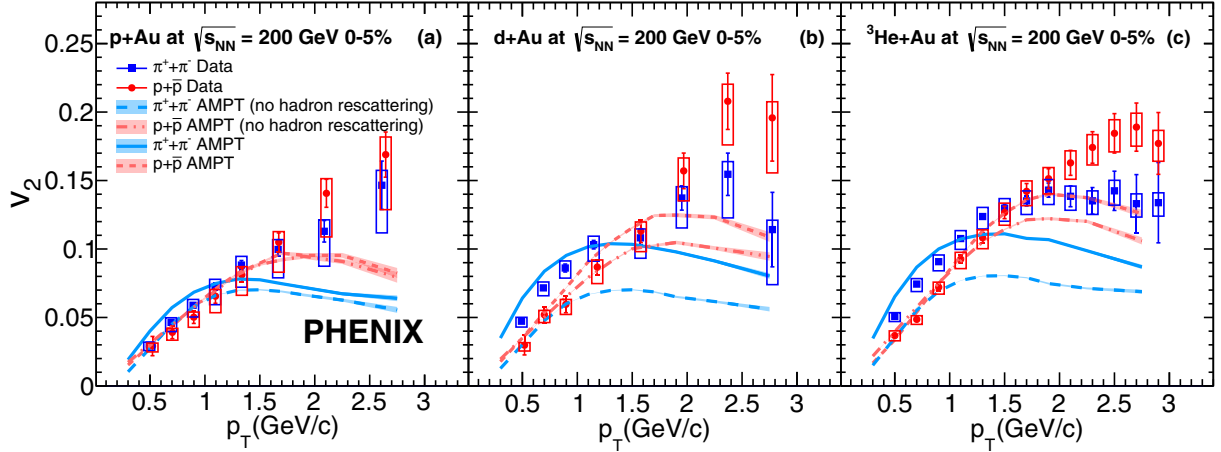


FIG. 3. Same as Fig. 1, but also shown are  $v_2(p_T)$  transport model calculations using AMPT [23].

rescattering plays a modest but important role in the system development and particle species dependence of  $v_2$  in these small systems.

Figure 3 compares the experimental data to transport model calculations of  $v_2(p_T)$  for each system using AMPT [23]. The AMPT model has been successful in describing various features of small-system collectivity at RHIC and the LHC, over a wide range of collision energies [50–54]. It uses Monte Carlo Glauber initial conditions, and it models the evolution of the system via strings that melt into partons, followed by a succession of partonic scattering, spatial coalescence, and late-stage hadronic scattering implemented in ART [55]. We show results from the full AMPT time evolution with a partonic cross section  $\sigma_{\text{part}} = 1.5$  mb, as well as results with the hadronic rescattering turned off. We calculate  $v_2$  in central (i.e.,  $b < 2$  fm) AMPT events, relative to the parton participant plane. That is, the event plane is calculated using the initial coordinates of the partons, as they emerge from string melting at early times. We observe that the full AMPT describes the mass-dependent splitting in  $d + \text{Au}$  and  $^3\text{He} + \text{Au}$  for  $p_T < 1.5$  GeV/c. In  $p + \text{Au}$  collisions, the model results in a smaller mass splitting, which is reversed at high  $p_T$  yet below the experimental

data. As noted in [24], AMPT generates significant  $v_2$ , and in particular mass splitting, in the hadronic rescattering stage. As also shown in Fig. 3, the results without rescattering have significantly lower  $v_2$  values and almost no mass splitting for  $p_T < 1$  GeV/c. At higher  $p_T$ , the feature of  $v_2$  for protons being greater than pions remains without hadronic rescattering and is associated with the spatial coalescence implementation for hadronization.

Figure 4 shows the ratio of pion to proton  $v_2(p_T)$  in all collision systems, with the corresponding theory curves overlaid. In the ratio, many systematic uncertainties cancel and thus one sees more precisely that the data exhibit a similar trend in all collision systems where pion  $v_2$  is larger than proton  $v_2$  for  $p_T < 1.5$  GeV/c, with the order reversed at higher  $p_T$ . Linear fits on these ratios ranged from 0.5 to 3.0 GeV/c, which include both the statistical and the systematic uncertainties, yield slope values of  $-0.22 \pm 0.07$  in  $p + \text{Au}$  collisions,  $-0.40 \pm 0.07$  in  $d + \text{Au}$  collisions, and  $-0.34 \pm 0.03$  in  $^3\text{He} + \text{Au}$  collisions. In this ratio, one can clearly see that SUPERSONIC, iEBE-VISHNU, and full AMPT modeling describe the mass splitting in  $d + \text{Au}$  and  $^3\text{He} + \text{Au}$  for  $p_T < 1.5$  GeV/c. In the  $p + \text{Au}$  case, it appears that the

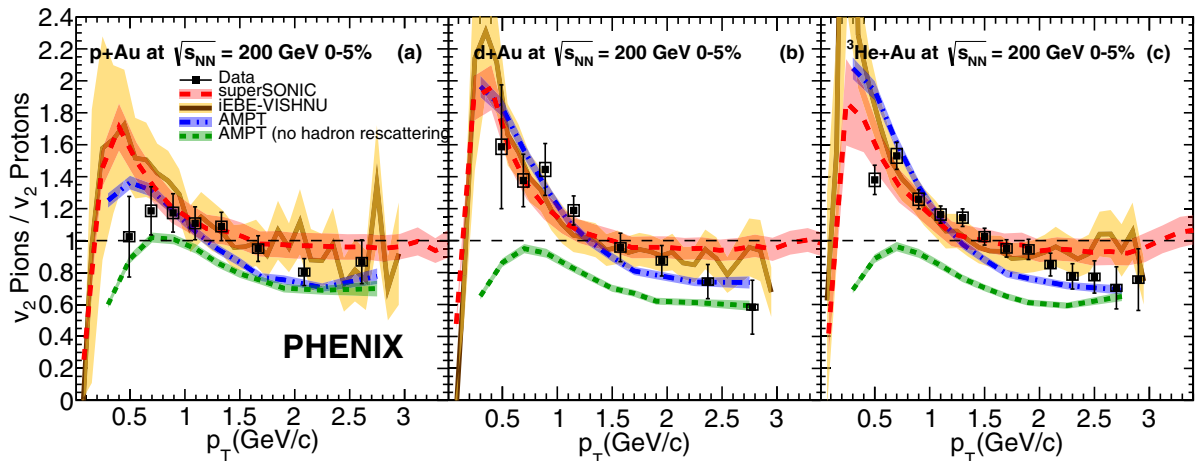


FIG. 4. Ratio of  $v_2^{\text{pion}}$  over  $v_2^{\text{proton}}$  in central 0%–5% (a)  $p + \text{Au}$ , (b)  $d + \text{Au}$ , and (c)  $^3\text{He} + \text{Au}$  collisions at  $\sqrt{s_{NN}} = 200$  GeV. Theoretical calculations from SUPERSONIC and AMPT are also shown.



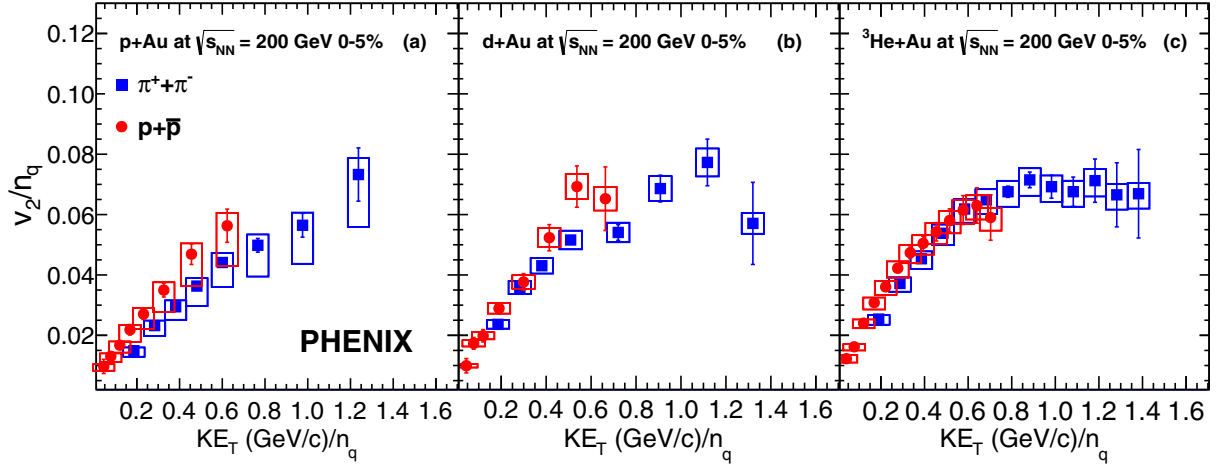


FIG. 5. Scaling of  $v_2(p_T)$  with the number of constituent quarks in each hadron species, in 0%–5% central (a)  $p + Au$ , (b)  $d + Au$ , and (c)  ${}^3\text{He} + Au$  collisions at  $\sqrt{s_{NN}} = 200$  GeV.

calculations over predict the more modest splitting at the lowest measured  $p_T = 0.5$  GeV/ $c$ . The results from AMPT without hadronic rescattering have very little mass splitting at low  $p_T$  in disagreement with the experimental data, particularly for  $d + Au$  and  ${}^3\text{He} + Au$  collisions. Above the crossing point, SUPERSONIC, and iEBE-VISHNU predict nearly flat ratios, while AMPT describes the ratio of the  $v_2$  values, but not their individual magnitudes. These differences may be attributed to the different hadronization mechanisms (e.g., if recombination is included) in the models.

The observation of a mass-dependent  $v_2$  strengthens the case for associating small-system collectivity with the expansion of QGP droplets formed in these collisions, where the splitting can be understood in terms of the presence of a common radial flow field with anisotropic modulations driven by initial geometry. However, the theoretical calculations presented in this paper provide several alternative explanations of how the azimuthal anisotropies for different particle species may occur. For instance, in kinetic transport, parton scattering translates initial geometry into final-state momentum anisotropy, but it does not account for the observed mass splitting. Instead, this feature has been shown to arise solely from the hadronic rescattering stage where different hadrons have different inelastic cross sections [24]. There is more hadronic rescattering in  ${}^3\text{He} + Au$  and  $d + Au$  than in  $p + Au$  for these central collisions because they have a higher particle density. It is interesting that this conclusion based on AMPT regarding the contribution of the hadronic rescattering stage is opposite to that reached using viscous hydrodynamics [18]. Differences in the hadronic scattering packages B3D [39] used in SUPERSONIC, URQMD [49] used in iEBE-VISHNU, and ART [23] used in AMPT warrant further investigation.

Finally, we return to the high  $p_T$  region where neither viscous hydrodynamics nor parton transport calculations match the data. Figure 5 shows the scaling of  $v_2$  with constituent quarks as a function of transverse kinetic energy per quark  $KE_T/n_q = (\sqrt{p_T^2 + m^2} - m)/n_q$ , where  $m$  is the mass of the hadron and  $n_q$  represents the number of constituent quarks in the hadron. In all three systems, the  $v_2/n_q$  for pions and protons

as a function of  $KE_T/n_q$  follow an approximate quark-number scaling. The same scaling was previously observed in  $A + A$  collisions [20,37,56,57]. At intermediate  $p_T$  (1.5–4 GeV/ $c$ ), the enhancement of baryons over mesons and the reversed mass ordering of  $v_2$  in  $A + A$  collisions have been interpreted in terms of hadronization via recombination. At even higher  $p_T$ , the scaling breaks down in noncentral  $A + A$  collisions [58]. Similar to the observations in  $A + A$ , the enhancement of baryon over meson yields at intermediate  $p_T$  has been observed in central  $d + Au$  collisions [31], and now we also see the scaling with  $n_q$  in all three small collision systems. The scaling works better in  $d + Au$  and  ${}^3\text{He} + Au$  collisions, where the projectile sizes and the particle densities are higher.

## V. SUMMARY

We have presented results on the transverse momentum dependence of elliptic flow  $v_2$  of identified pions and (anti)protons in central 0%–5%  $p + Au$ ,  $d + Au$ , and  ${}^3\text{He} + Au$  at  $\sqrt{s_{NN}} = 200$  GeV. The  $d + Au$  and  ${}^3\text{He} + Au$  data show a clear mass splitting with  $v_2$  for pions larger than  $v_2$  of protons for  $p_T < 1.5$  GeV/ $c$ , and then a reversal of the ordering at higher  $p_T$ . The mass dependence is smaller in  $p + Au$  collisions than in  $d + Au$  and  ${}^3\text{He} + Au$  collisions. Theoretical calculations, from viscous hydrodynamics and parton transport, yield a reasonable description of the low  $p_T$  mass splitting, despite having quite different mechanisms responsible for the observed mass dependence. At higher  $p_T$ , both models fail to describe the data, missing either the absolute value or the observed mass dependence. A scaling of  $v_2$  with the number of constituent quarks, motivated by recombination, is observed in the data and is found to hold better in  $d + Au$  and  ${}^3\text{He} + Au$  collisions, where the particle multiplicities are larger. All of these observations are qualitatively similar to previously measured effects in  $A + A$  collisions. This again puts into sharp focus the question of whether the observations can be understood as arising from the same underlying physics, e.g., inviscid fluid expansion, in both large and small collision systems. While alternative physics mechanisms have been

proposed, detailed comparisons with the experimental results are not yet available. This paper provides important constraints on the mass dependence of the particle correlations in small collision systems.

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### APPENDIX: DATA TABLES

Tables II and III show the values of  $v_2(p_T)$  for pions, kaons, and protons in central 0%–5%  $p + Au$  and  ${}^3\text{He} + Au$  collisions at  $\sqrt{s_{NN}} = 200$  GeV.

TABLE III. Values of  $v_2(p_T)$  for pions, kaons, and protons in central 0%–5%  ${}^3\text{He} + Au$  collisions at  $\sqrt{s_{NN}} = 200$  GeV.

TABLE II. Values of  $v_2(p_T)$  for pions, kaons, and protons in central 0%–5%  $p + Au$  collisions at  $\sqrt{s_{NN}} = 200$  GeV.

	$p_T$ range (GeV/ $c$ )	$v_2$	$\pm$ stat	+ syst	– syst
$\pi^+ + \pi^-$	0.40–0.60	0.030	0.001	0.002	0.004
	0.60–0.80	0.046	0.002	0.003	0.007
	0.80–1.00	0.059	0.002	0.004	0.009
	1.00–1.20	0.073	0.003	0.005	0.013
	1.20–1.50	0.088	0.003	0.006	0.016
	1.50–1.90	0.100	0.005	0.007	0.021
	1.90–2.40	0.113	0.008	0.008	0.025
	2.40–3.00	0.147	0.018	0.011	0.035
$K^+ + K^-$	0.40–0.60	0.022	0.006	0.002	0.003
	0.60–0.80	0.037	0.005	0.003	0.005
	0.80–1.00	0.056	0.006	0.004	0.008
	1.00–1.20	0.068	0.007	0.005	0.012
	1.20–1.50	0.079	0.007	0.006	0.015
	1.50–1.90	0.091	0.009	0.007	0.019
$p + \bar{p}$	0.40–0.60	0.029	0.007	0.002	0.004
	0.60–0.80	0.039	0.005	0.003	0.006
	0.80–1.00	0.050	0.005	0.004	0.007
	1.00–1.20	0.066	0.005	0.005	0.012
	1.20–1.50	0.081	0.005	0.006	0.015
	1.50–1.90	0.105	0.007	0.008	0.022
	1.90–2.40	0.141	0.010	0.011	0.032
2.40–3.00	0.169	0.016	0.013	0.040	

	$p_T$ range (GeV/ $c$ )	$v_2$	$\pm$ stat	+ syst	– syst
$\pi^+ + \pi^-$	0.40–0.60	0.051	0.001	0.003	0.004
	0.60–0.80	0.074	0.001	0.004	0.005
	0.80–1.00	0.091	0.001	0.005	0.007
	1.00–1.20	0.108	0.002	0.006	0.008
	1.20–1.40	0.124	0.002	0.007	0.009
	1.40–1.60	0.130	0.003	0.007	0.010
	1.60–1.80	0.135	0.004	0.007	0.010
	1.80–2.00	0.143	0.005	0.008	0.011
	2.00–2.20	0.138	0.008	0.007	0.010
	2.20–2.40	0.135	0.010	0.007	0.010
	2.40–2.60	0.142	0.014	0.008	0.010
	2.60–2.80	0.133	0.021	0.007	0.010
	2.80–3.00	0.134	0.029	0.007	0.010
	$K^+ + K^-$	0.40–0.60	0.041	0.003	0.002
0.60–0.80		0.054	0.003	0.003	0.004
0.80–1.00		0.077	0.003	0.004	0.006
1.00–1.20		0.093	0.004	0.005	0.007
1.20–1.40		0.109	0.005	0.006	0.008
1.40–1.60		0.115	0.006	0.006	0.008
1.60–1.80		0.123	0.007	0.007	0.009
1.80–2.00		0.142	0.009	0.008	0.010
$p + \bar{p}$	0.40–0.60	0.037	0.002	0.003	0.004
	0.60–0.80	0.049	0.002	0.003	0.004
	0.80–1.00	0.072	0.002	0.004	0.005
	1.00–1.20	0.093	0.003	0.005	0.007
	1.20–1.40	0.108	0.004	0.006	0.008
	1.40–1.60	0.127	0.005	0.007	0.009
	1.60–1.80	0.142	0.006	0.008	0.010
	1.80–2.00	0.151	0.007	0.008	0.011
	2.00–2.20	0.163	0.009	0.009	0.012
	2.20–2.40	0.174	0.012	0.009	0.013
	2.40–2.60	0.184	0.014	0.010	0.014
2.60–2.80	0.189	0.018	0.010	0.014	
2.80–3.00	0.177	0.023	0.010	0.013	

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