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Optical conductivity of the type-II Weyl semimetal TaIrTe$_4$

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TaIrTe$_4$ is an example of a candidate Weyl type-II semimetal with a minimal possible number of Weyl nodes. Four nodes are reported to exist in a single plane in $k$ space. The existence of a conical dispersion linked to Weyl nodes has yet to be shown experimentally. Here, we use optical spectroscopy as a probe of the band structure on a low-energy scale. Studying optical conductivity allows us to probe intraband and interband transitions with zero momentum. In TaIrTe$_4$, we observe a narrow Drude contribution and an interband conductivity that may be consistent with a tilted linear band dispersion up to 40 meV. The interband conductivity allows us to establish the effective parameters of the conical dispersion; effective velocity $v = 1.1 \times 10^5$ m/s and tilt $\gamma = 0.37$. The transport data, Seebeck and Hall coefficients, are qualitatively consistent with conical features in the band structure. Quantitative disagreement may be linked to the multiband nature of TaIrTe$_4$.

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Weyl semimetals are currently intensely studied both by theoretical and experimental methods. Their effective description at low energies is given by the Weyl equation, which is a variant of the Dirac equation for particles with zero rest mass. This effective description results in special properties of the wave functions, leading to the appearance of pairs of Berry monopoles. The effective Weyl description also leads to a linear dispersion of energy, usually constrained to a low-energy range.

The first realization of Weyl nodes in a solid came in the TaAs family. However, the band structure in that family is far from simple, and the number of nodes is very high: 24. In the past few years, efforts have been made to pinpoint a simpler realization of Weyl semimetals. Theoretically, the minimal allowed number of Weyl nodes is four, for Weyl semimetals with broken inversion symmetry. These Weyl nodes are all located on a single plane in $k$ space. Arguably, TaIrTe$_4$ is an example of the theoretically predicted minimal Weyl semimetal, possessing only four Weyl nodes [1,2]. While ab initio calculations predicted the existence of Weyl nodes in TaIrTe$_4$, surface techniques reported signatures of Fermi arcs [3], despite the challenge of Weyl cones residing above the Fermi level. A number of exotic properties have been claimed to arise in TaIrTe$_4$, among them being topological edge states [4], unconventional surface superconductivity [5], bulk superconductivity under pressure [6], large Fermi arcs reaching 1/3 of the Brillouin zone dimension [3], stretchable Weyl points and line nodes [2], and a circular photogalvanic effect linked to the Berry curvature [7].

Unfortunately, many of these results hinge on the ab initio calculations, which become fairly unreliable at low energies on a scale of tens of milli-electron volts. One cannot trust the density functional theory (DFT) calculations to tell correctly what is the energy scale of the linear dispersion, which would be linked to the Weyl cones. Experimentally, it is difficult to expose those experimental features which are directly linked to the Weyl dispersion, particularly in the bulk properties of the candidate material. There are still only few explicit confirmations of the conical features in three-dimensional (3D) materials such as TaIrTe$_4$. This is why, for TaIrTe$_4$, a number of questions remain unclear: Can one detect the conical dispersion and what is its scale? Where is it located with respect to the Fermi level? How much are these energy-band cones tilted?

In this paper we determine the optical conductivity of TaIrTe$_4$. We focus in particular on its low-energy range, in order to identify the possible signatures of tilted Weyl dispersion, expected to be characteristic of this material. While one inherently cannot say anything about the Weyl character of the bands from probing the simple optical response, one can reach conclusions about the energy dispersion and its possible linearity. Weyl cones in TaIrTe$_4$ are of type II, meaning that they are predicted to have a certain tilt. This tilt drastically changes properties, for example, it removes the electron-hole symmetry. As a result, the optical response of a tilted cone will be different than that of a nontilted cone. The tilted conical dispersion may be simply described by a $2 \times 2$ Hamiltonian matrix. From such a model, one can analytically derive various physical quantities. Specifically, here we derive the Seebeck coefficient or thermoelectric power, Hall coefficient, and the optical conductivity, in the tilted and nontilted direction. We show, using our optical spectrum calculation for a tilted 3D conical dispersion, that even in an apparently
FIG. 1. (a) The unit cell of TaIrTe$_4$. Purple balls are tellurium atoms. The green and brown octahedra contain, respectively, tantalum and iridium atoms. The metal-metal zigzag chains run along the $a$ axis. (b) Resistivity as a function of temperature, in zero magnetic field and in 14 T. Magnetic field is applied along the $c$ axis. (c) Thermoelectric power or Seebeck coefficient as a function of temperature. The black line shows a linear fit below 60 K, whose slope may be used to extract the Fermi level position. (d) Hall coefficient and Hall mobility as a function of temperature.

simple situation, there is some ambiguity in the parameters that describe this dispersion. Results of our analysis are that the fingerprints of Weyl dispersion may exist on a scale of up to 40 meV.

Single crystals of TaIrTe$_4$ have been grown by a self-flux method. High-purity starting elements in a ratio Ta:Ir:Te=1:1:25 were sealed in a quartz tube under a vacuum of better than 10$^{-5}$ mbar. The mixture was heated to 950 °C (keeping it below the boiling point of Te), allowing the flux to become homogeneous and slowly cooled for several days to 500 °C. By centrifugation of the mixture, shiny, easy to cleave, needlelike single crystals of TaIrTe$_4$ with a longitudinal dimension (along the $b$ axis) of several millimeters were obtained. The structure and composition of the crystals were confirmed using x-ray diffraction and energy-dispersive x-ray spectroscopy. The electrical resistivity and Hall coefficient were measured in a physical property measurement system from Quantum Design as a function of temperature. The sample was measured using a four-probe technique in a longitudinal dimension (along the $a$ axis) of several millimeters.

The crystal structure of TaIrTe$_4$ is shown in Fig. 1(a). Its orthorhombic structure is derived from the structure of WTe$_2$, with a doubling of the $b$ axis [10]. TaIrTe$_4$ has the crystallographic space group $Pmn2_1$, with four formula units per unit cell.

Figures 1(b)–1(d) show the resistivity $\rho$, Seebeck coefficient $S$, Hall coefficient $R_H$, and Hall mobility $\mu_H$, each as a function of temperature. The resistivity in Fig. 1(b) is metallic, with a residual resistivity ratio RRR = $\rho$(300 K)/$\rho$(0 K) = 7.4. This value is much smaller than in WTe$_2$, but comparable to the results in the literature [5,11]. The resistivity is somewhat enhanced in the magnetic field, mostly at low temperature. The effect is much smaller than in WTe$_2$ [12], ZrTe$_5$ [13], or in MoTe$_2$ [14]. Although the three systems are similar to TaIrTe$_4$ to a certain extent, an important difference is that this compound is not nearly as close to a perfect compensation between the electron and hole pockets.

The Seebeck coefficient [Fig. 1(c)] is negative in the entire temperature range. $S(T)$ has a specific shape given by a linear dependence at low temperatures, which is followed by a broad minimum around 120 K, and an increase towards room temperature. The linear $S(T)$ can be understood, in a first approximation, through the Mott expression which describes the diffusion of electrons in a parabolic energy band. The Mott formula relates the Seebeck coefficient to the Fermi level, $S_{\text{Mott}}(T) = k_B T / (\varepsilon_F)$. Through this formula, the experimental $S(T)$ would indicate that the Fermi level is $\varepsilon_F \sim 100$ meV.

Using magnetotransport data [15], the Hall coefficient can be determined as $R_H = \lim_{B \to 0} \rho_{xy}/B$, where $\rho_{xy}$ is a component of the resistivity tensor. The Hall coefficient is shown in Fig. 1(d). $R_H$ is positive with a value in fairly good agreement with the literature [5]. Its temperature dependence suggests there is an increase in the carrier density as the temperature increases. It is known that TaIrTe$_4$ has a complex Fermi surface, composed of two electron and two nested hole pockets [1,11]. Such a multiband nature means that one cannot talk about electron- or hole-dominant conduction. This explains why the Hall coefficient has the opposite sign from the Seebeck coefficient. Figure 1(d) also shows the Hall mobility, $\mu_H = \lim_{B \to 0} \rho_{xy}/(\rho_{xx} B)$. The value of $\mu_H$ is low; the maximum mobility is at 1.8 K and it is equal to 380 cm$^2$/V s.

Overall, the transport coefficients paint a picture of TaIrTe$_4$ as a poor metal, characterized by fairly high values of resistivity, small RRR, high values of the Seebeck coefficient, but with a metallic temperature dependence. The quantum
oscillation measurements, shown in the Supplemental Material [15], confirm that the Fermi surface is made out of several pockets [11]. Through the transport measurements, we are able to access the intraband excitations, described by the Drude response. However, it is not possible based on transport alone to find the scattering rate, nor to identify if it is the carrier density, or the scattering rate, that causes most of the temperature dependence of the resistivity.

To address these questions, we resort to optical spectroscopy. The scattering rate and the carrier density are separated in the optical conductivity as the width and strength of the Drude peak. The comparative advantage with respect to the transport measurements is not only the ability to disentangle different parameters of the Drude response, but also the capability to access the excitations between different energy bands. These interband excitations directly probe the energy band dispersion through its joint density of states (JDOS) [16].

The reflectance of TaIrTe$_4$ at seven different temperatures is shown in Fig. 2(a). The response is decidedly metallic, with $R \to 1$ in the low-energy limit, $\omega \to 0$. The temperature dependence is particularly strong in the far-infrared range, and similar to what was observed in WTe$_2$ or MoTe$_2$ [17,18]. A single strong, sharp phonon mode is detected at 24 meV (200 cm$^{-1}$). Through Kramers-Kronig relations, one can determine the complex optical conductivity $\sigma = \sigma_1 + i\sigma_2$. The real part of this response function, $\sigma_1$, leads to absorption of radiation by the material. This component is of particular interest, because it is directly proportional to the JDOS. On the contrary, the imaginary component $\sigma_2$ does not result in absorption, but only leads to a phase lag.

The real part of the optical conductivity, $\sigma_1(\omega)$, is shown in Fig. 2(b) for the low photon energies, and in Fig. 2(c) for the broad energy range. The inset of Fig. 2(b) shows the imaginary component $\sigma_2(\omega)$, and similar to what was observed in WTe$_2$ or MoTe$_2$ [17,18]. The Drude component strongly narrows at low temperatures, similar to what is generally seen in similar compounds [16–18]. The scattering rate is shown in the inset of Fig. 1(b). The Drude component strongly narrows at low temperatures, similar to what is generally seen in similar compounds [16–18]. The scattering rate is shown in the inset of Fig. 3(a) as a function of temperature. Expectedly, it increases with temperature.

In $\sigma_1$, low-energy interband excitations dominate the optical response between 10 and 200 meV. These excitations leave a characteristic signature which is intimately related to the JDOS, and may leave imprints of conical dispersion around the Weyl nodes. The nearly linear dependence of $\sigma_1(\omega)$ extrapolates into a finite value at $\omega \to 0$. We will show later that such a finite offset is indeed expected for a tilted conical dispersion. In Fig. 2(c), the high-energy excitations are also visible, centered at 0.2, 0.4, and 1.8 eV. Due to the complex band structure, it is not possible to assign these excitations to specific features of the band structure [1,3].

Intraband excitations can be described by the Drude component, which may be characterized by a plasma frequency $\omega_{p,\text{Drude}}$ and a scattering rate $1/\tau$. The narrow Drude component in TaIrTe$_4$ is well distinguished in our measurements. This is seen in Fig. 3(a), which shows $\sigma_1(\omega)$ in the far-infrared region. The dynamical conductivity is consistent with the $\sigma_{dc}$ values extracted from the resistivity measurement in Fig. 1(b). The Drude component strongly narrows at low temperatures, similar to what is generally seen in similar compounds [16–18]. The scattering rate is shown in the inset of Fig. 3(a) as a function of temperature. Expectedly, it increases with temperature.

At low temperatures, the Drude plasma frequency is $\omega_{p,\text{Drude}} = 0.1$ eV, and the Drude scattering rate is 2.6 meV. For comparison, similarly small scattering rates $\hbar/\tau \lesssim 1$ meV were found in the related compounds [17,18] MoTe$_2$ and WTe$_2$, as well as in other candidate topological semimetals [16,19–21]. Such a small value is characteristic of a compound with a small Fermi surface, resulting in a small $k$ space available for intraband scattering.

We distinguish three parts in $\sigma_1$ at low energies: a narrow Drude contribution, a sharp phonon contribution, and an interband part. Separating the Drude and phonon contributions allows us to access the interband optical response: $\sigma_1(\text{interband}) = \sigma_1 - \sigma_1(\text{Drude}) - \sigma_1(\text{phonon})$. The premise is that at low temperatures this interband response contains a signature of tilted conical dispersion linked to Weyl nodes. We perform the low-energy optical analysis under certain assumptions.
First, there are multiple bands at the Fermi level, as inferred by DFT, but there are no interband transitions below 50 meV (400 cm\(^{-1}\)) except from those arising within the tilted cone. Second, the sum of all band contributions to the conductivity is contained in the \(\sigma_{dc}\) and \(\tau\) of the single Drude Lorentzian. Third, the footprint of any linear-dispersion-like signature is found in the data interval from 15 to 35 meV, where we see a linearlike conductivity [see Fig. 3(b)].

To identify the response from a possible Weyl dispersion, a numerical calculation can be done, and the parameters used to describe the Weyl cones can be adapted to best describe the experimental optical conductivity. The Hamiltonian for a tilted Weyl cone is

\[ \hat{H}_0 = \hbar w k \sigma_z + \hbar v k \cdot \sigma, \]

where \(\sigma_x,\sigma_y,\sigma_z\) are Pauli matrices, \(\mathcal{I}\) the identity operator, \(v\) the Dirac velocity, and \(w\) the tilt velocity. Diagonalizing the Hamiltonian gives its eigenvalues for conduction \(c\) and valence \(v\) bands, \(\varepsilon_n^{c,v} = \hbar w k_z \pm \hbar v |k|\). Using these eigenvalues one can numerically calculate the optical conductivity [15]. We take into account four Weyl nodes, as given by DFT. The result is given in Fig. 3(b) in red and blue lines, with the following parameters: Fermi level, with respect to the tip of the cone, \(\varepsilon_F = 4.3\) meV, tilt of the cone \(\gamma = w/v = 0.37\), and Fermi velocity \(v = 1.1 \times 10^5\) m/s. The parameter \(\gamma < 1\) that we obtain describes an undertilted Weyl cone. This model can describe our data up to \(\sim 40\) meV. Although favored by the DFT, the undertilted Weyl scenario (\(\gamma > 1\)) gives a significantly different shape of the interband part, incompatible with our experimental data. The dotted green line in Fig. 3(b) shows such a fit with undertilted Weyl cones. The best fit obtained in this regime gives \(\varepsilon_F = 12.5\) meV, tilt of the cone \(\gamma = w/v = 2.8\), and Fermi velocity \(v = 0.55 \times 10^4\) m/s. The discrepancy between the measured and modeled interband conductivity grows with photon energy.

Undertilted Weyl cones give a linear response above the Pauli edge, extrapolating to zero at \(\omega = 0\). In contrast, overtilted Weyl cones have a more complex response, which is nonlinear above the Pauli edge.

The optical conductivity is consistent with the calculated interband conductivity within a tilted conical dispersion. This cannot be taken as a smoking gun of Weyl dispersion, as we cannot exclude other dispersions which would result in a similar interband conductivity. For example, an energy-dispersive nodal line at the Fermi level would produce a similar response, with a quasilinear dependence of \(\sigma_1\), followed by a plateau. This would be consistent with Ref. [2] which shows the coexistence of twelve Weyl points and dispersive nodal lines in the low energy band structure of TaIrTe\(_4\). However, if the band structure indeed contains four Weyl cones at low energies, then our result indicates that their energy scale is less than 40 meV.

The same effective Hamiltonian model can be used to calculate the Seebeck coefficient and the Hall constant. These are shown together in Fig. 3(c). Both are calculated assuming that the Fermi level is \(\varepsilon_F = 4.3\) meV, which we obtained from the undertilted Weyl cone model. While there is some agreement in the temperature dependence for both coefficients, quantitatively the model overestimates both \(S\) and \(R_H\). The amplitude disagreement is likely caused by the multiband nature of TaIrTe\(_4\). The important takeaway is the shape of \(S\) and \(R_H\), which is determined in our model by the thermal shift of the chemical potential, and not by the scattering rate \(1/\tau\).

To further connect the dc transport and the optical conductivity to the effective model, we look at the carrier mobility. From the magnetotransport data, we determined the Hall mobility as shown in Fig. 1(d). At finite temperatures, \(\mu_H\) differs from the simple mobility \(\mu = \sigma_{dc}/(en)\), where \(n\) is the total carrier density. At \(T = 0\), these two become equal, and in a 3D Dirac case (equivalent to the undertilted Weyl case),
they are given by [15]

\[ \mu = \frac{e\tau n_s}{m_e n} = \frac{e\tau m_e v^2}{m_e \varepsilon_F}. \]

Using our optical data as a source of \( v, \varepsilon_F, \) and \( \tau, \) we get \( \mu = 185 \text{ cm}^2/(\text{V s}). \) This is equal to roughly half the experimental value, which we judge as a reasonably good agreement. The relatively small mobility can thus be traced back to the small ratio \( m_e v^2/\varepsilon_F = 0.16. \) It is interesting that our effective model gives a much better estimate of mobility than that of the Hall coefficient \( R_H, \) in comparison to the experimental values. This is related to the way in which the small energy scale \( m_e v^2 \) enters each coefficient. While in \( R_H \) it is present directly, in the mobility \( \mu \) it only appears through the ratio \( m_e v^2/\varepsilon_F. \)

Although generally a complex quantity [15], the Seebeck coefficient is simplified dramatically for a system with linear bands, when the effective Fermi velocity is constant. In such a case, \( S = (1/e) \partial \mu(T)/\partial T, \) where \( \mu(T) \) is the chemical potential [15]. This generically gives \( S(T) \propto T \) at low temperatures, after which \( S(T) \) reaches an extremum value, and then it decreases in absolute value. One interesting consequence of the above simple expression is that the minimum of \( S(T) \) depends linearly on the Fermi energy, measured from the tip of the cone (or the Weyl node). In the case of TaIrTe\(_4\), the experimental thermopower [Fig. 1(c)] qualitatively resembles the calculated \( S(T) \), shown in Fig. 3(c). The experimental minimum of \( S(T) \) is observed at 100 K, and its absolute value is about five times smaller than in the calculation. Once again it is important to recall that TaIrTe\(_4\) is a multiband system. While its optical conductivity may well be dominated by the interband transitions arising within the tilted cones, the intraband channel will contain contributions from all the bands that cross the chemical potential, as shown schematically in the inset of Fig. 3(c). All these intraband excitations are reflected in the transport coefficients. Specifically, we see that \( S(T) \) cannot be described by a simple linear-dispersion term shown in Fig. 3(c), and multiband contributions lead to a smaller experimental thermopower. Similarly, if other bands at the Fermi level are considered, \( R_H \) will be lower than what our model predicts, bringing it in closer agreement to the experiment.

In conclusion, we have determined the optical conductivity of a candidate type-II Weyl semimetal, TaIrTe\(_4\). Through a combined use of detailed infrared spectroscopy and effective modeling, we show that the low-energy dynamical conductivity is broadly consistent with a tilted conical dispersion. This dispersion may explain the interband response at low energies, below 40 meV. The Fermi level may be within those conically dispersing bands.

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